

# Testing the Origins of Neutrino Mass with Supernova Neutrino Time Delay

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**Based on arXiv: 2404.17352 [hep-ph] (Phys.Rev.Lett. 133 (2024) 12, 121802)**

**In collaboration with: Shao-Feng Ge & Alexei Y. Smirnov**



李政道研究所  
TSUNG-DAO LEE INSTITUTE

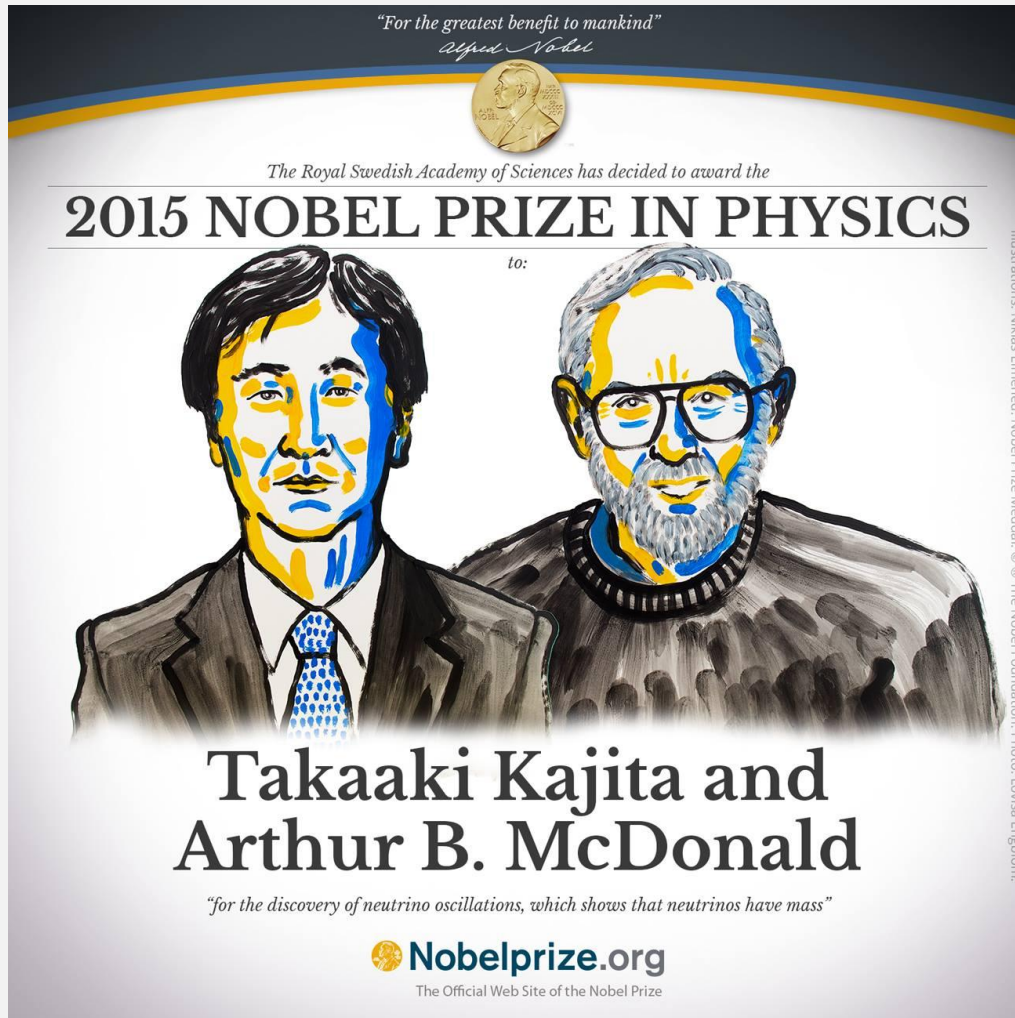


EuCAPT  
Astroneutrino Theory Workshop 2024  
Prague, Czech Republic

**EuCAPT @ Prague, 2024 Sep. 24**



# • Evidence of Neutrino Mass

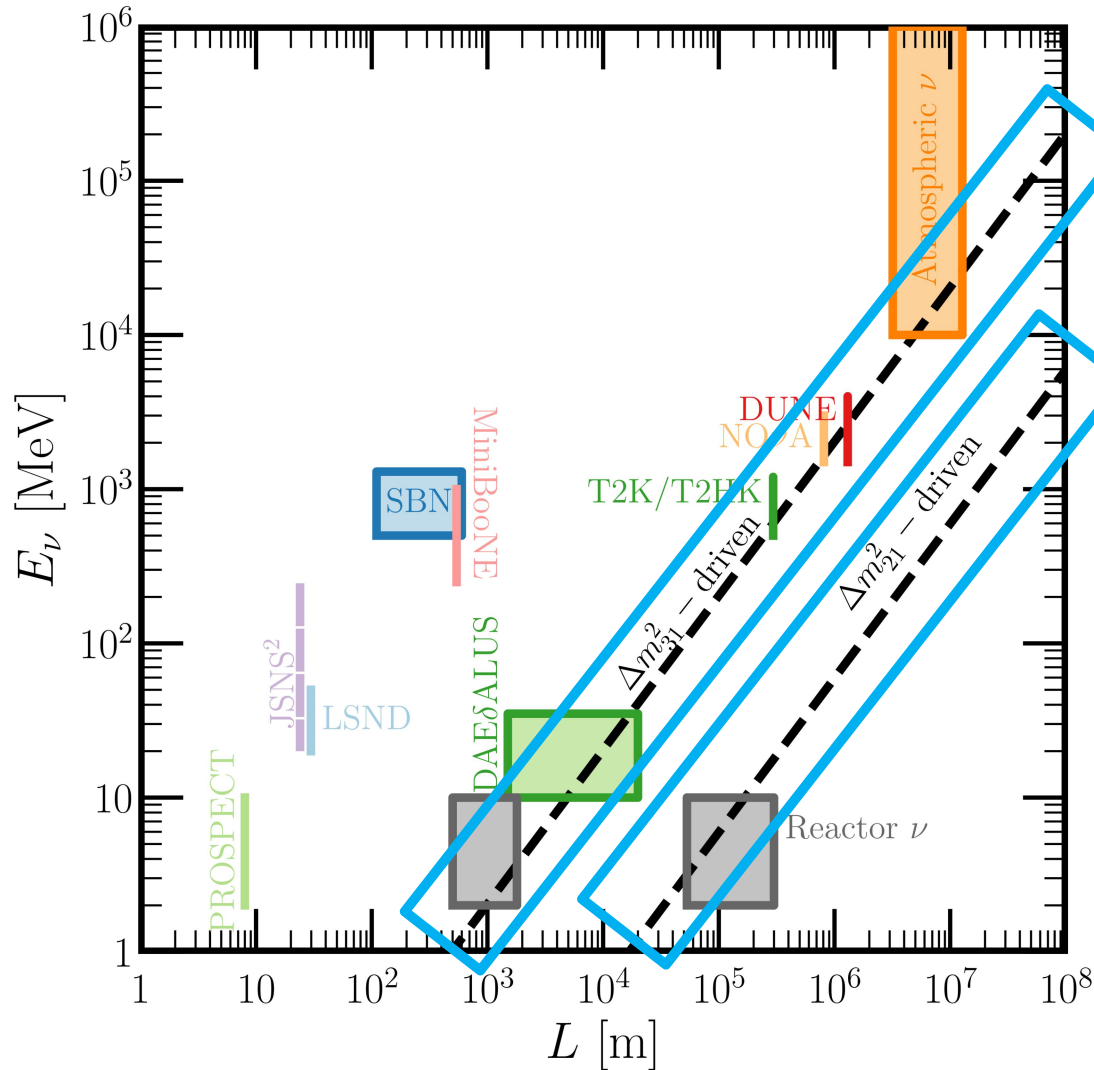


*"for the discovery of neutrino oscillations, which shows that neutrinos have mass"*

# Evidence of Neutrino Mass

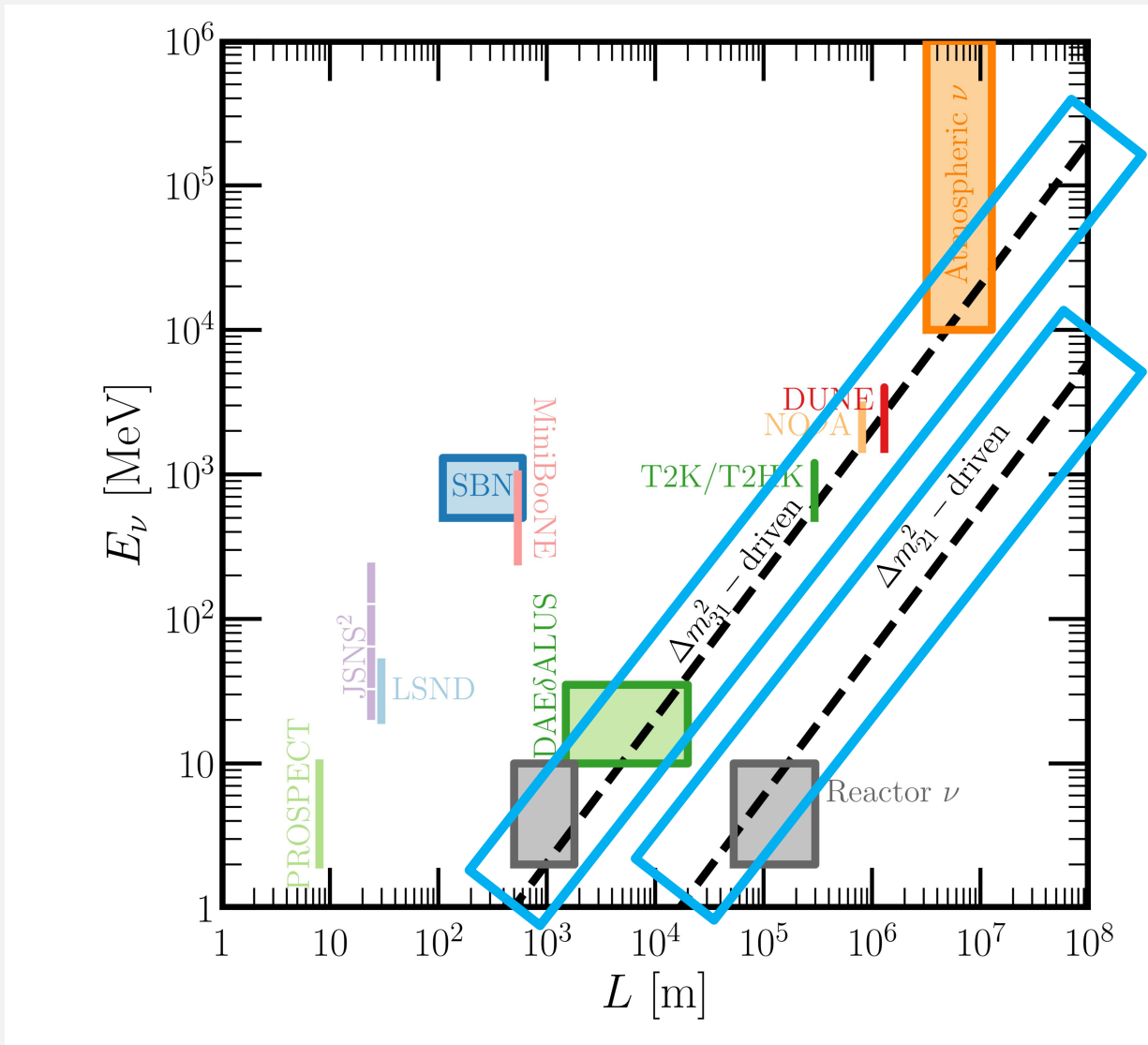
