

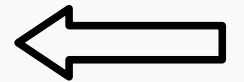
Detecting the Cosmic Neutrino Background

Jack Shergold



What we will cover

- Lecture 1: Introduction to the CvB
- Lecture 2: Direct detection proposals
- Lecture 3: Indirect detection, constraints and future prospects

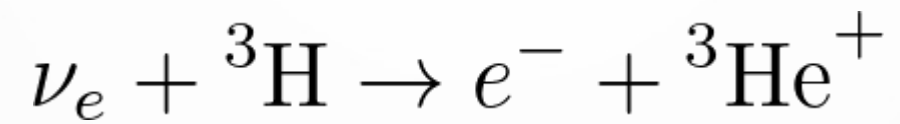


Contents

- Recap ←
- Indirect detection proposals:
 - Cosmic ray attenuation
 - Exclusion principle
- Constraints and sensitivities
- What's next?

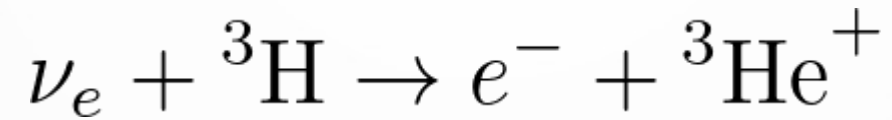
Recap

- PTOLEMY:



Recap

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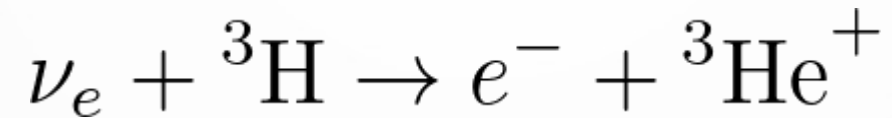
- Event rate:

$$\Gamma \sim 4y^{-1}$$

$$\Delta \leq 2m_\nu$$

Recap

- PTOLEMY:



- Event rate:

$$\Gamma \sim 4 \text{y}^{-1}$$

$$\Delta \leq 2m_\nu$$

- Uncertainty principle causes issues

Recap

- Coherent scattering:

$$\nu + X \rightarrow \nu + X$$

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$$a_\nu \simeq 10^{-28} \left(\frac{m_\nu}{0.1 \text{ eV}} \right)^2 \text{ cm s}^{-2}$$

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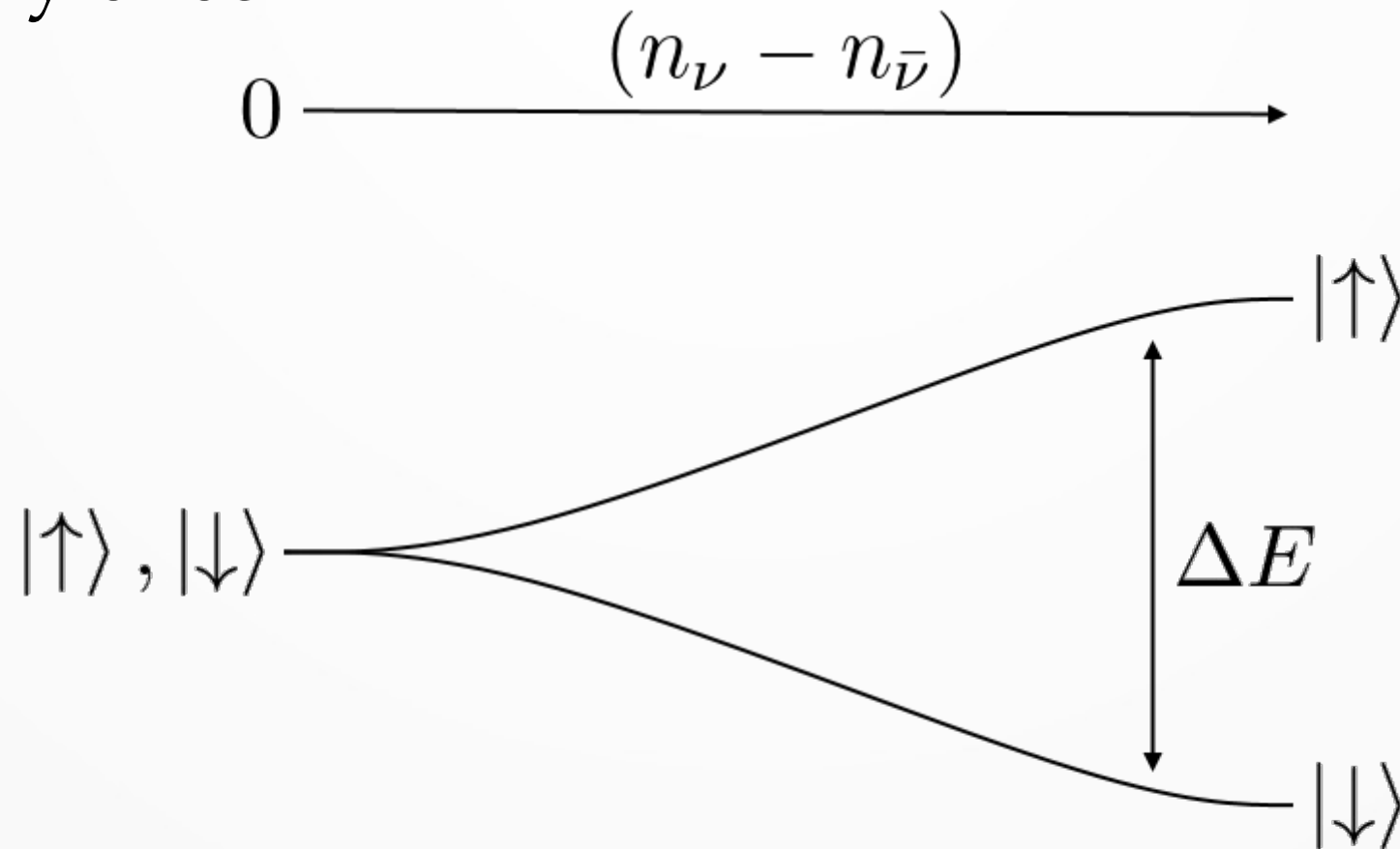
$$a_\nu \simeq 10^{-28} \left(\frac{m_\nu}{0.1 \text{ eV}} \right)^2 \text{ cm s}^{-2}$$

$$a_{\text{ref}} \simeq 10^{-15} \text{ cm s}^{-2}$$

- Future techniques could significantly improve this

Recap

- Stodolsky effect:



$$\Delta E \sim G_F \beta_\oplus (n_\nu - n_{\bar{\nu}})$$

Recap

- Energy shift giving rise to magnetic field (larger helicity term):

