





Neutrino Non-Standard Interactions (NSI)

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Outline

- Lecture 1: NSI Basics
 - Why care about NSI?
 - Review of SI and matter effect
 - Wolfenstein parametrization of (vector) NSI
 - NSI in propagation (NC), production and detection (CC)
 - Current status and future prospects of NSI constraints
 - Possible hint of NSI in oscillation data?

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- Lecture 2: NSI Model Building and Phenomenology
- Lecture 3: Beyond ε Scalar NSI, NSSI, Neutrino-DM interactions, ...

References

- $\mathcal{O}(500)$ papers on NSI.
- Apologies if your favorite paper(s) not cited here.
- Reviews:
 - T. Ohlsson, Rept. Prog. Phys. **76**, 044201 (2013) [arXiv:1209.2710].
 - O. G. Miranda and H. Nunokawa, New J. Phys. 17, no.9, 095002 (2015)
 [arXiv:1505.06254].
 - Y. Farzan and M. Tortola, Front. in Phys. **6**, 10 (2018) [arXiv:1710.09360].
 - P. S. B. Dev et al., SciPost Phys. Proc. 2, 001 (2019) [arXiv:1907.00991].
 - S. K. Agarwalla et al., Snowmass LOI (2022).

Why Non-Standard Interactions?

 $Neutrino\ Oscillations \Longrightarrow Nonzero\ Neutrino\ Mass \Longrightarrow BSM\ Physics$

Why Non-Standard Interactions?

Neutrino Oscillations \Longrightarrow Nonzero Neutrino Mass \Longrightarrow BSM Physics

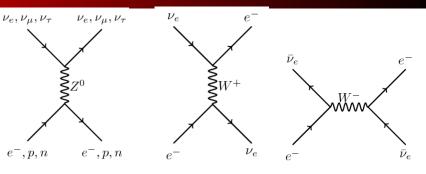
- Must introduce new fermions, scalars and/or gauge bosons messengers of neutrino mass physics.
- New couplings involving neutrinos inevitably lead to NSI.
- Potentially observable effects in neutrino production, propagation, and/or detection.
- Relevant for all kinds of neutrinos (accelerator, reactor, atmospheric, solar, supernova, astrophysical, cosmic).

Why Non-Standard Interactions?

Neutrino Oscillations \Longrightarrow Nonzero Neutrino Mass \Longrightarrow BSM Physics

- Must introduce new fermions, scalars and/or gauge bosons messengers of neutrino mass physics.
- New couplings involving neutrinos inevitably lead to NSI.
- Potentially observable effects in neutrino production, propagation, and/or detection.
- Relevant for all kinds of neutrinos (accelerator, reactor, atmospheric, solar, supernova, astrophysical, cosmic).
- Complementary to direct search for new physics at the LHC.
- At the very least, could serve as a foil for the standard 3-neutrino oscillation scheme.
- Better understanding of NSI is crucial for correct interpretation of oscillation data.
- Potential hints of NSI in recent T2K/NO ν A data.

Standard Neutrino Interactions with Matter



$$\mathcal{H}_Z = \frac{G_F}{\sqrt{2}} J_Z^\mu J_{Z_\mu}^\dagger , \text{ where } J_Z^\mu = \sum_{i=\ell,\nu_\ell,u,d} \overline{\psi}_i \gamma^\mu \left[I_i^3 (1-\gamma_5) - 2Q_i \sin^2 \theta_W \right] \psi_i ,$$

$$\mathcal{H}_W = \frac{G_F}{\sqrt{2}} J_W^\mu J_{W_\mu}^\dagger , \text{ where } J_W^\mu = \overline{e} \gamma^\mu (1-\gamma_5) \nu_e .$$

.

Effective Matter Potential

Type of reaction	Matter potential
V_Z^n	$\mp G_F N_n/\sqrt{2}$
V_Z^p	$\pm G_F(1-4\sin^2\theta_W)N_p/\sqrt{2}$
V_Z^e	$\mp G_F(1-4\sin^2 heta_W)N_e/\sqrt{2}$
V_W^e	$\pm\sqrt{2}G_FN_e$

[For a derivation, see e.g., J. Linder,, hep-ph/0504264]

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FFD 1 1 1 11	T. T. 1 1 1 1/05040641

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- Upper (Lower) sign is for neutrino (antineutrino).
- In an electrically neutral medium $(N_e = N_p)$, $V_Z^e + V_Z^p = 0$.
- V_Z^n is diagonal in neutrino flavor, and gives an overall phase shift, which is of no physical significance in oscillations.
- Effective neutrino matter potential induced by Earth:

$$V_{\rm CC} = V_W^e = \sqrt{2}G_F N_e \simeq 3.8 \times 10^{-14} \text{ eV} \left(\frac{\rho}{\text{gm/cm}^3}\right) \left(\frac{Y_e}{0.5}\right).$$

Oscillation Probability

• Time evolution governed by Schrödinger equation:

$$i\frac{d}{dt}\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = H\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \left[\frac{MM^\dagger}{2E} + V(t)\right]\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix},$$

where E is the neutrino energy, $M = U \operatorname{diag}(m_1, m_2, m_3)U^T$ is the neutrino mass matrix and $V = \operatorname{diag}(V_{CC}, 0, 0)$.

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• Probability of oscillation over a length L (in the 2-flavor limit):

$$P(\nu_{\alpha} \to \nu_{\beta}) = \left| \langle \nu_{\beta} | e^{-iHL} | \nu_{\alpha} \rangle \right|^{2} \simeq \sin^{2} 2\theta_{M} \sin^{2} \left(\frac{\Delta m_{M}^{2} L}{4E} \right) ,$$
where $\tan 2\theta_{M} = \frac{\Delta m^{2} \sin 2\theta}{\Delta m^{2} \cos 2\theta - A} ,$

$$\Delta m_{M}^{2} = \sqrt{(\Delta m^{2} \cos 2\theta - A)^{2} + (\Delta m^{2} \sin 2\theta)^{2}} ,$$

$$A = 2EV_{\text{CC}} .$$

Neutral Current NSI

$$\mathcal{L}_{\mathrm{NSI}}^{\mathrm{NC}} = -2\sqrt{2}G_F \sum_{f,X,\alpha,\beta} \varepsilon_{\alpha\beta}^{fX} (\bar{\nu}_{\alpha}\gamma^{\mu}P_L\nu_{\beta})(\bar{f}\gamma_{\mu}P_Xf) ,$$

with X=L,R, and $f\in\{e,u,d\}$. [L. Wolfenstein,, PRD '78)]