*[see Prof. Smirnov & Prof. Schwetz's lectures]*

Neutrino oscillations have  $\Delta m_{ij}^2 / 2E_\nu$  dependence



R. Harnik, K. Kelly, P. Machado  
*arXiv: 1911.05088*

# Evidence of Neutrino Mass



*[see Prof. Smirnov & Prof. Schwetz's lectures]*

Neutrino oscillations have  $\Delta m_{ij}^2/2E_\nu$  dependence



Q: What's the origin of  $\Delta m_{ij}^2$ ?

R. Harnik, K. Kelly, P. Machado  
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# • Neutrino Mass Origin I: vacuum mass

## Vacuum Neutrino Mass

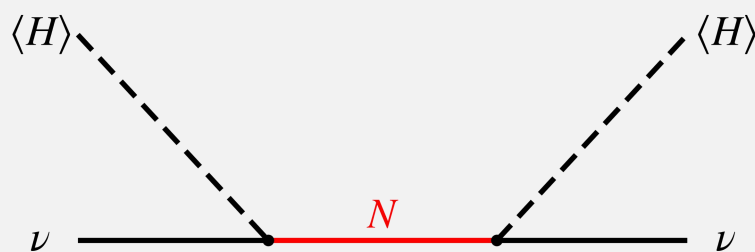
*[see Prof. Malinsky  
& Prof. Deppisch's lectures]*

Type-I seesaw

Type-II seesaw

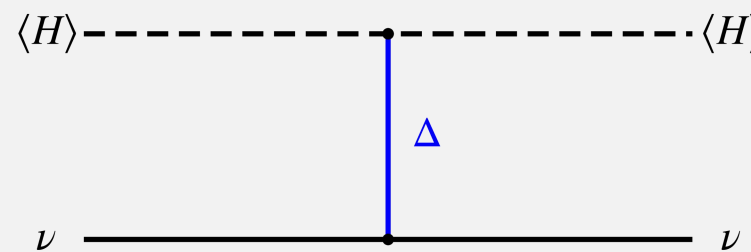
Type-III seesaw

...