$$B_{\perp} \simeq 10^{-25} \delta_{\nu} \text{ T}$$

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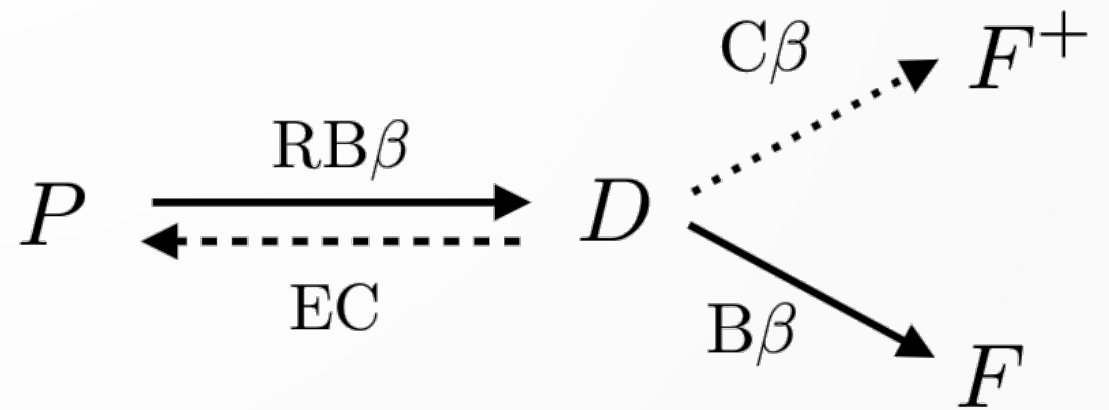
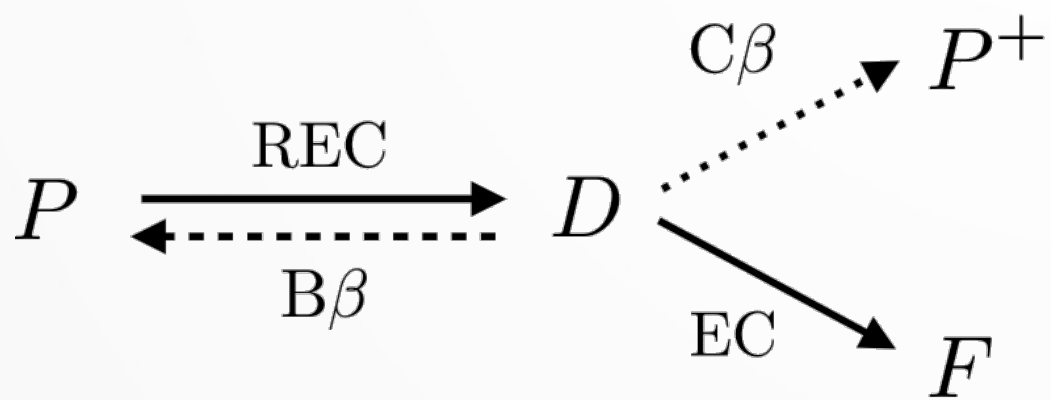
$$B_{\text{ref}} \simeq 10^{-16} \text{ T}$$

- Asymmetry constrained by BBN:

$$B_{\perp} \lesssim 10^{-24} \text{ T}$$

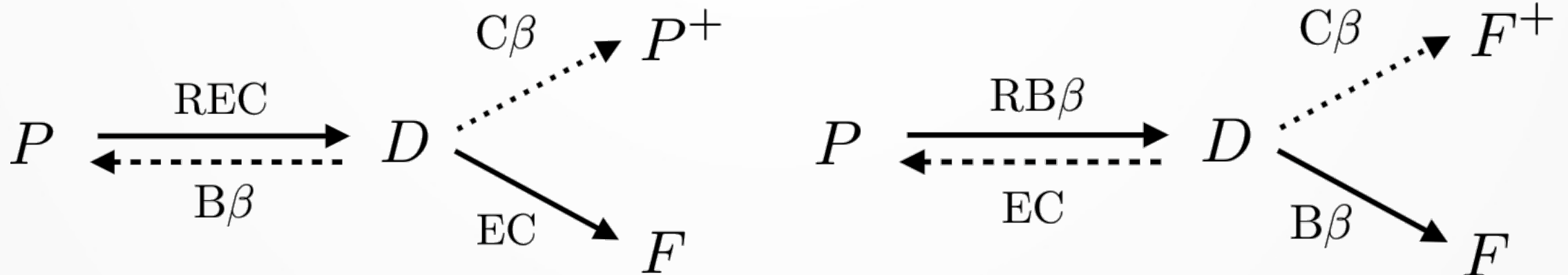
Recap

- Accelerator:



Recap

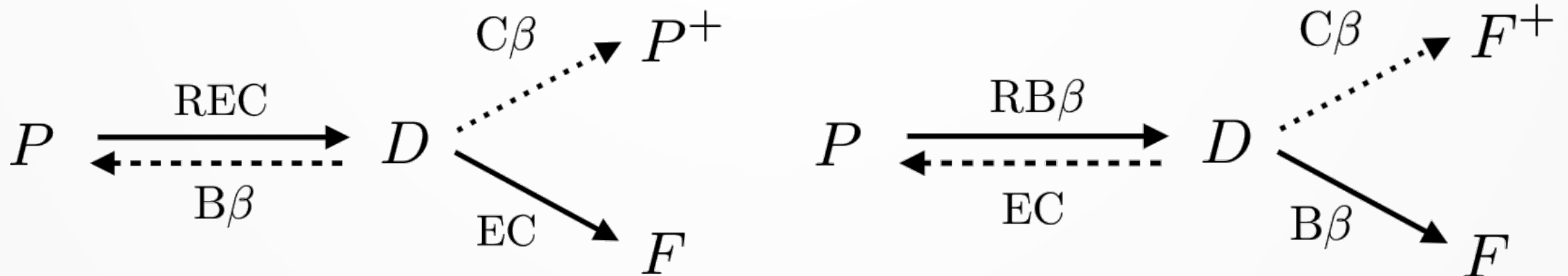
- Accelerator:



- Need target with small gap

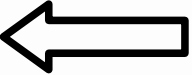
Recap

- Accelerator:



- Need target with small gap
- No suitable targets discovered (yet)

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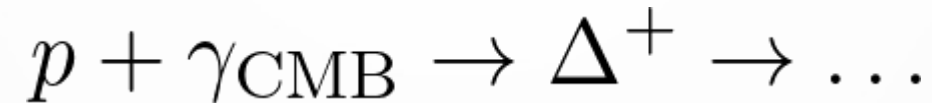
Cosmic ray attenuation

- The GZK limit:

$$p + \gamma_{\text{CMB}} \rightarrow \Delta^+ \rightarrow \dots$$

Cosmic ray attenuation

- The GZK limit:

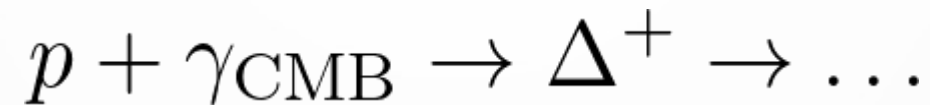


- Occurs at energy:

$$E_p \simeq \frac{m_{\Delta}^2}{2E_{\text{CMB}}}$$

Cosmic ray attenuation

- The GZK limit:



- Occurs at energy:

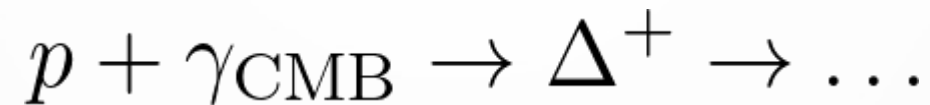
$$E_p \simeq \frac{m_{\Delta}^2}{2E_{\text{CMB}}}$$

$$\langle E_{\text{CMB}} \rangle \simeq 0.6 \text{ meV}$$

$$m_{\Delta} \simeq 1.2 \text{ GeV}$$

Cosmic ray attenuation

- The GZK limit:



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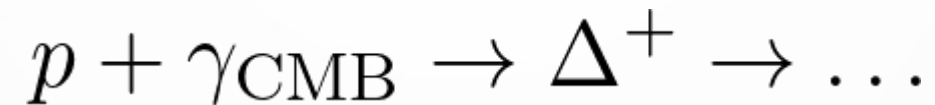
$$E_p \simeq 10^{21} \text{ eV}$$

$$\langle E_{\text{CMB}} \rangle \simeq 0.6 \text{ meV}$$

$$m_{\Delta} \simeq 1.2 \text{ GeV}$$

Cosmic ray attenuation

- The GZK limit:

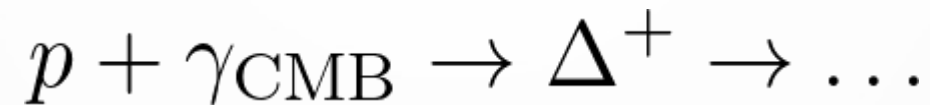


- Occurs at energy:

$$E_p \simeq 10^{19} \text{ eV}$$

Cosmic ray attenuation

- The GZK limit:



- Occurs at energy:

$$E_p \simeq 10^{19} \text{ eV}$$

- Limits the proton flux above these energies (see Mauricio's lectures)

Cosmic ray attenuation

- Similar principle for neutrinos:

$$\bar{\nu}_{\text{CR}} + \nu_{\text{C}\nu\text{B}} \rightarrow Z \rightarrow \dots$$

Cosmic ray attenuation

- Similar principle for neutrinos:

$$\bar{\nu}_{\text{CR}} + \nu_{\text{C}\nu\text{B}} \rightarrow Z \rightarrow \dots$$

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$$E_{\nu} \simeq \frac{m_Z^2}{2m_{\nu}}$$

Cosmic ray attenuation

- Similar principle for neutrinos:

$$\bar{\nu}_{\text{CR}} + \nu_{\text{C}\nu\text{B}} \rightarrow Z \rightarrow \dots$$

- Occurs at energy:

$$E_{\nu} \simeq 4 \cdot 10^{22} \text{ eV} \left(\frac{0.1 \text{ eV}}{m_{\nu}} \right)$$

Cosmic ray attenuation

- Similar principle for neutrinos:

$$\bar{\nu}_{\text{CR}} + \nu_{\text{C}\nu\text{B}} \rightarrow Z \rightarrow \dots$$

- Occurs at energy:

$$E_{\nu} \simeq 4 \cdot 10^{22} \text{ eV} \left(\frac{0.1 \text{ eV}}{m_{\nu}} \right)$$

- No neutrinos observed at these energies

Cosmic ray attenuation

- Other processes? [1]

$$\bar{\nu}_{\text{CR}} + \nu_{\text{C}\nu\text{B}} \rightarrow X \rightarrow \dots$$

Cosmic ray attenuation

- Other processes? [1]

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Cosmic ray attenuation

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- Occurs at energy:

$$E_{\nu} \simeq \frac{m_X^2}{2m_{\nu}}$$

- Meson resonances much lighter than EW bosons

[1] V. Brdar, P. S. B. Dev, R. Plestid, A. Soni, Phys. Lett. B **833**, 137358 (2022)

Cosmic ray attenuation

- Issues?

$$\sigma(\bar{\nu}\nu \rightarrow X) \propto \text{Br}(X \rightarrow \bar{\nu}\nu)$$

Cosmic ray attenuation

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$$\sigma(\bar{\nu}\nu \rightarrow X) \propto \text{Br}(X \rightarrow \bar{\nu}\nu)$$

- For EW bosons:

$$\text{Br}(Z \rightarrow \bar{\nu}\nu) \simeq 0.07$$

Cosmic ray attenuation

- Issues?

$$\sigma(\bar{\nu}\nu \rightarrow X) \propto \text{Br}(X \rightarrow \bar{\nu}\nu)$$

- For mesons:

$$\text{Br}(X \rightarrow \bar{\nu}\nu) \lesssim 10^{-11}$$

Cosmic ray attenuation

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$$\sigma(\bar{\nu}\nu \rightarrow X) \propto \text{Br}(X \rightarrow \bar{\nu}\nu)$$

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- Need huge density of neutrinos

Cosmic ray attenuation

- What about the final states?

$$X \rightarrow \dots$$

Cosmic ray attenuation

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$$X \rightarrow \dots$$

- Glashow resonance observed by IceCube [2]:

$$e^- + \bar{\nu}_e \rightarrow W^- \rightarrow e^- + \bar{\nu}_e$$

Cosmic ray attenuation

- What about the final states?

$$X \rightarrow \dots$$

- Glashow resonance observed by IceCube [2]:

$$e^- + \bar{\nu}_e \rightarrow W^- \rightarrow e^- + \bar{\nu}_e$$

- Perhaps we can do the same for CνB

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Exclusion principle

- Neutrinos are fermions

Exclusion principle

- Neutrino emitting process:

$$A \rightarrow B + \nu$$

Exclusion principle

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$$A \rightarrow B + \nu$$

- Exclusion principle:

$$\int d^3 p_\nu \rightarrow \int d^3 p_\nu (1 - f(p_\nu))$$

Exclusion principle

Follow a Fermi-Dirac distribution:

$$f(p) = \frac{1}{\exp\left(\frac{p}{T}\right) + 1}$$

Exclusion principle

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- At very small momenta:

$$f(p) \rightarrow \frac{1}{2}$$

Exclusion principle

- Atomic and nuclear transitions [3]:

$$|e\rangle \rightarrow |g\rangle + \gamma + \nu + \bar{\nu}$$

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- Maximum photon energy \rightarrow minimum neutrino energy