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• Only vector part is relevant (axial-vector part is spin-dependent):

$$\begin{split} \varepsilon_{\alpha\beta} &= \sum_{f \in \{e,u,d\}} \frac{N_f}{N_e} \varepsilon_{\alpha\beta}^{fV} = \varepsilon_{\alpha\beta}^{eV} + \frac{N_p}{N_e} (2\varepsilon_{\alpha\beta}^{uV} + \varepsilon_{\alpha\beta}^{dV}) + \frac{N_n}{N_e} (\varepsilon_{\alpha\beta}^{uV} + 2\varepsilon_{\alpha\beta}^{dV}) \\ &= \varepsilon_{\alpha\beta}^{eV} + (2 + Y_n) \varepsilon_{\alpha\beta}^{uV} + (1 + 2Y_n) \varepsilon_{\alpha\beta}^{dV} \end{split}$$

with $\varepsilon_{\alpha\beta}^{fV}=\varepsilon_{\alpha\beta}^{fL}+\varepsilon_{\alpha\beta}^{fR}$ and $Y_n=N_n/N_e\simeq 1$ for Earth.

Neutral Current NSI

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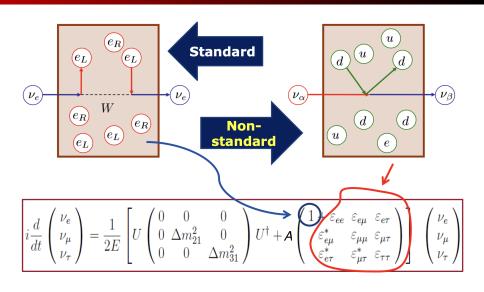
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with $\varepsilon_{\alpha\beta}^{fV} = \varepsilon_{\alpha\beta}^{fL} + \varepsilon_{\alpha\beta}^{fR}$ and $Y_n = N_n/N_e \simeq 1$ for Earth.

• Leads to extra matter effect in propagation:

$$P(\nu_{\alpha} \to \nu_{\beta}) = \left| \langle \nu_{\beta} | e^{-i(H + V_{\rm NSI})L} | \nu_{\alpha} \rangle \right|^2 \,,$$
 where
$$V_{\rm NSI} = \sqrt{2} G_F N_e \begin{pmatrix} \varepsilon_{ee} & \varepsilon_{e\mu} & \varepsilon_{e\tau} \\ \varepsilon_{e\mu}^* & \varepsilon_{\mu\mu} & \varepsilon_{\mu\tau} \\ \varepsilon_{e\tau}^* & \varepsilon_{\mu\tau}^* & \varepsilon_{\tau\tau} \end{pmatrix}$$

What does NSI do?



[figure adapted from T. Ohlsson]

Induces non-standard oscillations during propagation

$$i\frac{d}{dL} \begin{pmatrix} \nu_e \\ \nu_\tau \end{pmatrix} = \begin{bmatrix} \frac{1}{2E} U \begin{pmatrix} 0 & 0 \\ 0 & \Delta m^2 \end{pmatrix} U^\dagger + A \begin{pmatrix} 1 + \epsilon_{ee} & \epsilon_{e\tau} \\ \epsilon_{e\tau} & \epsilon_{\tau\tau} \end{bmatrix} \end{pmatrix} \begin{pmatrix} \nu_e \\ \nu_\tau \end{pmatrix}$$



Induces non-standard oscillations during propagation

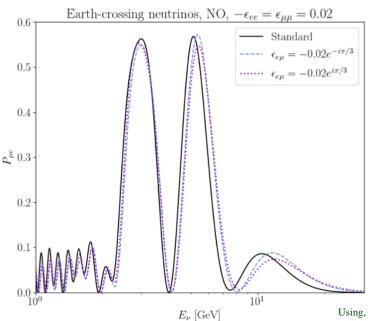
$$i\frac{d}{dL} \left(\begin{array}{c} \nu_{e} \\ \nu_{\tau} \end{array} \right) \quad = \quad \left[\frac{1}{2E} U \left(\begin{array}{cc} 0 & 0 \\ 0 & \Delta m^{2} \end{array} \right) U^{\dagger} + A \left(\begin{array}{cc} 1 + \epsilon_{ee} & \epsilon_{e\tau} \\ \epsilon_{e\tau} & \epsilon_{\tau\tau} \end{array} \right) \right] \left(\begin{array}{c} \nu_{e} \\ \nu_{\tau} \end{array} \right)$$

$$P(\nu_e \to \nu_\tau) = \sin^2 2\theta_M \sin^2 \left(\frac{\Delta m_M^2 L}{4E}\right)$$

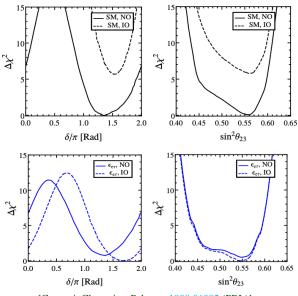
$$\left(\frac{\Delta m_{M}^{2}}{2EA}\right)^{2} \equiv \left(\frac{\Delta m^{2}}{2EA}\cos 2\theta - (1 + \epsilon_{ee} - \epsilon_{\tau\tau})\right)^{2} + \left(\frac{\Delta m^{2}}{2EA}\sin 2\theta + 2\epsilon_{e\tau}\right)^{2}$$

$$\sin 2\theta_{M} \equiv \frac{\Delta m^{2}\sin 2\theta + 4EA\epsilon_{e\tau}}{\Delta m_{M}^{2}}$$

Modifies standard oscillation probabilities

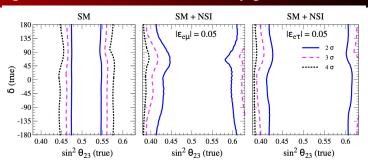


Can obscure mass-ordering determination

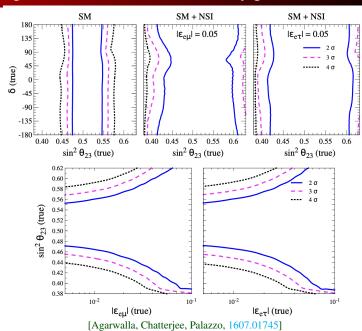


[Capozzi, Chatterjee, Palazzo, 1908.06992 (PRL)]

Can degrade octant and $\delta_{\rm CP}$ discovery potential



Can degrade octant and $\delta_{\rm CP}$ discovery potential



[Y. Grossman,, hep-ph/9507344]

$$\mathcal{L}_{\mathrm{NSI}}^{\mathrm{CC}} = -2\sqrt{2}G_{F}\varepsilon_{\alpha\beta}^{ff'X}(\bar{\nu}_{\alpha}\gamma^{\mu}P_{L}\ell_{\beta})(\bar{f}'\gamma_{\mu}P_{X}f)$$