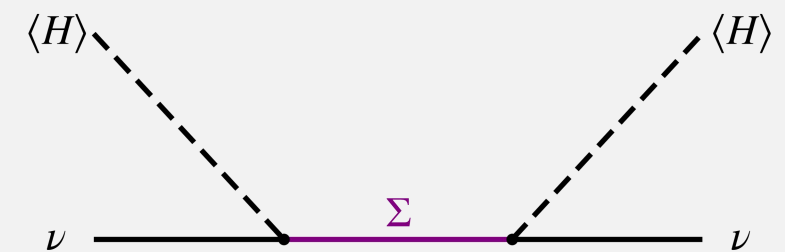
$$M_\nu = -\frac{1}{2} Y_\nu \frac{v^2}{M_R} Y_\nu^T$$

*P. Minkowski  
T. Yanagida  
M. Gell-Mann*



$$M_\nu = \lambda_\Delta Y_\Delta \frac{v^2}{M_\Delta}$$

*M. Magg & C. Wetterich  
G. Lazarides, Q. Shafi, & C. Wetterich  
R. Mohapatra & G. Senjanovic*



$$M_\nu = -\frac{1}{2} Y_\Sigma \frac{v^2}{M_\Sigma} Y_\Sigma^T$$

*R. Foot, H. Lew, X.-G. He, & G.C. Joshi  
E. Ma*

# • Neutrino Mass Origin I: vacuum mass

## Vacuum Neutrino Mass

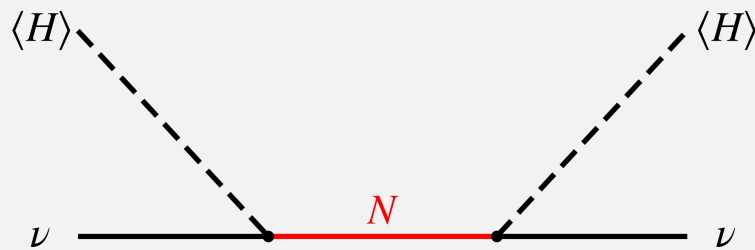
*[see Prof. Malinský  
& Prof. Deppisch's lectures]*

Type-I seesaw

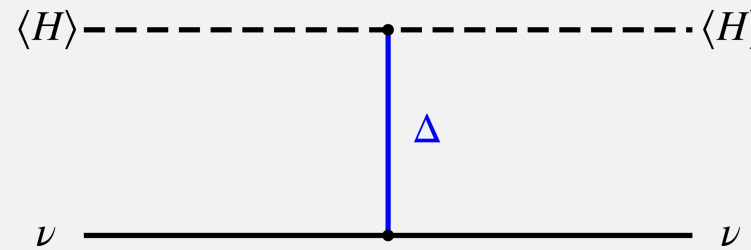
Type-II seesaw

Type-III seesaw

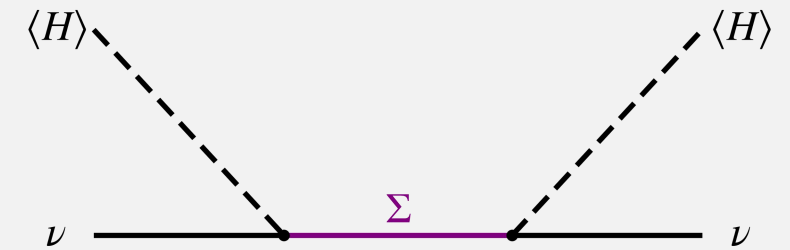
...



$$M_\nu = -\frac{1}{2} Y_\nu \frac{v^2}{M_R} Y_\nu^T$$



$$M_\nu = \lambda_\Delta Y_\Delta \frac{v^2}{M_\Delta}$$



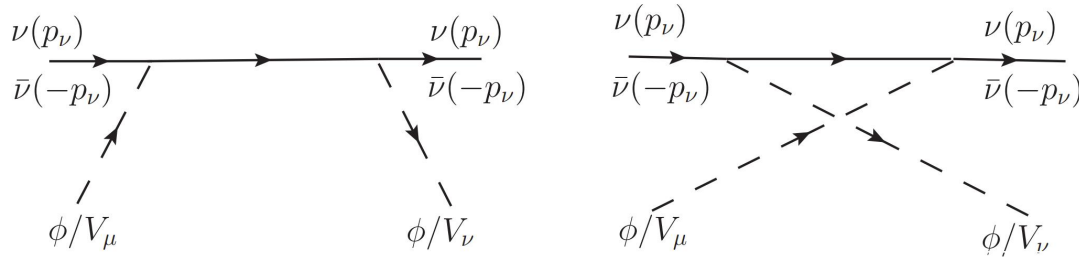
$$M_\nu = -\frac{1}{2} Y_\Sigma \frac{v^2}{M_\Sigma} Y_\Sigma^T$$

$$m_{\text{vac}}^2 = A$$

# Neutrino Mass Origin II: dark mass

## Dark Neutrino Mass

- The **forward scattering** with the **DM background**



- Due to  **$1/E_\nu$  dependence**, the **dark potential** is promoted to mass correction

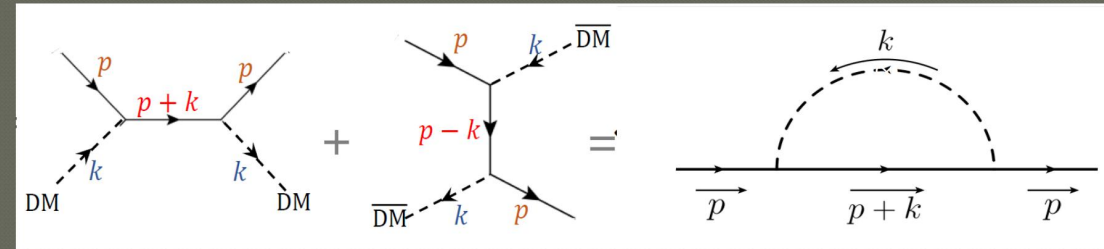
$$H = \frac{M^2}{2E_\nu} - \frac{1}{E_\nu} \sum_j y_{\alpha j} y_{j\beta}^* \frac{\rho_\chi}{m_\phi^2} \equiv \frac{M^2 + \delta M^2}{2E_\nu}$$

*S.-F. Ge & H. Murayama, arXiv:1904.02518*

*S.-F. Ge, PoS NuFact 2019, 108 (2020)*

*S.-F. Ge, J. Phys. Conf. Ser. 1468, no.1,012125 (2020)*

- Coherent forward scattering=medium one-loop correction



- Massless neutrinos get the dispersion  $E = \sqrt{p^2 + \delta m^2}$ , that is,  $E \approx p + \frac{\delta m^2}{2p}$  for  $p^2 \gg \delta m^2$ .
- Neutrino oscillation from flavor-dependent couplings:

$$\mathcal{L}' = g_{\alpha\beta} \phi \bar{\nu}_\alpha \nu_\beta + h.c. \Rightarrow (\delta m^2)_{\alpha\beta} = (g g^\dagger)_{\alpha\beta} \frac{\rho_\phi}{m_\phi^2}$$