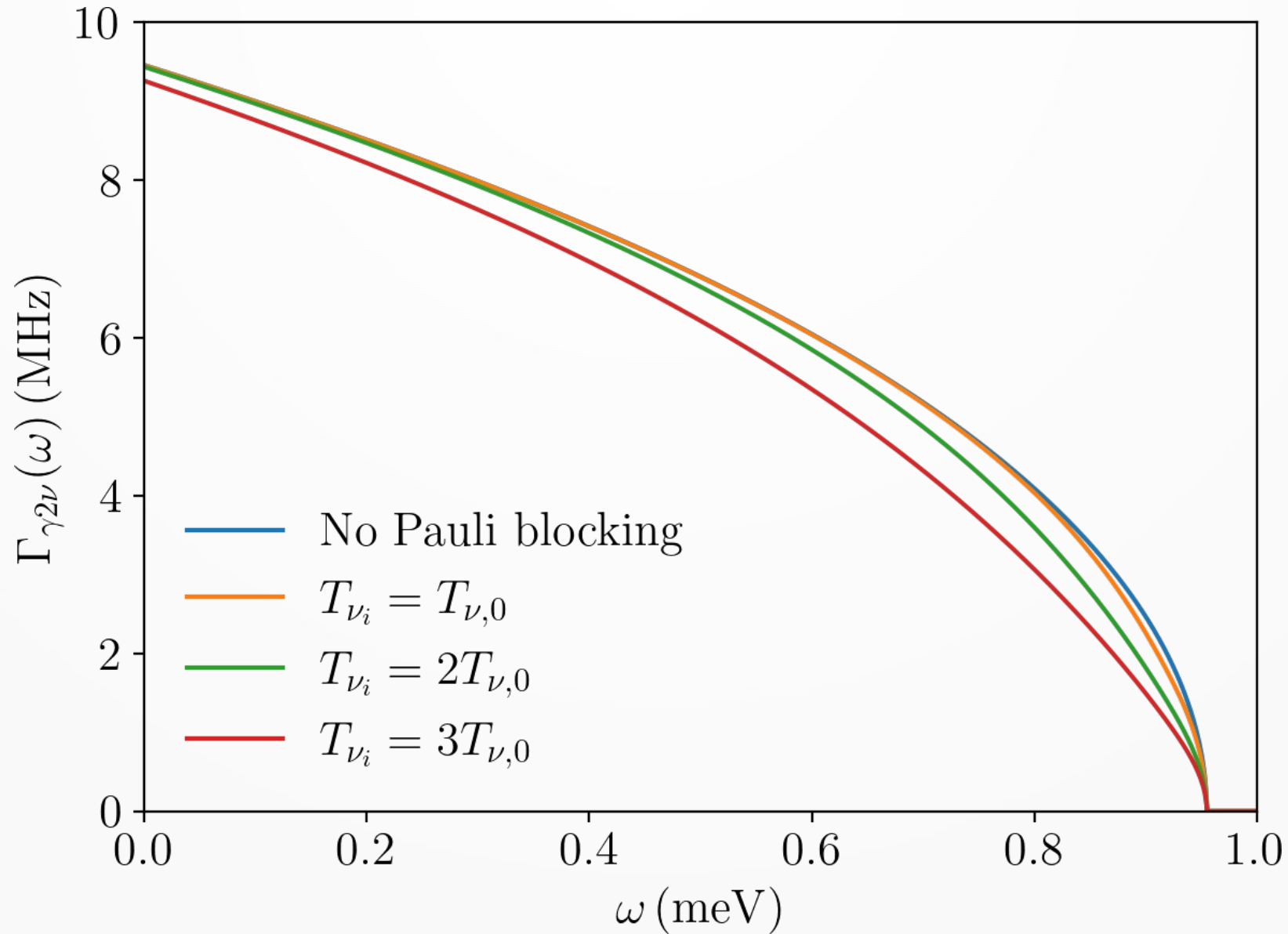
Exclusion principle

- Atomic and nuclear transitions [3]:

$$|e\rangle \rightarrow |g\rangle + \gamma + \nu + \bar{\nu}$$

- Maximum photon energy \rightarrow minimum neutrino energy
- Look for suppression at the tail end

Exclusion principle



Exclusion principle

- Realistically?

Exclusion principle

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- For a given photon energy, lots of combinations of momenta

Exclusion principle

- Realistically?
- For a given photon energy, lots of combinations of momenta
- Neutrinos are cold:

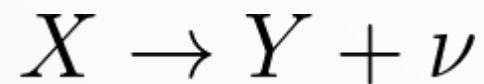
$$1 - f(p_\nu) \rightarrow 1$$

Exclusion principle

- So what now?

Exclusion principle

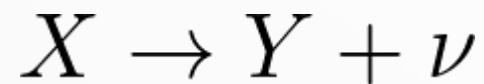
- So what now?
- Need a restricted phase space, e.g. 2-body decay



$$E_\nu = E_X - E_Y$$

Exclusion principle

- So what now?
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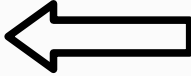


$$E_\nu = E_X - E_Y$$

- Chemical potentials?

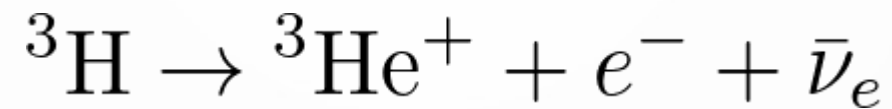
$$f(p_\nu) > \frac{1}{2}$$

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Constraints: mass

- KATRIN:



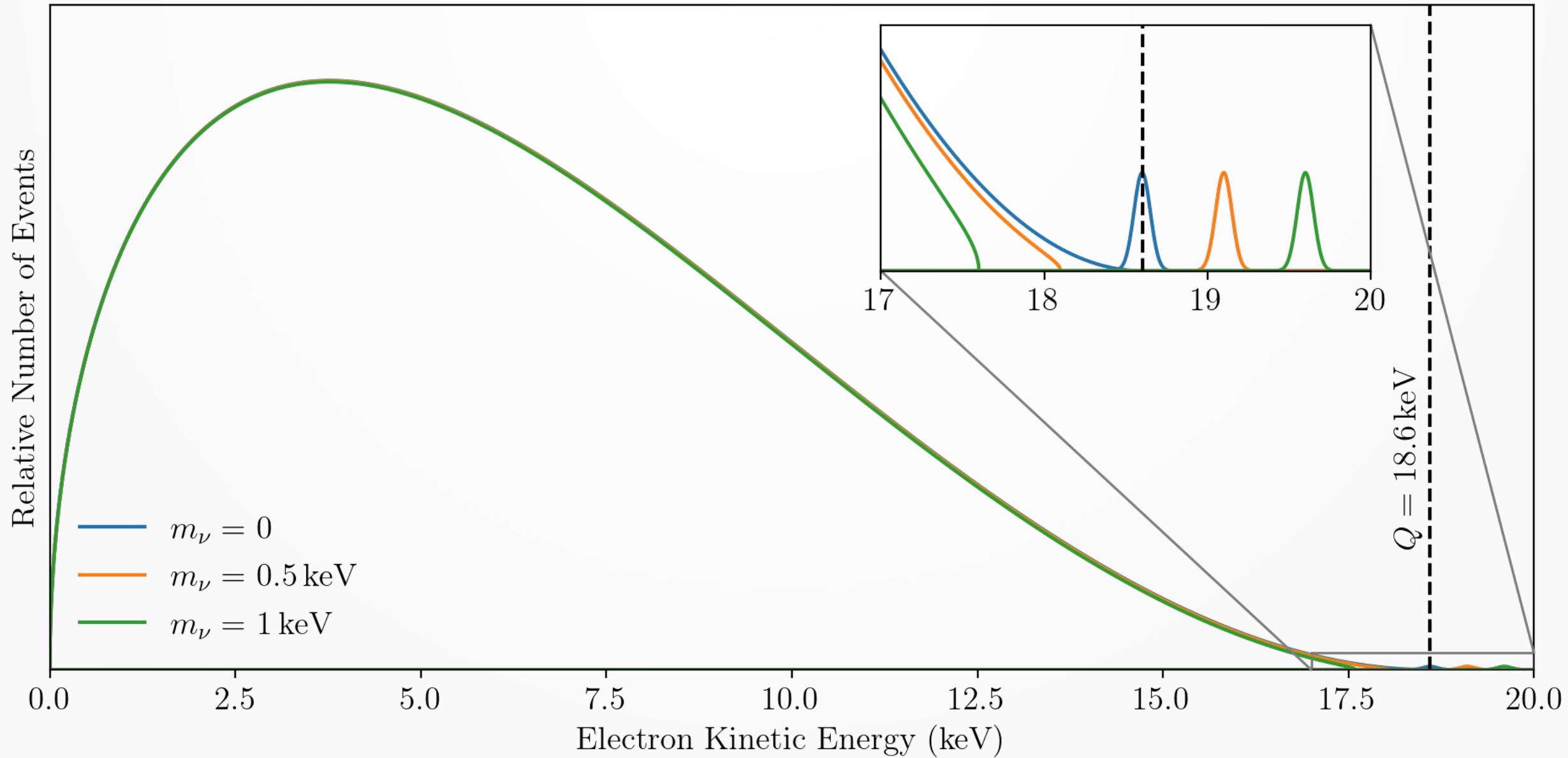
Constraints: mass

- KATRIN:



- Analogous to PTOLEMY

Constraints: mass



Constraints: mass

- Current constraints:

$$\sqrt{\sum_i |U_{ei}|^2 m_{\nu_i}^2} < 0.45 \text{ eV}$$

Constraints: mass

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- Quasi-degenerate regime:

$$m_{\nu_i} \gg \sqrt{\Delta m_{ij}^2}$$

Constraints: mass

- Current constraints:

$$\sqrt{\sum_i |U_{ei}|^2 m_{\nu_i}^2} < 0.45 \text{ eV}$$

- Quasi-degenerate regime:

$$m_{\nu_i} \gg \sqrt{\Delta m_{ij}^2} \implies m_{\nu_i} \simeq m_{\nu}$$

Constraints: mass

- Current constraints:

$$m_\nu < 0.45 \text{ eV}$$

Constraints: mass

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- Projection:

$$m_\nu < 0.2 \text{ eV}$$

Constraints: mass

- Current constraints:

$$m_\nu < 0.45 \text{ eV}$$

- Projection:

$$m_\nu < 0.2 \text{ eV}$$

- Also weakly sensitive to density

Constraints: mass

- DESI [4]:

$$\sum_i m_{\nu_i} < 0.07 \text{ eV}$$

Constraints: mass

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$$\sum_i m_{\nu_i} < 0.07 \text{ eV}$$

- Heavily disfavours inverted hierarchy!

Constraints: mass

- What if neutrinos are unstable? [5]

$$\sum_i m_{\nu_i} < 1 \text{ eV}$$

[5] M. Escudero, J. Lopez-Pavon, N. Rius, S. Sandner, JHEP **12** (2020) 119

Constraints: mass

- What if neutrinos are unstable? [5]

$$\sum_i m_{\nu_i} < 1 \text{ eV}$$

- Stronger KamLAND bound exists for Majorana neutrinos [6]:

$$\sum_i |U_{ei}|^2 m_{\nu_i} < 0.12 \text{ eV}$$

[5] M. Escudero, J. Lopez-Pavon, N. Rius, S. Sandner, JHEP **12** (2020) 119

[6] KamLAND-ZEN, arXiv: 2406.11438

Constraints: exclusion principle

- Also heavily constrains the CvB

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- CνB has two components – clustered + free streaming:

$$n_\nu = n_{\nu,C} + n_{\nu,FS}$$

Constraints: exclusion principle

- Also heavily constrains the CνB
- CνB has two components – clustered + free streaming:

$$n_\nu = n_{\nu,C} + n_{\nu,FS}$$

- Ratio set by mass and temperature

Constraints: exclusion principle

- Clustered component:

$$n_{\nu, C} \leq \underbrace{\frac{1}{(2\pi)^3}}_{V_{\nu}} \underbrace{\left(\frac{4}{3} \pi p_f^3 \right)}_{V_{\text{tot}}}$$

Constraints: exclusion principle

- Clustered component:

$$n_{\nu, \text{C}} \leq \underbrace{\frac{1}{(2\pi)^3}}_{V_{\nu}} \underbrace{\left(\frac{4}{3} \pi p_f^3 \right)}_{V_{\text{tot}}}$$

- Fermi momentum set by escape velocity:

$$p_f \simeq \beta_{\text{esc}} m_{\nu}$$

Constraints: exclusion principle

- Clustered component:

$$n_{\nu,C} \leq 12.8 \text{ cm}^{-3} \left(\frac{m_{\nu}}{0.1 \text{ eV}} \right)^3$$