• Flavor mixture states at source and detection.

$$P(\nu_{\alpha} \to \nu_{\beta}) = \left| \langle \nu_{\beta}^{\mathrm{d}} | e^{-iHL} | \nu_{\alpha}^{\mathrm{s}} \rangle \right|^{2}$$

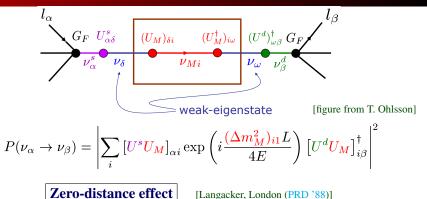
• Source NSI (e.g. in pion decay):

$$|\nu_{\alpha}^{\rm s}\rangle = |\nu_{\alpha}\rangle + \sum_{\beta=e,\mu,\tau} \varepsilon_{\alpha\beta}^{\rm s} |\nu_{\beta}\rangle, \quad \text{e.g. } \pi^+ \xrightarrow{\varepsilon_{e\mu}^{\rm s}} \mu^+\nu_e$$

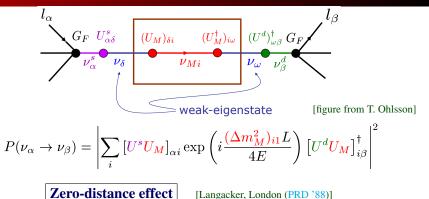
• Detection NSI (e.g. in neutrino-nucleon scattering):

$$\langle \nu_{\alpha}^{\mathrm{d}} | = \langle \nu_{\alpha} | + \sum_{\beta = e, \mu, \tau} \varepsilon_{\alpha\beta}^{\mathrm{d}} \langle \nu_{\beta} |, \quad \text{e.g. } \nu_{\tau} n \xrightarrow{\varepsilon_{e\tau}^{\mathrm{d}}} e^{-} p$$

Interesting Near-Detector Physics



Interesting Near-Detector Physics

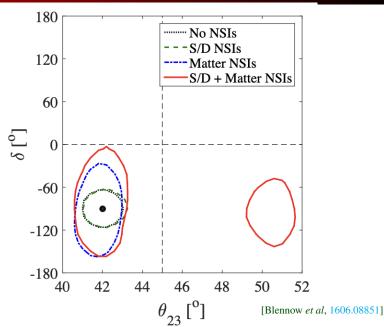


• In the 2-flavor case.

$$\frac{\Delta m^2 L}{4E} \to 0 \Longrightarrow P(\nu_e \to \nu_\mu) \to \left(\epsilon_{e\mu}^s - \epsilon_{e\mu}^d\right)^2$$

• Can in principle be probed with a near detector close to the source (e.g., $ESS\nu SB$), assuming that the neutrino fluxes at source are well-known.

CC+NC NSI can make things worse!



Current Constraints* on NC NSI

[Farzan, Tortola, 1710.09360]

	90% C.L. range	origin
		NSI with quarks
ϵ_{ee}^{dL}	[-0.3, 0.3]	CHARM
ϵ_{ee}^{dR}	[-0.6, 0.5]	CHARM
$\epsilon_{\mu\mu}^{dV}$	$\left[-0.042, 0.042\right]$	atmospheric + accelerator
$\epsilon^{uV}_{\mu\mu}$	[-0.044, 0.044]	atmospheric + accelerator
$\epsilon_{\mu\mu}^{dA}$	[-0.072, 0.057]	atmospheric + accelerator
$\epsilon^{uA}_{\mu\mu}$	[-0.094, 0.14]	atmospheric + accelerator
$\epsilon_{\tau\tau}^{dV}$	[-0.075, 0.33]	oscillation data $+$ COHERENT
$\epsilon_{\tau\tau}^{uV}$	[-0.09, 0.38]	oscillation data $+$ COHERENT
$\epsilon_{\tau\tau}^{qV}$	$\left[-0.037, 0.037\right]$	atmospheric
		NSI with electrons
ϵ_{ee}^{eL}	[-0.021, 0.052]	solar + KamLAND
ϵ_{ee}^{eR}	[-0.07, 0.08]	TEXONO
$\epsilon^{eL}_{\mu\mu}$, $\epsilon^{eR}_{\mu\mu}$	[-0.03, 0.03]	reactor + accelerator
$\epsilon_{\tau\tau}^{eL}$	[-0.12, 0.06]	${\rm solar}+{\rm KamLAND}$
$\epsilon_{\tau\tau}^{eR}$	[-0.98, 0.23] [-0.25, 0.43]	$\begin{array}{c} \mathrm{solar} + \mathrm{KamLAND} \ \mathrm{and} \ \mathrm{Borexino} \\ \mathrm{reactor} + \mathrm{accelerator} \end{array}$

Current Constraints* on NC NSI

[Farzan, Tortola, 1710.09360]