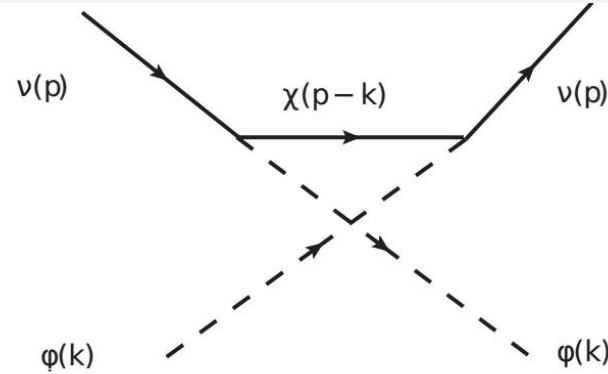
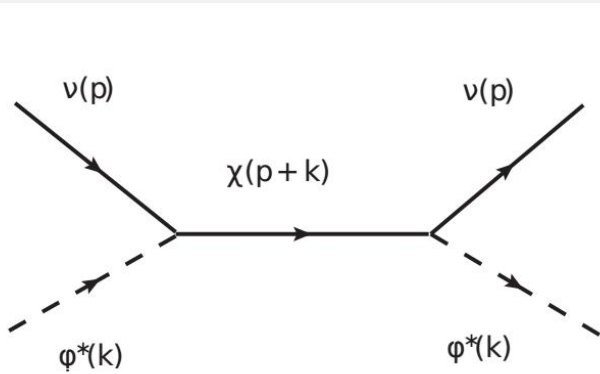
*K. Y. Choi, E. J. Chun & J. Kim, arXiv:1909.10478*

*K. Y. Choi, E. J. Chun & J. Kim, arXiv:2012.09474*

*E. J. Chun, talks@TDLI*

# Neutrino Mass Origin II: dark mass

## Dark Neutrino Mass



Mass depends on the DM density

$$m_{\text{dark}}^2(x) \propto \rho_{\phi}$$

Introduce the effective or refractive mass squared as

$$V = m_{\text{ref}}^2 / 2E$$

$$m_{\text{ref}}^2 = 2EV$$

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$$m_{\text{ref}}^2 = m_{\text{as}}^2 \frac{y(y - \varepsilon)}{y^2 - 1}$$

$$m_{\text{as}}^2 = \sum_k g_{\alpha k} g_{\beta k}^* \frac{\rho_{\phi}}{m_{\phi}^2}$$

*M. Sen and A. Y. Smirnov, arXiv:2306.15718*  
*A. Y. Smirnov, talks@MAYORANA Workshop*



# • Neutrino Mass Origins Comparison

Vacuum Neutrino Mass:  $m_{\text{vac}}^2 = A$

vs.

Dark Neutrino Mass:  $m_{\text{dark}}^2(x) \propto \rho_\phi$

# • Neutrino Mass Origins Comparison

Vacuum Neutrino Mass:  $m_{\text{vac}}^2 = A$

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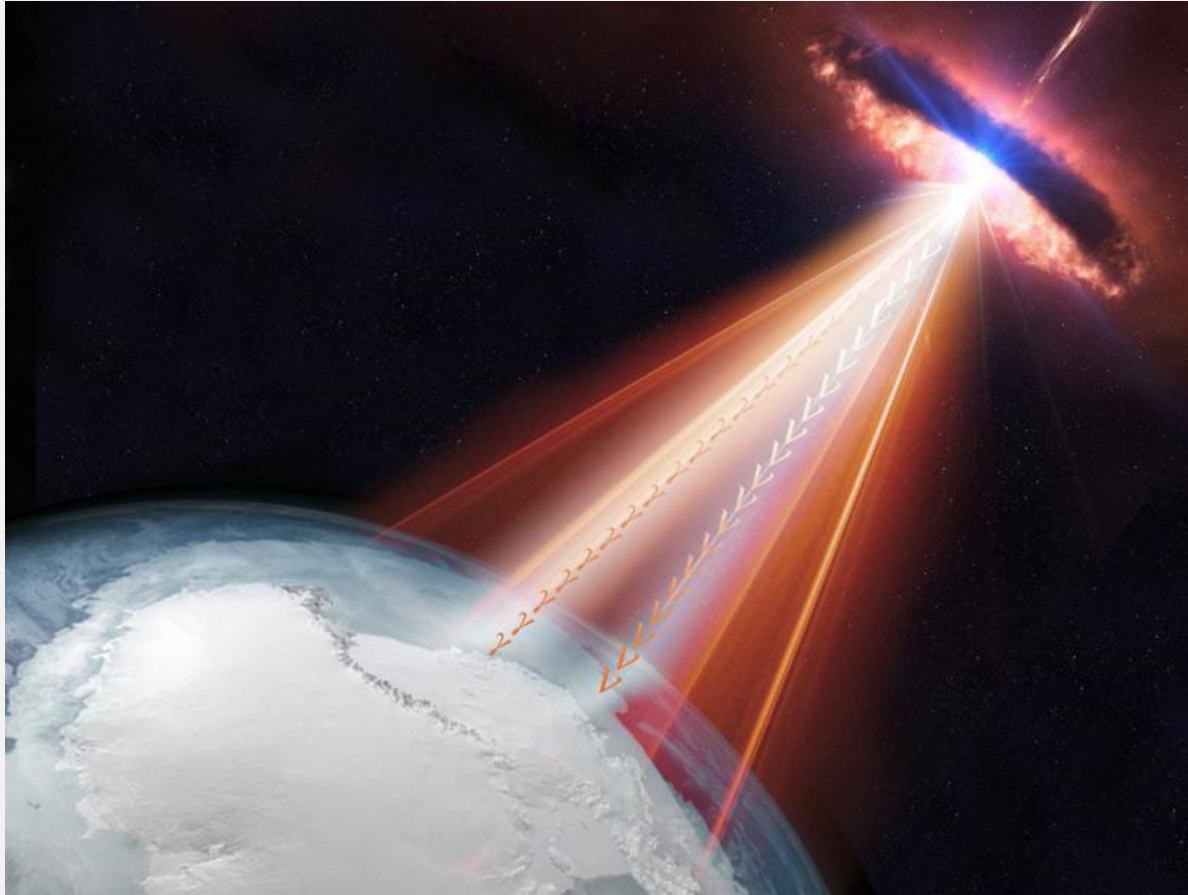
Dark Neutrino Mass:  $m_{\text{dark}}^2(x) \propto \rho_\phi$

Can we distinguish these two origins ?