Constraints: exclusion principle

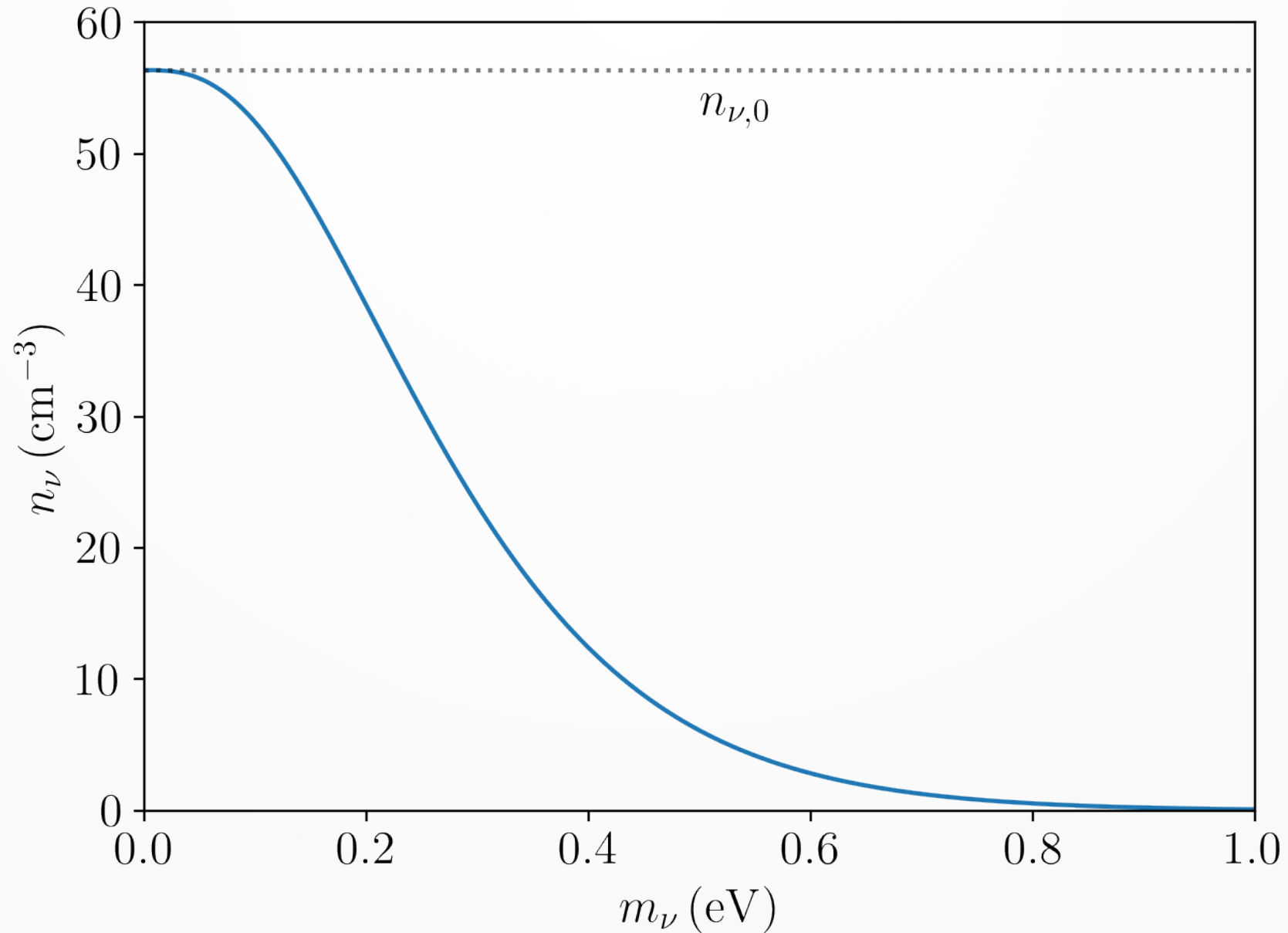
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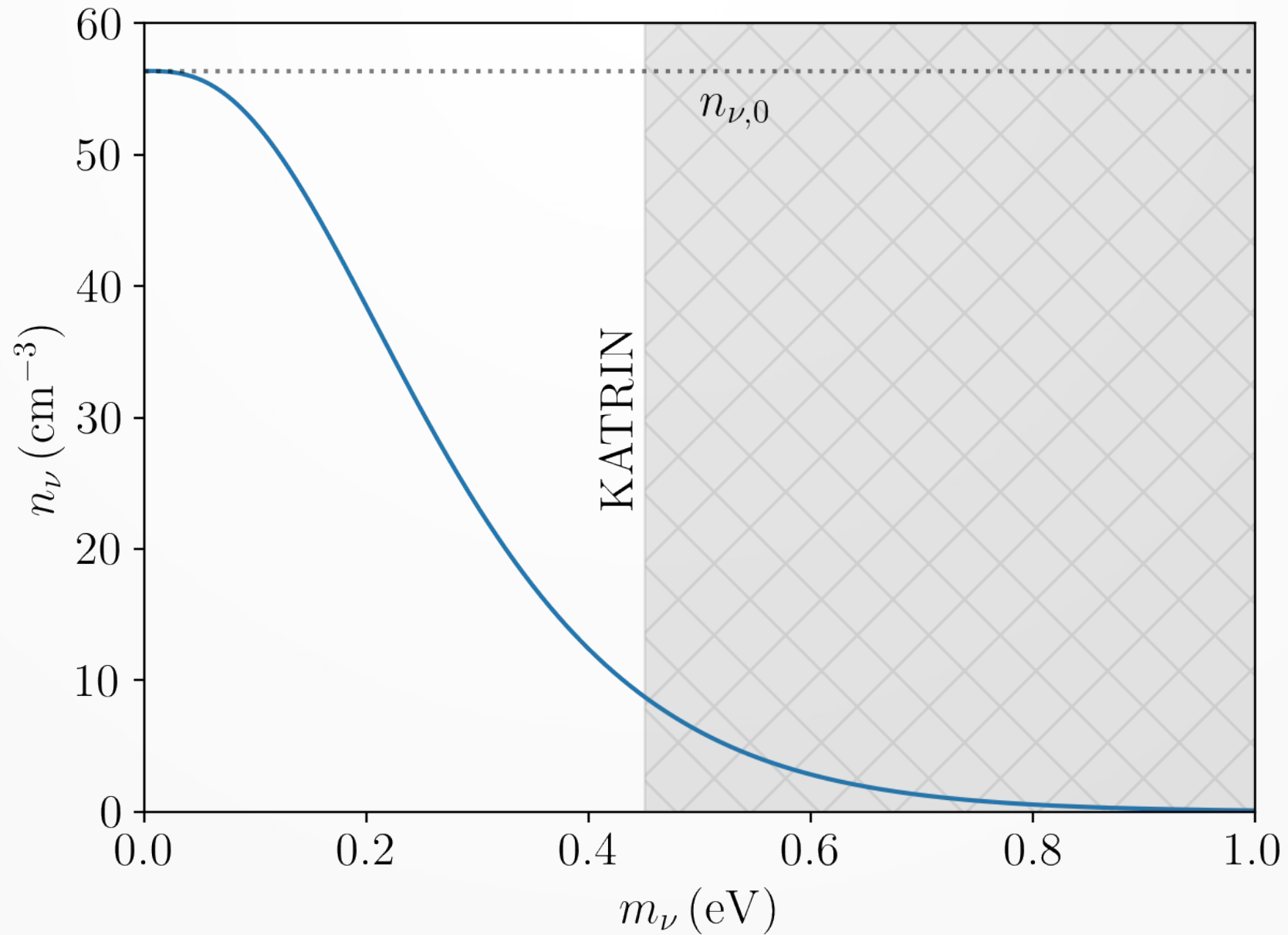
- Unclustered component:

$$n_{\nu,FD} = \frac{1}{2\pi^2} \int_{p_f}^{\infty} \frac{p^2}{\exp\left(\frac{p}{T} + 1\right)}$$