	90% C.L. range	origin		90% C.L. range	origin
		NSI with quarks		NSI w	vith quarks
ϵ_{ee}^{dL}	[-0.3, 0.3]	CHARM	$\epsilon_{e\mu}^{qL}$	[-0.023, 0.023]	accelerator
$\begin{array}{l} \epsilon^{dR}_{ee} \\ \epsilon^{dV}_{\mu\mu} \\ \epsilon^{uV}_{\mu\mu} \\ \epsilon^{dA}_{\mu\mu} \\ \epsilon^{uA}_{\mu\mu} \\ \epsilon^{dA}_{\mu\mu} \\ \epsilon^{dV}_{\tau\tau} \\ \epsilon^{dV}_{\tau\tau} \\ \epsilon^{dV}_{\tau\tau} \end{array}$	$ \begin{bmatrix} -0.6, 0.5 \\ [-0.042, 0.042] \\ [-0.044, 0.044] \\ [-0.072, 0.057] \\ [-0.094, 0.14] \\ [-0.075, 0.33] \\ [-0.09, 0.38] \end{bmatrix} $	CHARM atmospheric + accelerator oscillation data + COHERENT oscillation data + COHERENT	$\begin{aligned} & \epsilon_{e\mu}^{qR} \\ & \epsilon_{e\mu}^{uV} \\ & \epsilon_{e\mu}^{uV} \\ & \epsilon_{e\tau}^{dV}, \ \epsilon_{e\tau}^{qR} \\ & \epsilon_{e\tau}^{uV}, \ \epsilon_{e\tau}^{qR} \\ & \epsilon_{e\tau}^{dV}, \ \epsilon_{e\tau}^{qL} \\ & \epsilon_{\mu\tau}^{qL}, \end{aligned}$	$ \begin{bmatrix} -0.036, 0.036, \\ -0.073, 0.044 \end{bmatrix} $ $ \begin{bmatrix} -0.07, 0.04 \end{bmatrix} $ $ \begin{bmatrix} -0.5, 0.5 \end{bmatrix} $ $ \begin{bmatrix} -0.15, 0.13 \end{bmatrix} $ $ \begin{bmatrix} -0.13, 0.12 \end{bmatrix} $ $ \begin{bmatrix} -0.023, 0.023 \end{bmatrix} $	$\begin{tabular}{ll} accelerator \\ oscillation data + COHERENT \\ oscillation data + COHERENT \\ CHARM \\ oscillation data + COHERENT \\ oscillation data + COHERENT \\ accelerator \\ \end{tabular}$
E ₇₇	[-0.037, 0.037]	atmospheric NSI with electrons	$\epsilon^{qR}_{\mu\tau}$ $\epsilon^{qV}_{\mu\tau}$ $\epsilon^{qA}_{\mu\tau}$	[-0.036, 0.036] [-0.006, 0.0054] [-0.039, 0.039]	accelerator IceCube
ϵ_{ee}^{eL} ϵ_{ee}^{eR}	[-0.021, 0.052] [-0.07, 0.08]	solar + KamLAND TEXONO	έμτ		atmospheric + accelerator th electrons
ϵ_{ee} $\epsilon_{\mu\mu}^{eL}$, $\epsilon_{\mu\mu}^{eR}$ $\epsilon_{\tau\tau}^{eL}$ $\epsilon_{\tau\tau}^{eR}$ $\epsilon_{\tau\tau}^{eV}$	[-0.07, 0.08] [-0.03, 0.03] [-0.12, 0.06] [-0.98, 0.23] [-0.25, 0.43] [-0.11, 0.11]	reactor + accelerator solar + KamLAND and Borexino reactor + accelerator atmospheric	$\begin{array}{c} & \\ \epsilon_{e\mu}^{eL}, \epsilon_{e\mu}^{eR} \\ \epsilon_{e\tau}^{eL} \\ \epsilon_{e\tau}^{eR} \end{array} \begin{bmatrix} \\ \epsilon_{e\tau}^{eL}, \epsilon_{\mu\tau}^{eR} \\ \epsilon_{\tau}^{eV} \\ \end{bmatrix}$	[-0.13, 0.13] [-0.33, 0.33] -0.28, -0.05] & [0.05, 0.28] [-0.19, 0.19] [-0.10, 0.10] [-0.018, 0.016]	reactor + accelerator reactor + accelerator reactor + accelerator TEXONO reactor + accelerator lceCube

(Flavor-diagonal)

(Flavor-changing)

^{*}Conditions apply (one at a time, some constraints do not apply to light mediators)

Current Constraints* on CC NSI

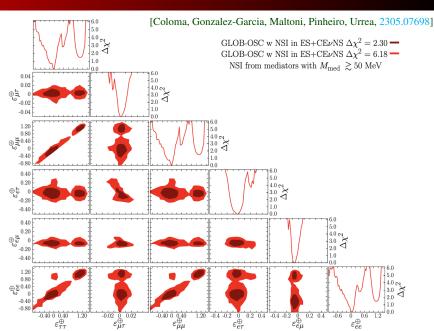
	90% C.L. range	origin
		semileptonic NSI
ϵ_{ee}^{udP}	[-0.015, 0.015]	Daya Bay
$\epsilon_{e\mu}^{udL}$	[-0.026, 0.026]	NOMAD
$\epsilon_{e\mu}^{udR}$	[-0.037, 0.037]	NOMAD
$\epsilon_{ au e}^{udL}$	[-0.087, 0.087]	NOMAD
$\epsilon_{ au e}^{udR}$	[-0.12, 0.12]	NOMAD
$\epsilon_{\tau\mu}^{udL}$	[-0.013, 0.013]	NOMAD
$\epsilon_{ au\mu}^{udR}$	$\left[-0.018, 0.018\right]$	NOMAD
		purely leptonic N
$\epsilon_{\alpha e}^{\mu e L}, \epsilon_{\alpha e}^{\mu e R}$	[-0.025, 0.025]	KARMEN
$\epsilon_{\alpha\beta}^{\mu e L}$, $\epsilon_{\alpha\beta}^{\mu e R}$	[-0.030, 0.030]	kinematic G_F

Current Constraints* on CC NSI

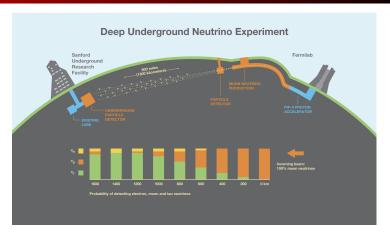
[Farzan, Tortola, 1710.09360]			
	90% C.L. range	origin	
		semileptonic NSI	
ϵ_{ee}^{udP}	[-0.015, 0.015]	Daya Bay	
$\epsilon_{e\mu}^{udL}$	[-0.026, 0.026]	NOMAD	
$\epsilon_{e\mu}^{udR}$	[-0.037, 0.037]	NOMAD	
$\epsilon_{ au e}^{udL}$	[-0.087, 0.087]	NOMAD	
$\epsilon_{ au e}^{udR}$	[-0.12, 0.12]	NOMAD	
$\epsilon_{ au\mu}^{udL}$	[-0.013, 0.013]	NOMAD	
$\epsilon_{ au\mu}^{udR}$	[-0.018, 0.018]	NOMAD	
		purely leptonic NSI	
$\epsilon_{\alpha e}^{\mu e L}, \epsilon_{\alpha e}^{\mu e L}$	R [-0.025, 0.025]	KARMEN	
$\epsilon^{\mu e L}_{\alpha \beta}, \; \epsilon^{\mu e}_{\alpha \beta}$	[-0.030, 0.030]	kinematic G_F	

- From model-building perspective, getting 'large' CC NSI is more difficult than NC NSI.
- In some models (with purely leptonic NSI), CC and NC NSI are correlated by Fierz transformation.
- We will mostly focus on NC NSI (unless otherwise specified).

Global Fit

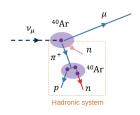


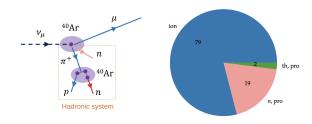
Future Prospects at DUNE

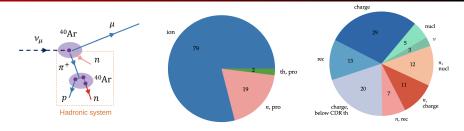


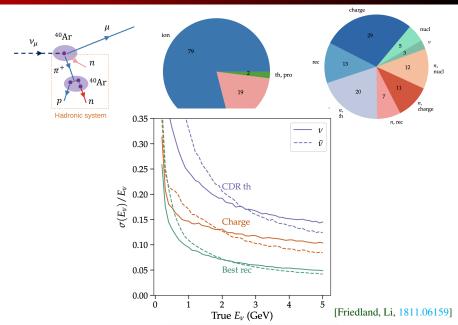
- Long baseline, huge statistics, intense & well-characterized beam.
- Excellent sensitivity to matter NSI.