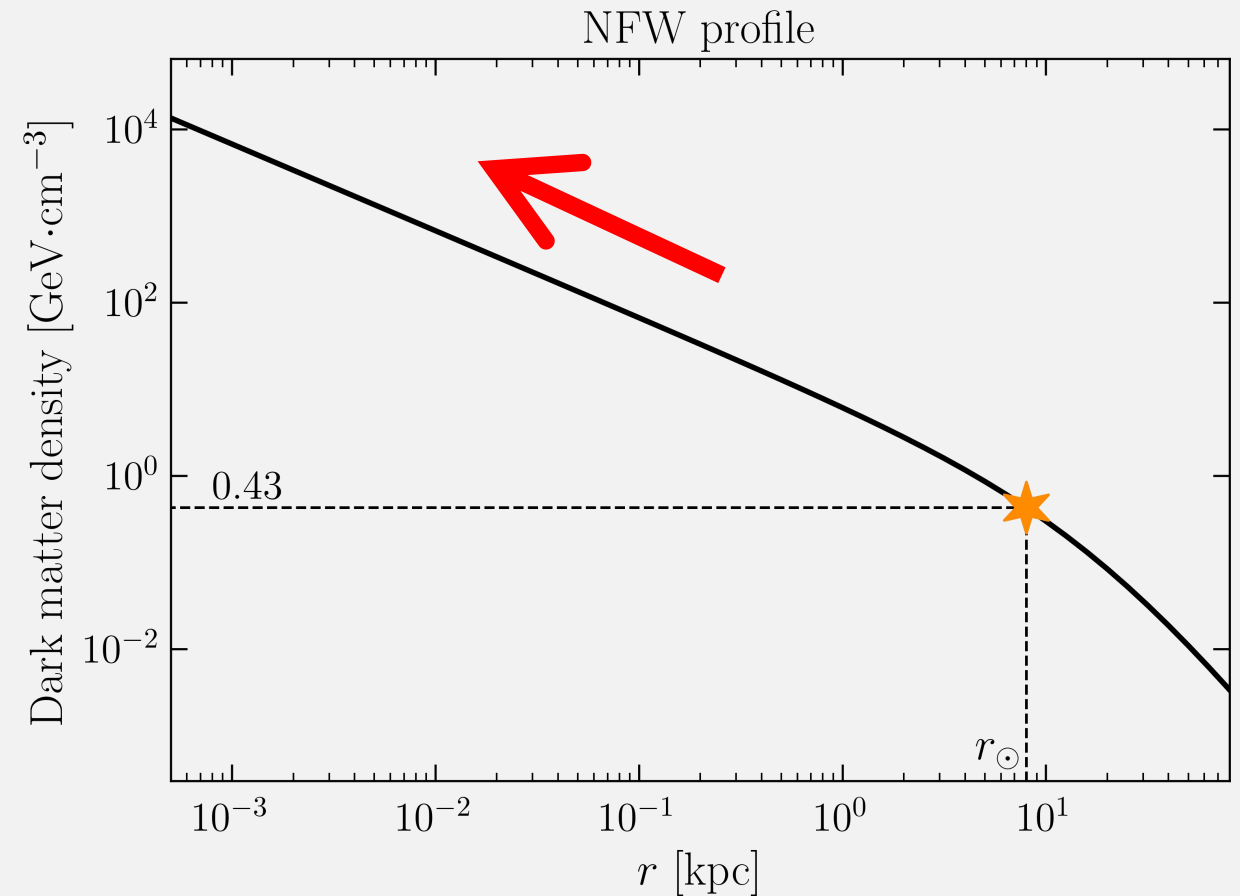
# Large Scales

Yes! Look into larger scales

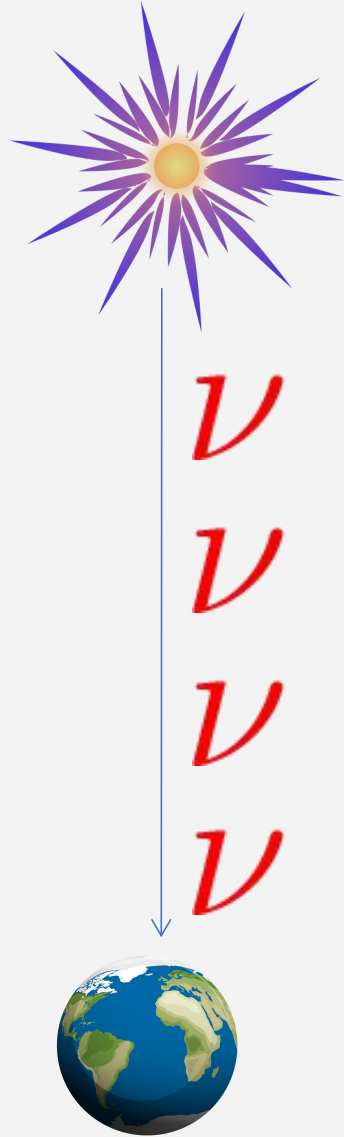
[see Prof. Dev's lecture]



Credit: IceCube/NASA



# Supernova Neutrino Time Delay



Neutrinos are massive

group velocity:

$$v = \frac{p}{E} = \sqrt{1 - \frac{m^2}{E^2}} \approx 1 - \frac{m^2}{2E^2}$$

time delay (vacuum mass):

$$\Delta t \equiv \frac{D}{v} - D = \frac{m^2}{2E^2} D = 5.14 \text{ ms} \left( \frac{m}{\text{eV}} \right)^2 \left( \frac{10 \text{ MeV}}{E} \right)^2 \frac{D}{10 \text{ kpc}}$$

# • Supernova Neutrino Time Delay

How about the dark mass?

$$\Delta t_{\text{dark}} \equiv \int_{\mathbf{x}_*}^{\mathbf{x}_\odot} \left( \frac{1}{v(\mathbf{x})} - 1 \right) |d\mathbf{x}| \approx \int_{\mathbf{x}_*}^{\mathbf{x}_\odot} (1 - v(\mathbf{x})) |d\mathbf{x}|$$

$$1 - v(\mathbf{x}) = \frac{m_{\text{dark}}^2(\mathbf{x}_\odot)}{2E^2} \frac{\rho_\phi(\mathbf{x})}{\rho_\phi(\mathbf{x}_\odot)}$$

$$\Delta t_{\text{dark}} = \frac{m_{\text{dark}}^2(\mathbf{x}_\odot) D}{2E^2} \frac{\int_{\mathbf{x}_*}^{\mathbf{x}_\odot} \rho_\phi(\mathbf{x}) |d\mathbf{x}|}{D \rho_\phi(\mathbf{x}_\odot)} \equiv \Delta t_\odot \frac{\overline{\rho_\phi}(\mathbf{x})}{\rho_\phi(\mathbf{x}_\odot)}$$