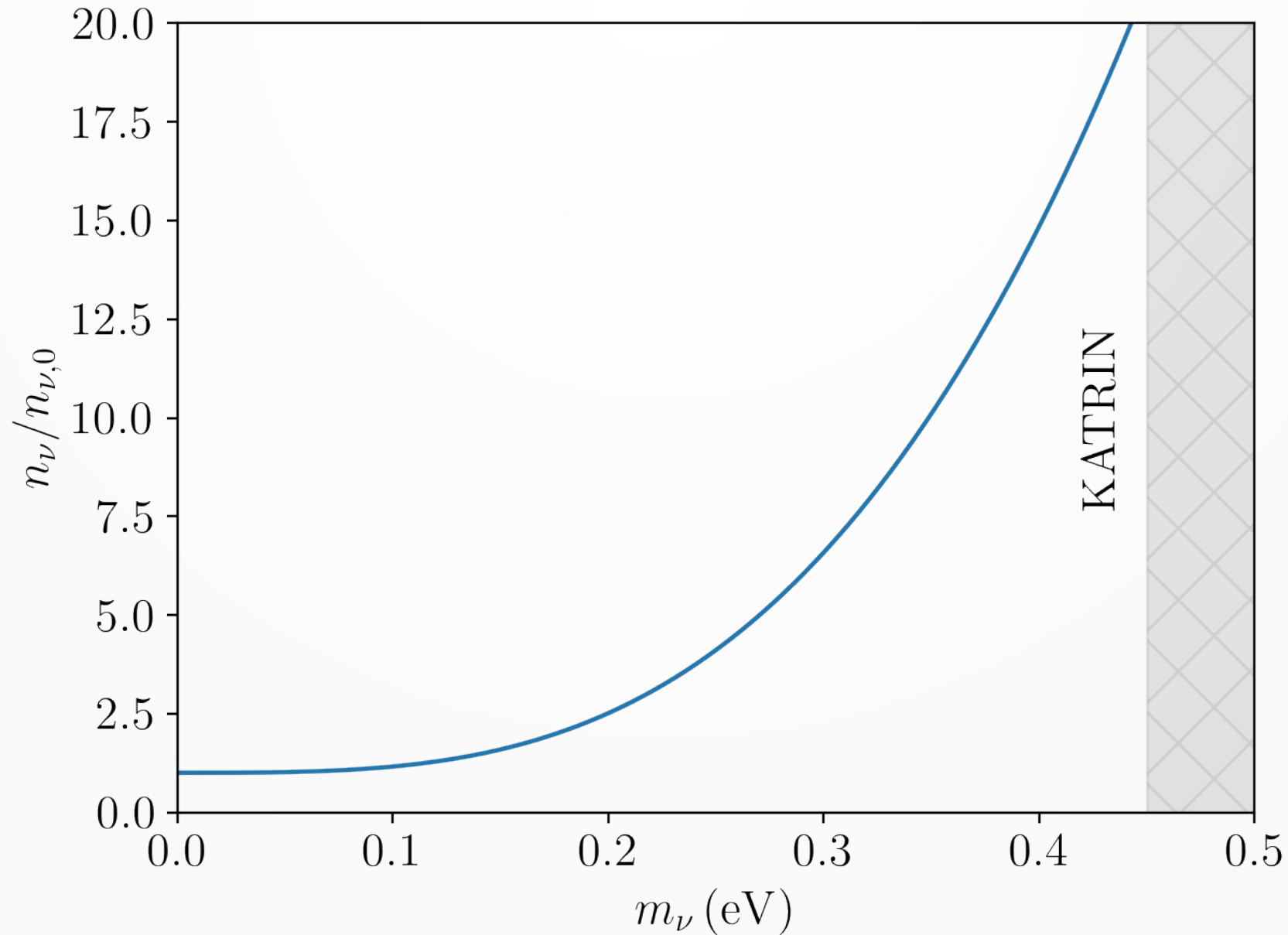
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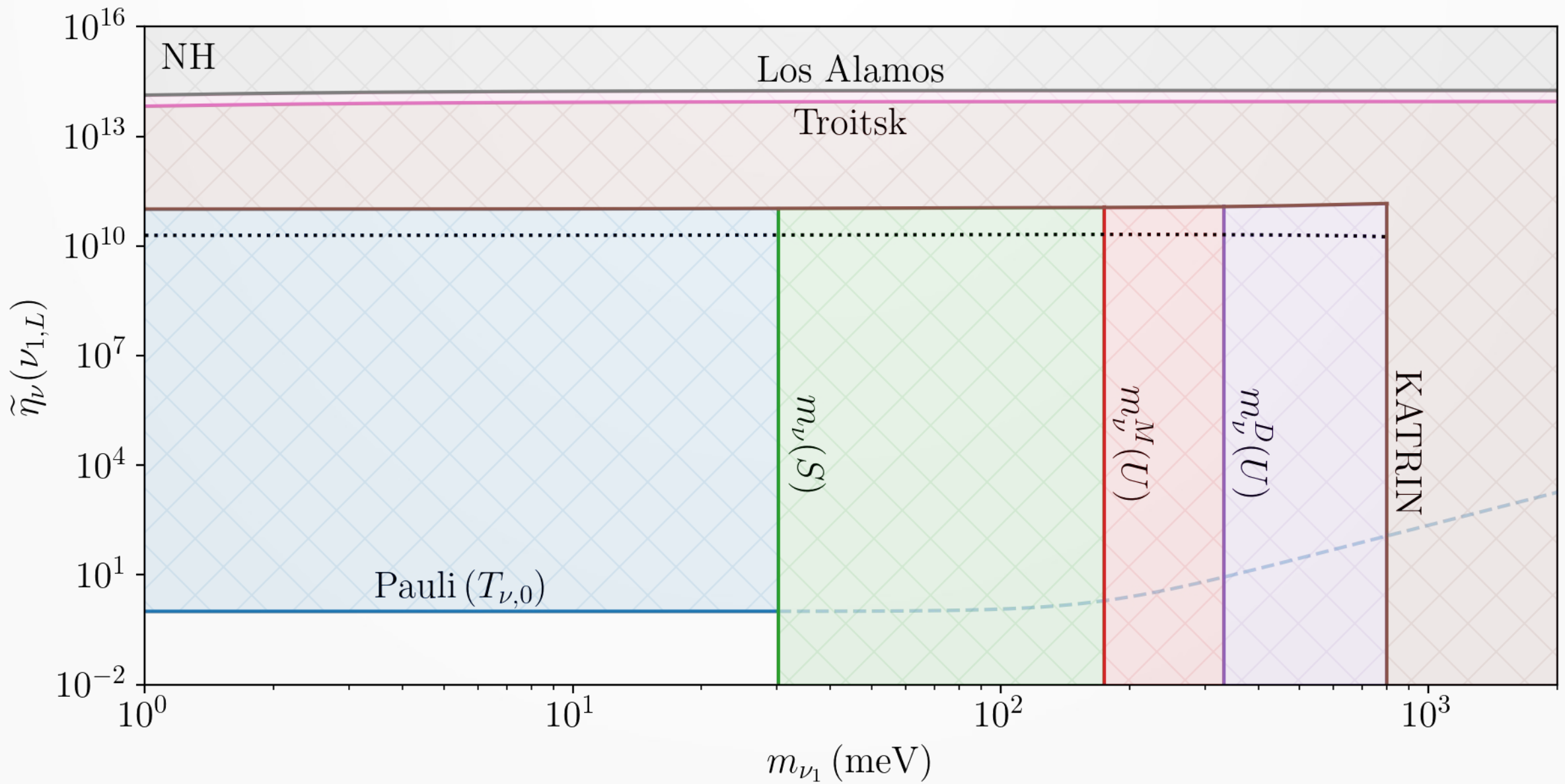
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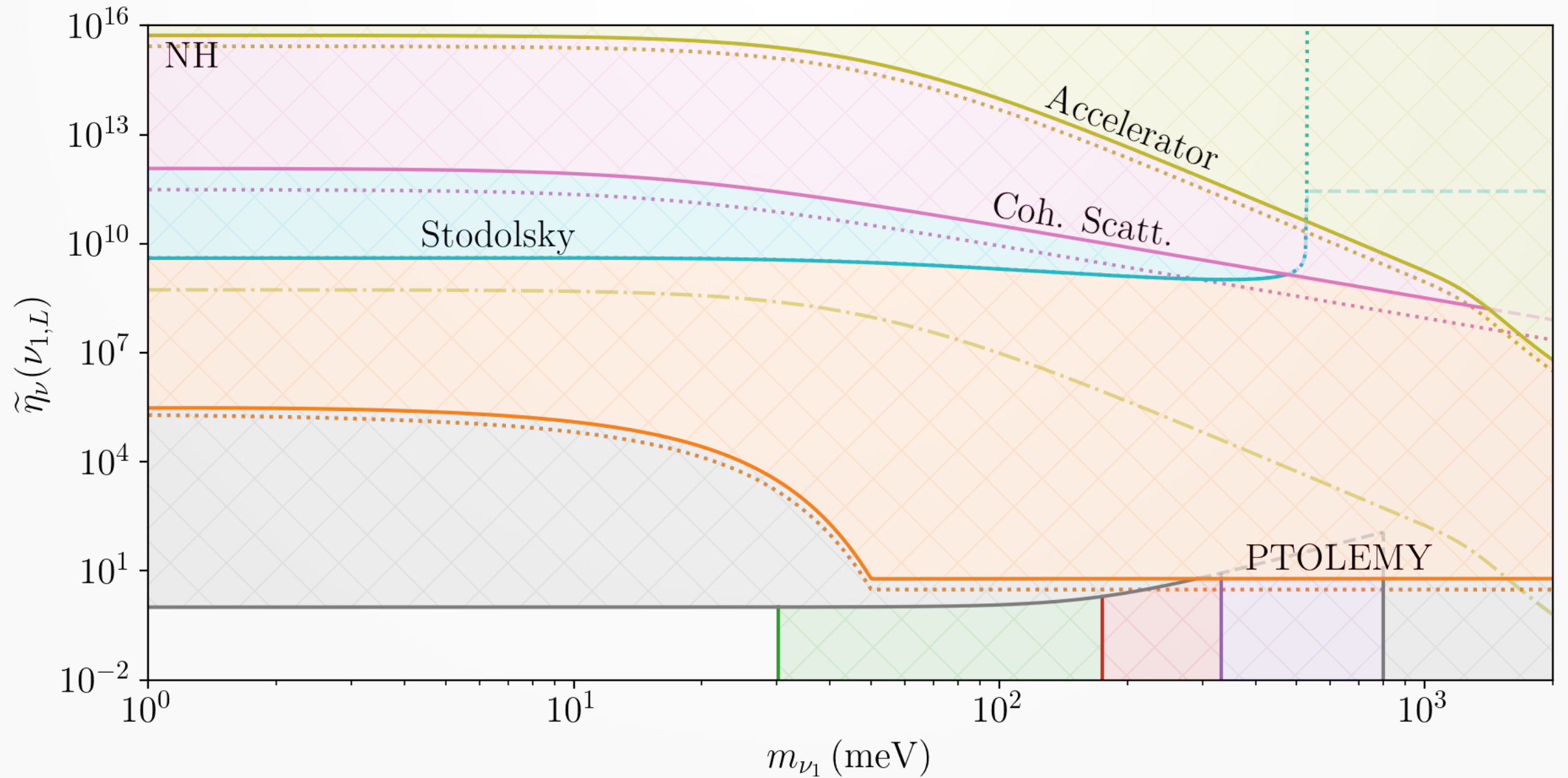
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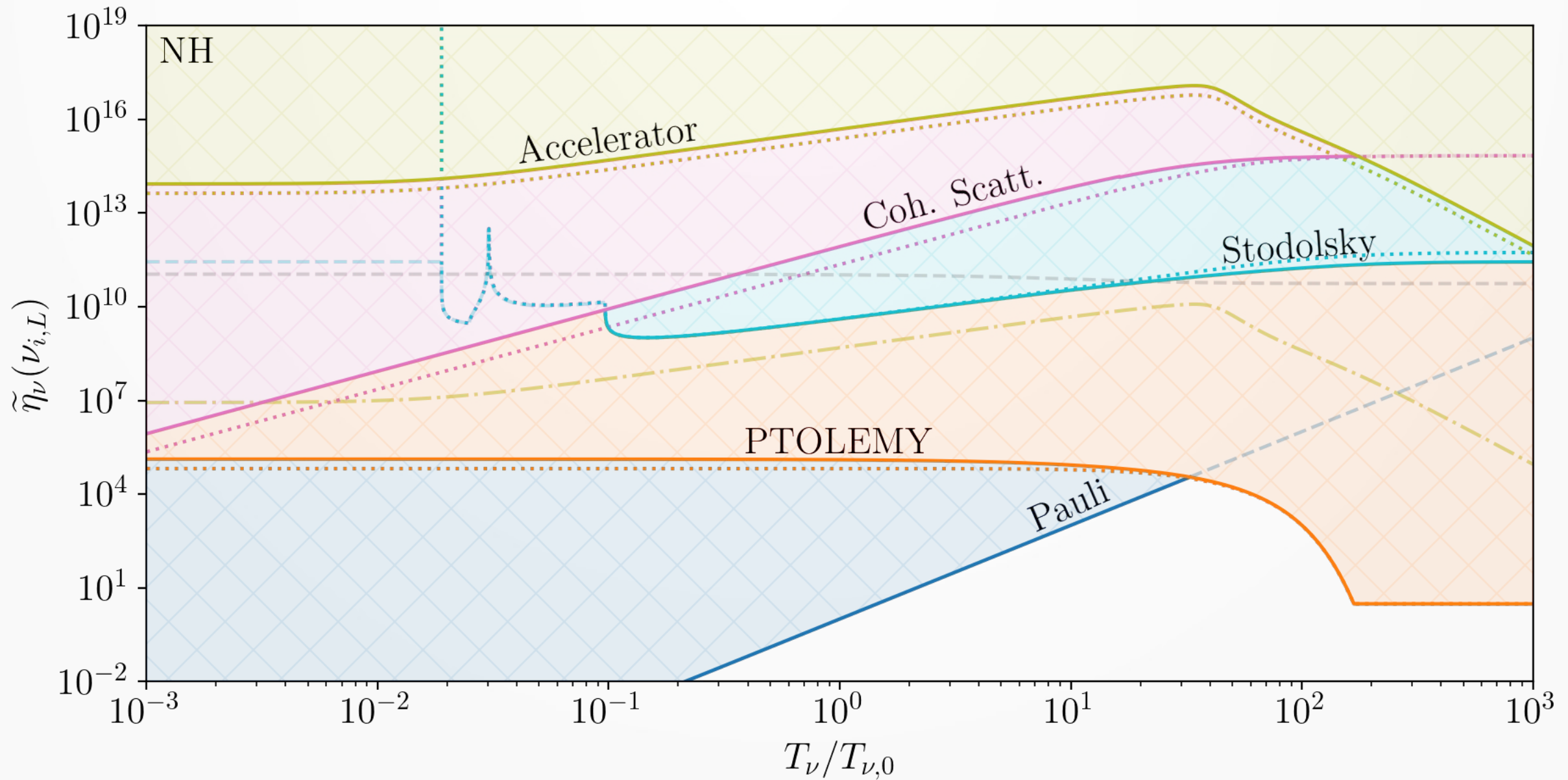
Constraints



Sensitivity



Sensitivity



Summary

- CνB detection is an almost impossible task:
 - Cold, almost non-interacting neutrinos
- Lots of reasons to look for the CνB:
 - New interactions, lepton asymmetries, N_{eff}
- Lots of ideas to detect the CνB!
 - None really work...
 - But there are hints!

Thank you!



Děkuju!