[de Gouvêa, Kelly, 1511.05562; Coloma, 1511.06357; Blennow *et al.*, 1606.08851; Liao, Marfatia, Whisnant, 1612.01443; Chatterjee *et al.*, 1809.09313; Han *et al.*, 1910.03272]

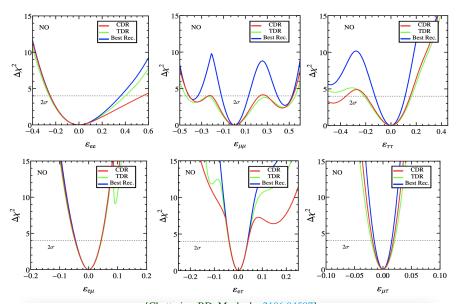




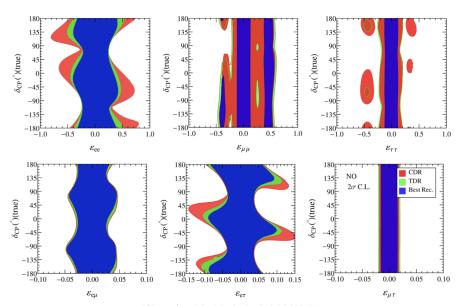




Improved DUNE Sensitivity to NSI

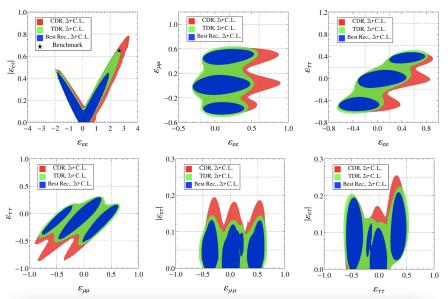


Dependence on δ_{CP}

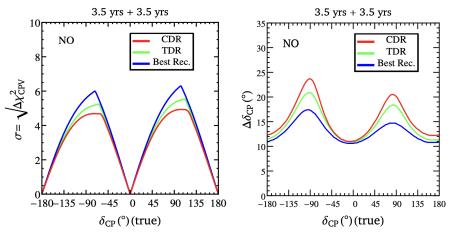


[Chatterjee, BD, Machado, 2106.04597]

Breaking Degeneracies



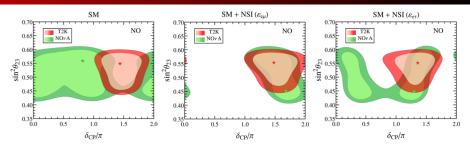
Improved $\delta_{\rm CP}$ Sensitivity



[Chatterjee, BD, Machado, 2106.04597;

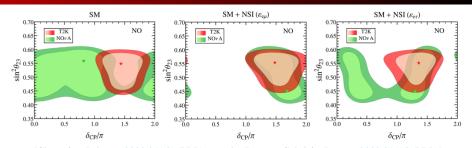
see also De Romeri, Fernandez-Martinez, Sorel,, 1607.00293]

Hint of NSI?



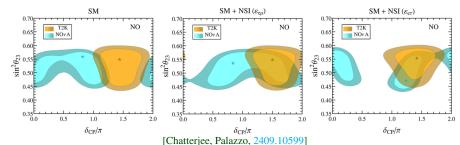
 $[Chatterjee, Palazzo, \\ 2008.04161 \ (PRL); see also \ Denton, Gehrlein, Pestes \\ , \\ 2008.01110 \ (PRL)]$

Hint of NSI?

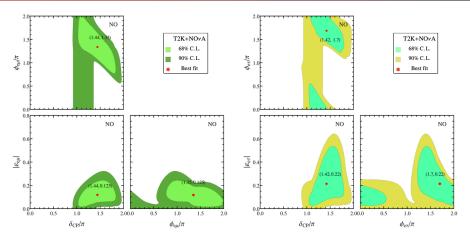


[Chatterjee, Palazzo, 2008.04161 (PRL); see also Denton, Gehrlein, Pestes, 2008.01110 (PRL)]

T2K-NOν**A** anomaly persists in 2024 data!

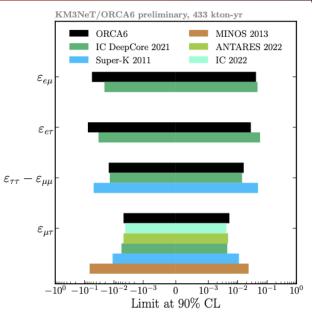


But not conclusive yet!



[Chatterjee, Palazzo, 2409.10599]

Strong constraints from IceCube and KM3NeT



[KM3NeT,, ICRC 2023; IceCube, 2201.03566 (PRL)]

Outline

- Lecture 1: NSI Basics
- Lecture 2: NSI Model Building and Phenomenology
 - Main challenge
 - EFT approach
 - UV-completion
 - Heavy mediators
 - Light mediators
 - Loop-induced NSI
- Lecture 3: Beyond ε Scalar NSI, NSSI, Neutrino-DM interactions, ...

NSI Model Building

• In the standard parametrization, NSI is a non-renormalizable, dimension-6 operator:

$$\mathcal{L}_{\mathrm{NSI}} = -2\sqrt{2}G_{F}\varepsilon_{\alpha\beta}^{fX}(\bar{\nu}_{\alpha}\gamma^{\mu}P_{L}\nu_{\beta})(\bar{f}\gamma_{\mu}P_{X}f)$$

$$\boxed{\varepsilon_{\alpha\beta} \sim \frac{g_{\Lambda}^{2}m_{W}^{2}}{\Lambda^{2}}}$$

- Two regimes to get 'observable' NSI, i.e. $\varepsilon_{\alpha\beta} \sim \mathcal{O}(1)$:
 - Heavy mediator: $g_{\Lambda} \sim \mathcal{O}(1)$ and $\Lambda \gtrsim m_W$.
 - Light mediator: $g_{\Lambda} \ll 1$ and $\Lambda \ll m_W$ such that $g_{\Lambda}^2/\Lambda^2 \sim \mathcal{O}(G_F)$.