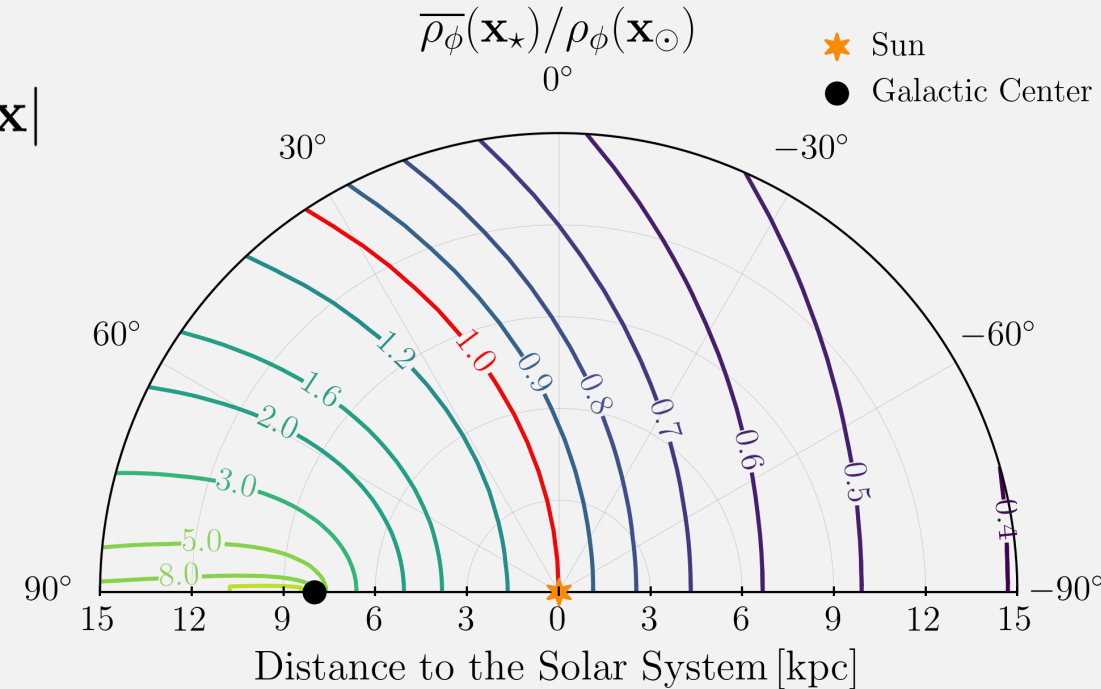
# Supernova Neutrino Time Delay

How about the dark mass?

$$\Delta t_{\text{dark}} \equiv \int_{\mathbf{x}_*}^{\mathbf{x}_\odot} \left( \frac{1}{v(\mathbf{x})} - 1 \right) |d\mathbf{x}| \approx \int_{\mathbf{x}_*}^{\mathbf{x}_\odot} (1 - v(\mathbf{x})) |d\mathbf{x}|$$

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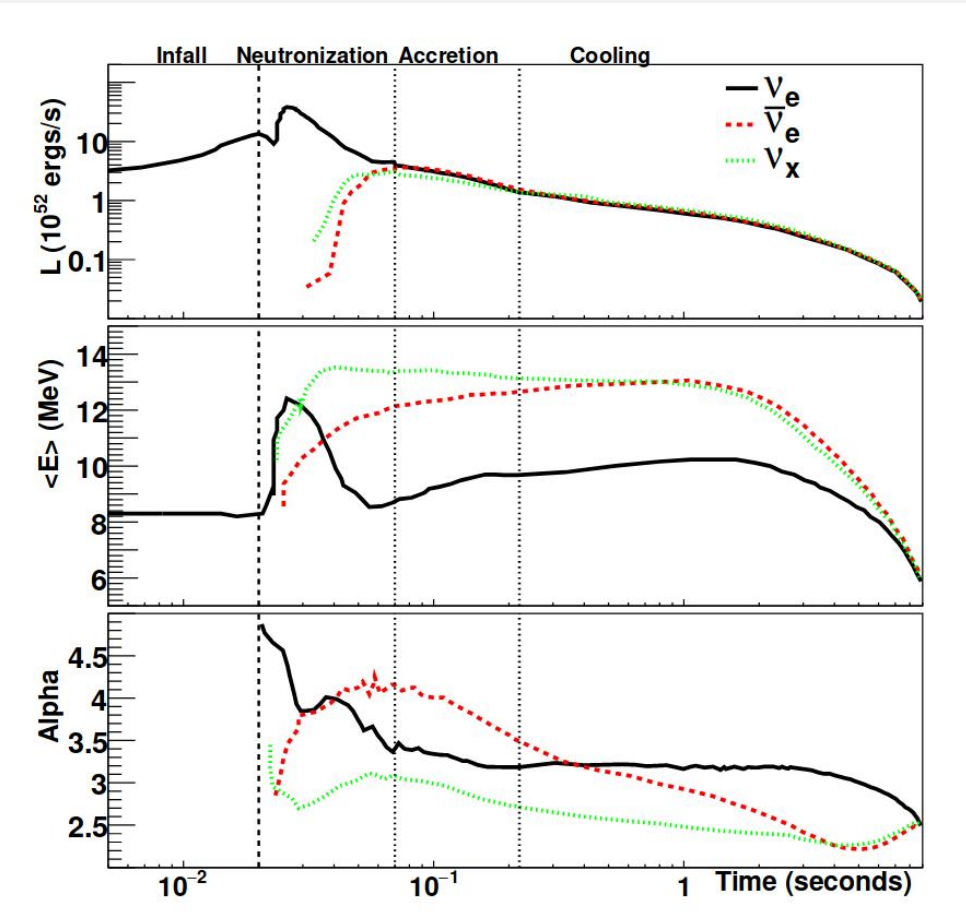
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Ge, CFK, Smirnov  
arXiv: 2404.17352

differed by this factor

# Supernova Neutrino Production & Detection



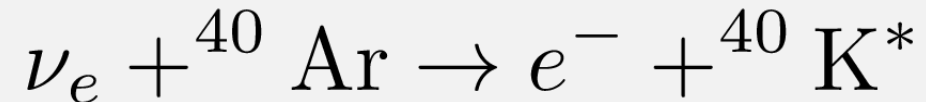
*DUNE Collaboration*  
*arXiv: 2008.06647*

❖  $\nu_e$  SN burst production (Garching model):

$$\Phi_{\nu\beta}^0(t_e, E_\nu) = \frac{L_{\nu\beta}(t_e)}{\langle E_{\nu\beta}(t_e) \rangle} \varphi_{\nu\beta}(t_e, E_\nu)$$