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- Two regimes to get 'observable' NSI, i.e. $\varepsilon_{\alpha\beta} \sim \mathcal{O}(1)$:
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 - Light mediator: $g_{\Lambda} \ll 1$ and $\Lambda \ll m_W$ such that $g_{\Lambda}^2/\Lambda^2 \sim \mathcal{O}(G_F)$.
- EFT approach is valid in *both* cases as long as $q^2 \ll \Lambda^2$.
- Always true for matter NSI, since $q^2 \to 0$ for coherent forward scattering.

31

Main Challenge

- ullet The NSI operator by itself is not $SU(2)_L$ gauge-invariant.
- Restoring gauge invariance in a renormalizable, UV-complete model will in general impose stringent constraints on NSI.

[Gavela, Hernandez, Ota, Winter, 0809.3451; Biggio, Blennow, Fernandez-Martinez, 0907.0097]

Main Challenge

- The NSI operator by itself is not $SU(2)_L$ gauge-invariant.
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[Gavela, Hernandez, Ota, Winter, 0809.3451; Biggio, Blennow, Fernandez-Martinez, 0907.0097]

• Consider the leptonic NSI operator of the form

$$\frac{1}{\Lambda^2}(\bar{\nu}_{\alpha}\gamma^{\mu}P_L\nu_{\beta})(\bar{\ell}_{\gamma}\gamma_{\mu}P_L\ell_{\delta}).$$

• In a UV-complete theory, it must be part of the more general form

$$\frac{1}{\Lambda^2}(\bar{L}_{\alpha}\gamma^{\mu}L_{\beta})(\bar{L}_{\gamma}\gamma_{\mu}L_{\delta}).$$

- Severely constrained by rare LFV processes like $\mu \to 3e$, viz. $\mathrm{BR}(\mu \to 3e) < 10^{-12}$ implies $\varepsilon_{e\mu}^e \lesssim 10^{-6}$.
- Similar constraints for quark NSI from atomic parity violation, CKM unitarity, etc. [Antusch, Baumann, Fernandez-Martinez, 0807.1003]

Why do we care?

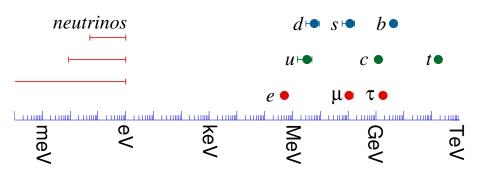
- Are there realistic UV-complete models having observable NSI?
- Important in order to understand which sort of new physics the neutrino experimental program is actually probing when model-independent NSI constraints are presented.
- Complementarity of neutrino oscillation and scattering experiments with traditional low- and high-energy experiments searching for new physics.

32

Why do we care?

- Are there realistic UV-complete models having observable NSI?
- Important in order to understand which sort of new physics the neutrino experimental program is actually probing when model-independent NSI constraints are presented.
- Complementarity of neutrino oscillation and scattering experiments with traditional low- and high-energy experiments searching for new physics.
- After all, neutrinos are the first (and so far only) ones to give concrete laboratory evidence of new physics.
- Can we use NSI to probe neutrino mass physics?
- Oscillation physics is insensitive to absolute neutrino mass, but not necessarily to the origin of neutrino mass.

Neutrino Mass Mechanism



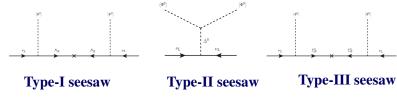
- \bullet Simplest solution: Add right-handed neutrinos N.
- Gives Dirac Yukawa term $Y_D L H N$ +H.c.
- After EWSB, gives Dirac neutrino mass $M_D = Y_D v$.
- But $m_{\nu} \lesssim 0.1$ eV implies $Y_D \lesssim 10^{-12}$. Possible but ugly!
- Perhaps something (beautiful) beyond the SM Higgs mechanism?

Seesaw Mechanism

- One possibility is to break the accidental B-L symmetry of the SM by higher-dimensional operators.
- Lowest-order is dimension-5 Weinberg operator: [Weinberg,, PRL '79]

$$\mathcal{O}_1 = \frac{1}{\Lambda} L^i L^j H^k H^l \epsilon_{ik} \epsilon_{jl}.$$

Only 3 tree-level realizations: [Ma,, hep-ph/9805219 (PRL)]



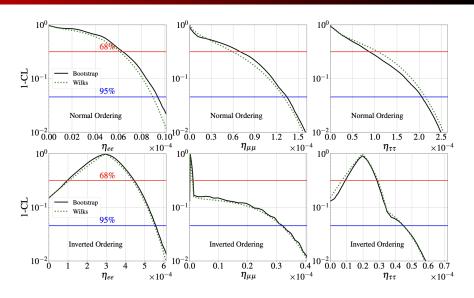
Minkowski (PLB '77); Moha- Schechter, Valle (PRD '80); Foot, Lew, He, Joshi (ZPC patra, Senjanovic (PRL '80); Lazarides, Shafi, Wetterich '89)

Yanagida '79; Gell-Mann, Ra- (NPB '81); Mohapatra, Senmond, Slansky '79 janovic (PRD '81)

NSI in Type-I Seesaw

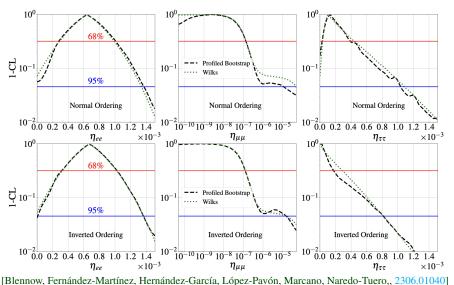
- Related to non-unitarity in the neutrino mixing matrix. [Blennow, Coloma, Fernandez-Martinez, Hernandez-Garcia, Lopez-Pavon, 1609.08637]
- The seesaw mass matrix $\mathcal{M}_{\nu} = \begin{pmatrix} 0 & M_D \\ M_D^T & M_N \end{pmatrix}$ is diagonalized by a $(3+n) \times (3+n)$ unitarity matrix $\mathcal{U} = \begin{pmatrix} U & R \\ S & V \end{pmatrix}$.
- $U \simeq (1 \eta) U_{\rm PMNS}$ with $\eta = R R^{\dagger} / 2$ and $R \simeq M_D M_N^{-1}$.
- $\varepsilon_{\alpha\beta}$ are identical to $\eta_{\alpha\beta}$ (up to a factor of 2 for the off-diagonals).
- Can also be derived from 'first principles' using the canonical diagonalization of the kinetic term. [Broncano, Gavela, Jenkins, hep-ph/0210271]
- Stringent constraints on non-unitarity from EWPD, LFV, CKM unitarity,
 etc. [Antusch, Biggio, Fernandez-Martinez, Gavela, Lopez-Pavon, hep-ph/0607020; Antusch,
 Fischer, 1407.6607]; Blennow, Fernández-Martínez, Hernández-García, López-Pavón, Marcano,
 Naredo-Tuero,, 2306.01040]

Global Analysis of NSI with 2 RHNs



[Blennow, Fernández-Martínez, Hernández-García, López-Pavón, Marcano, Naredo-Tuero,, 2306.01040]

Global Analysis of NSI with 3 RHNs



Mild preference for non-zero NSI at 10^{-4} level (in ee and $\tau\tau$) for NO.

NSI in Type-II Seesaw

• SM+ a scalar triplet $\Delta = \begin{pmatrix} \frac{\Delta^+}{\sqrt{2}} & \Delta^{++} \\ \Delta^0 & -\frac{\Delta^+}{\sqrt{2}} \end{pmatrix}$ [Schechter, Valle '80]

$$\mathcal{L}_Y = Y_{\alpha\beta} \left[\Delta^0 \overline{\nu_{\alpha R}^C} \nu_{\beta L} - \frac{1}{\sqrt{2}} \Delta^+ \left(\overline{\ell_{\alpha R}^C} \nu_{\beta L} + \overline{\nu_{\alpha R}^C} \ell_{\beta L} \right) - \Delta^{++} \overline{\ell_{\alpha R}^C} \ell_{\beta L} \right] + \text{h.c.}$$

• Integrating out the triplet scalars (with mass M_{Δ}),

$$\mathcal{L}_{\nu}^{m} = \frac{Y_{\alpha\beta} \, \lambda_{\phi} \, v^{2}}{M_{\Delta}^{2}} \, \left(\overline{\nu_{\alpha R}^{C}} \, \nu_{\beta L} \right) = -\frac{1}{2} \, (m_{\nu})_{\alpha\beta} \, \overline{\nu_{\alpha R}^{C}} \, \nu_{\beta L}, \quad \nu_{\beta}$$

$$\mathcal{L}_{\mathrm{NSI}} = \frac{Y_{\sigma\beta} \, Y_{\alpha\rho}^{\dagger}}{M_{\Delta}^{2}} \, \left(\overline{\nu_{\alpha L}} \, \gamma_{\mu} \, \nu_{\beta L} \right) \, \left(\overline{\ell_{\rho L}} \, \gamma^{\mu} \, \ell_{\sigma L} \right), \qquad \ell_{\sigma}$$

• Leads to the NSI parameters

$$\varepsilon_{\alpha\beta}^{\rho\sigma} = -\frac{M_{\Delta}^2}{8\sqrt{2}G_F v^4 \lambda_{\phi}^2} (m_{\nu})_{\sigma\beta} (m_{\nu}^{\dagger})_{\alpha\rho},$$

NSI in Type-II Seesaw

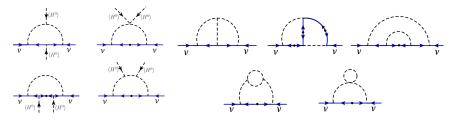
Strongly constrained by cLFV, neutrino mass and lab constraints on Δ^+ .

Decay	Constraint on	Bound
$\mu^- \to e^- e^+ e^-$	$ arepsilon_{ee}^{e\mu} $	3.5×10^{-7}
$\tau^- \to e^- e^+ e^-$	$ arepsilon^{e au}_{ee} $	1.4×10^{-4}
$\tau^- \to \mu^- \mu^+ \mu^-$	$ arepsilon^{\mu au}_{\mu\mu} $	1.2×10^{-4}
$\tau^- \to e^- \mu^+ e^-$	$ \varepsilon_{e\mu}^{e au} $	1.0×10^{-4}
$\tau^- \to \mu^- e^+ \mu^-$	$ arepsilon_{\mu e}^{\mu au} $	1.0×10^{-4}
$\tau^- \to e^- \mu^+ \mu^-$	$ arepsilon_{\mu\mu}^{e au} $	1.0×10^{-4}
$\tau^- \to e^- e^+ \mu^-$	$ arepsilon^{e au}_{\mu e} $	9.9×10^{-5}
$\mu^- \to e^- \gamma$	$ \sum_{\alpha} \varepsilon_{\alpha\alpha}^{e\mu} $	2.6×10^{-5}
$\tau^- \to e^- \gamma$	$ \sum_{\alpha} \varepsilon_{\alpha\alpha}^{e au} $	1.8×10^{-2}
$\tau^- \to \mu^- \gamma$	$ \sum_{\alpha} \varepsilon_{\alpha\alpha}^{\mu au} $	2.0×10^{-4}
$\mu^+e^- \to \mu^-e^+$	$ arepsilon_{\mu e}^{\mu e} $	3.0×10^{-3}

[Huitu, Karkkainen, Maalampi, Vihonen, 1711.02971]

Radiative Neutrino Mass Models

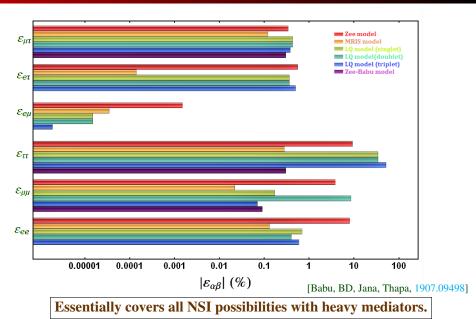
- Attractive alternative to tree-level seesaw.
- In-buit loop (and chiral) suppression factors naturally allows for lower new physics scale.



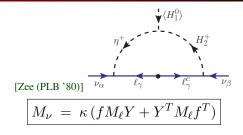
[Zee (PLB '80; NPB '86); Babu (PLB '88); Cai, Herrero-Garcia, Schmidt, Vicente, Volkas, 1706.08524]