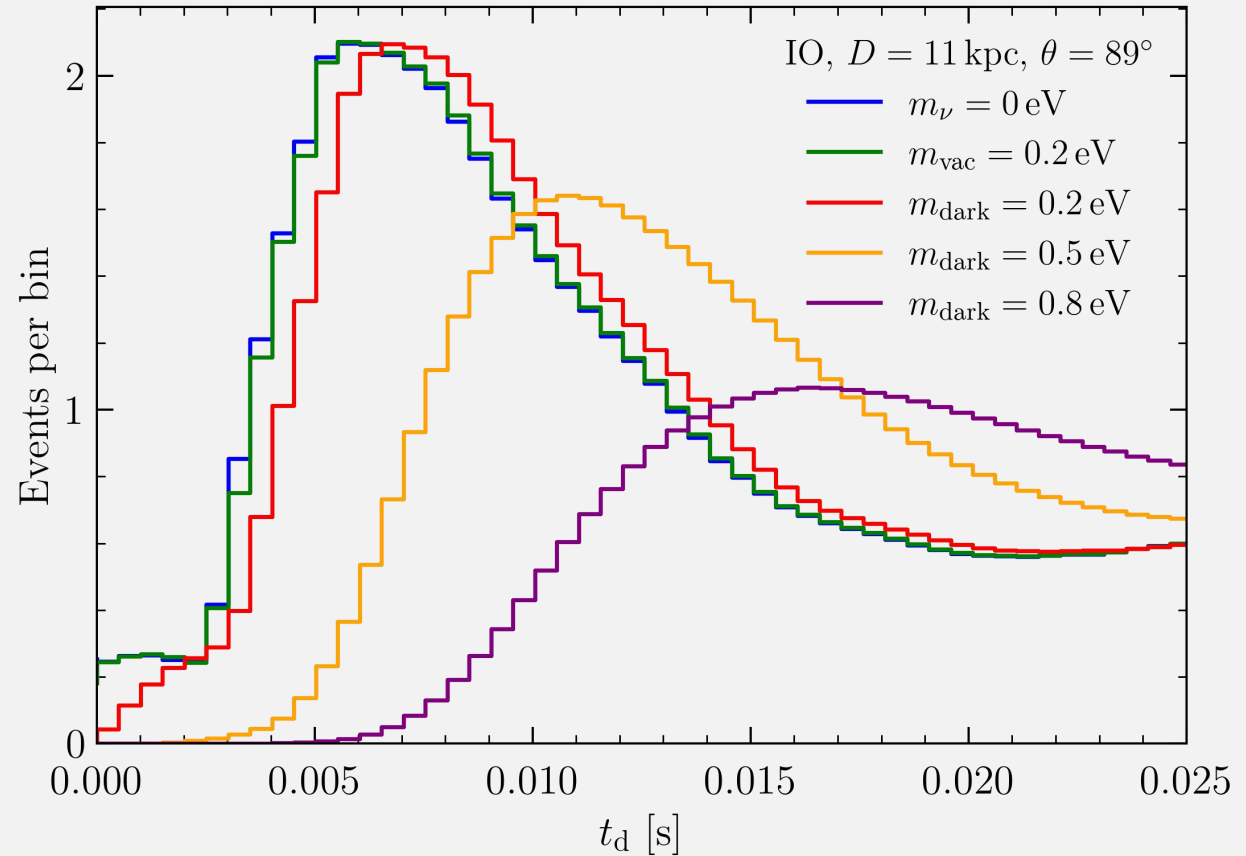
$$\varphi_{\nu\beta}(t_e, E_\nu) \equiv \xi_\beta(t_e) \left( \frac{E_\nu}{\langle E_{\nu\beta}(t_e) \rangle} \right)^{\alpha_\beta(t_e)} e^{-\frac{(\alpha_\beta(t_e)+1)E_\nu}{\langle E_{\nu\beta}(t_e) \rangle}}$$

❖  $\nu_e$  SN burst detection at DUNE:



# Time Distribution

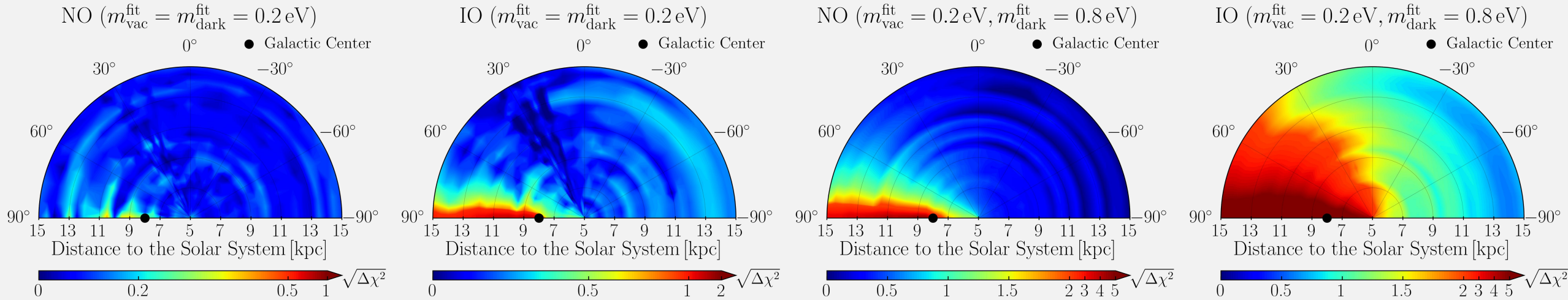
The time distribution becomes wider as the neutrino mass increases



*Ge, CFK, Smirnov*  
*arXiv: 2404.17352*



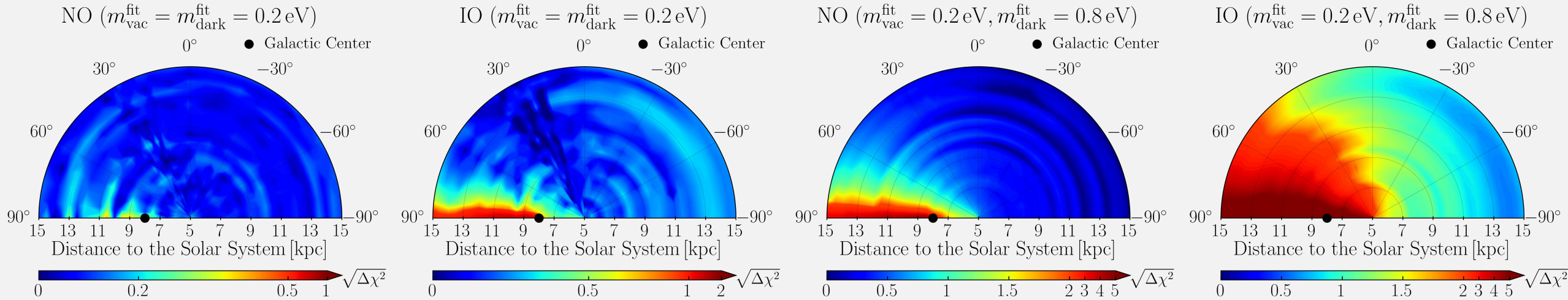
# Sensitivities



❖ **Location dependence:** the sensitivity is enlarged by measuring neutrinos around the galaxy center

*Ge, CFK, Smirnov*  
*arXiv: 2404.17352*

# Sensitivities



❖ **Location dependence:** the sensitivity is enlarged by measuring neutrinos around the galaxy center

❖ **Neutrino mass ordering dependence:** sensitivity for normal ordering (NO) is reduced by MSW effect

*Ge, CFK, Smirnov  
arXiv: 2404.17352*

# Summary

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- The dark neutrino mass is space-time dependent due to the dark matter distribution
- The supernova neutrino time delay can be much enhanced around galaxy center
- The neutrino mass origins (vacuum or dark mass) can be tested by measuring supernova neutrinos
- Better test can be done by measuring neutrinos from supernovae at different locations

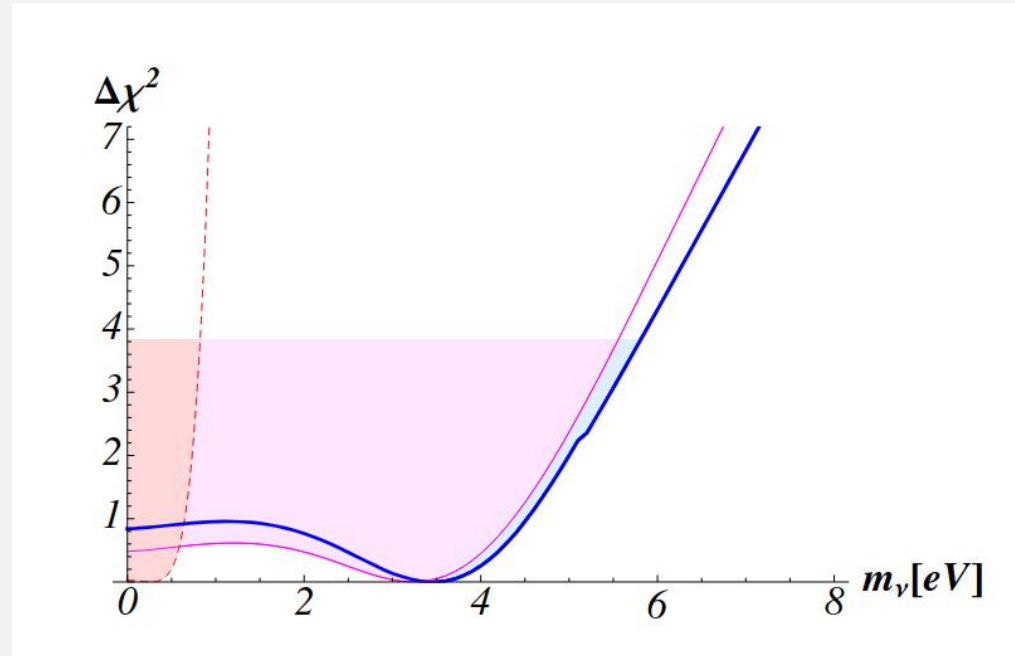
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*Thank you for your attention!*

## SN1987A



The minimum is located at  $\sim 3.5$  eV, although not statistically significant

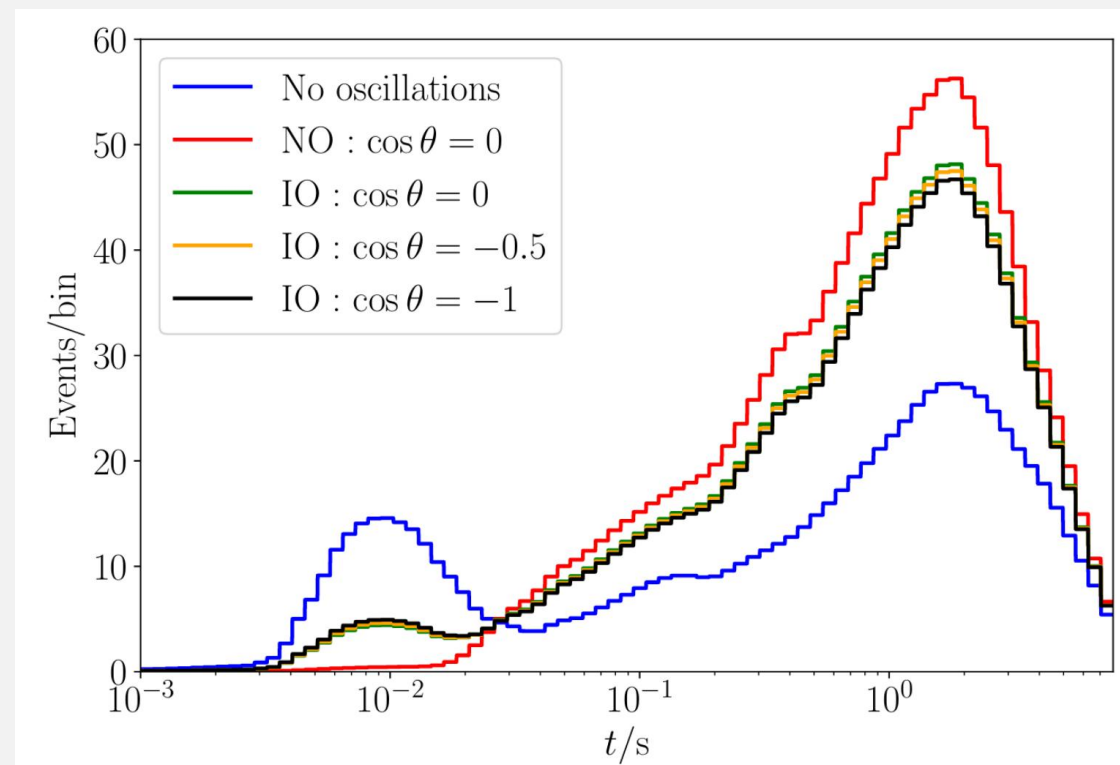
*G. Pagliaroli, F. Rossi-Torres, & F. Vissani*  
*arXiv:1002.3349*

## MSW effect

$$\Phi_{\nu_e} = p\Phi_{\nu_e}^0 + (1 - p)\Phi_{\nu_x}^0$$

$$p = |U_{e3}|^2 \approx \sin^2 \theta_{13}, \text{NO}$$

$$p \approx |U_{e2}|^2 \approx \sin^2 \theta_{12}, \text{IO}$$



*F. Pompa, F. Capozzi, O. Mena, & M. Sorel*  
*arXiv:2203.00024*

## neutrino group velocity

$$E_\nu = p_\nu + V, v \equiv \frac{dE_\nu}{dp_\nu}$$

$$1 - v(\mathbf{x}) = \frac{m_{\text{dark}}^2(\mathbf{x}, p_\nu)}{2p_\nu^2} - \frac{1}{2p_\nu} \frac{dm_{\text{dark}}^2(\mathbf{x}, p_\nu)}{dp_\nu}$$