40

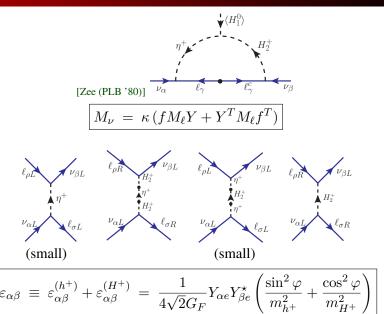
NSI in Radiative Neutrino Models

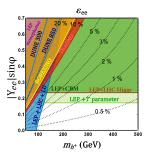


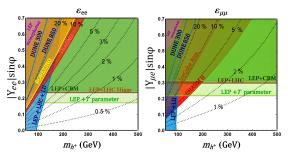
An Example: Zee Model

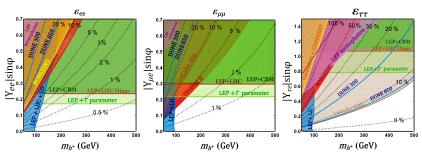


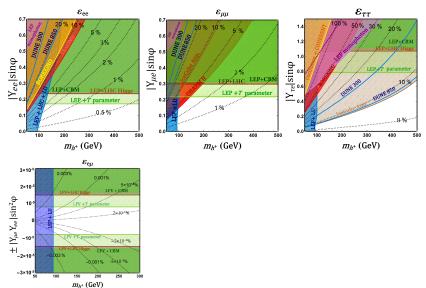
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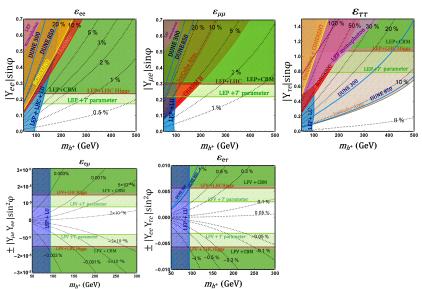


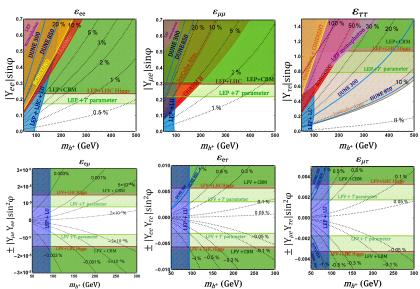


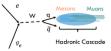












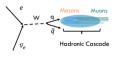
[Glashow (PR '60)]

Glashow resonance

$$E_{\nu}=\frac{m_W^2}{2m_e}=6.3~{\rm PeV}$$

Observed by IceCube

[Nature **591**, 220 (2021)]



[Glashow (PR '60)]

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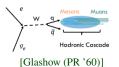
[Nature **591**, 220 (2021)]

$$\begin{array}{c} \nu \\ Z^0 \end{array} \qquad \begin{array}{c} \text{Mesons} \\ \overline{q} \end{array}$$

[Weiler (PRL '82)]

$$\begin{split} & \frac{Z\text{-burst}}{E_{\nu} = \frac{m_Z^2}{2m_{\nu}}} > 10^{14} \text{ GeV} \\ & \text{Beyond GZK cutoff} \end{split}$$

Unlikely to be seen

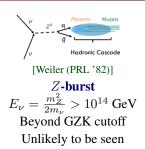


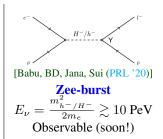
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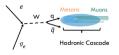
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[Nature **591**, 220 (2021)]





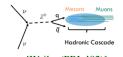


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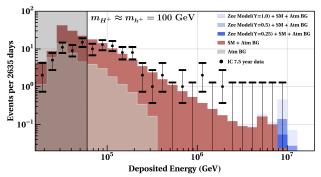
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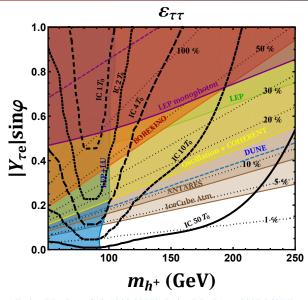
Unlikely to be seen



 $E_{\nu} = \frac{m_{h^-/H^-}^2}{2m_e} \gtrsim 10 \text{ PeV}$ Observable (soon!)



A New Probe of NSI using UHE Neutrinos



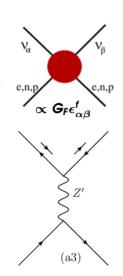
[Babu, BD, Jana, Sui, 1908.02779; Babu, BD, Jana, 2202.06975]

NSI with Light Mediators

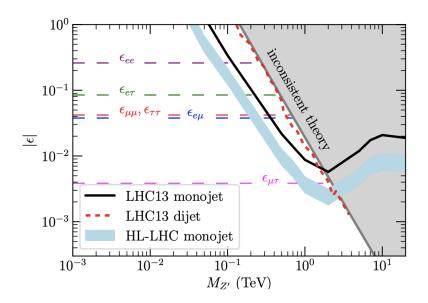
- Still lacking a comprehensive UV-complete exploration.
- Possible to avoid cLFV constraints with flavored light mediators.
- An explicit example with $(B-L)_3$ flavored light Z'. [Babu, Friedland, Machado, Mocioiu, 1705.01822]
- Large diagonal $\varepsilon_{\tau\tau}$ up to $\sim 50\%$.
- How about large off-diagonal NSI?
- In general, for light Z',

$$\varepsilon_{\alpha\beta}^f = \frac{g_f(g_\nu)_{\alpha\beta}}{2\sqrt{2}G_F m_{Z'}^2}$$

• An explicit example violating the Schwartz inequality, i.e. $|\varepsilon_{\alpha\beta}^f| > |\varepsilon_{\alpha\alpha}^f \varepsilon_{\beta\beta}^f|^{1/2}$, with $U(1)' \times Z_2$. [Farzan, 1912.09408]

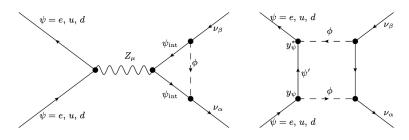


LHC Probe of NSI



[Babu, Gonçalves, Jana, Machado, 2003.03383]

Loop-induced NSI



$$\mathcal{L}_{\mathrm{NSI}} = \left(\epsilon_{\alpha\beta}^{\triangleright} + \epsilon_{\alpha\beta}^{\square}\right) \frac{G_F}{\sqrt{2}} \overline{\psi} \gamma^{\mu} \psi \overline{\nu_{\alpha}} \gamma_{\mu} P_L \nu_{\beta}, \quad (\psi = e_L, \ e_R, \ u_L, \ u_R, \cdots),$$

$$\epsilon_{\alpha\beta}^{\triangleright} = -\frac{8g_{\alpha\beta}^{(1)}}{g} Q_Z^{(\psi)} c_W, \quad \epsilon_{\alpha\beta}^{\square} = \frac{1}{16\pi^2} \frac{\sqrt{2} y_{\alpha}^* y_{\beta} |y_{\psi}|^2}{4m_{\phi}^2 G_F}.$$

	ϵ_e^F	$\epsilon_e^{\triangleright}$	$\epsilon_n^{ hd}$	$\epsilon_p^{\triangleright}$	ϵ_e^\square	ϵ_n^\square	ϵ_p^\square
model A	$O(10^{-3})$	$O(10^{-5})$	$O(10^{-4})$	$O(10^{-5})$	$O(10^{-3})$	0	0
model B	0	$O(10^{-1})$	$\mathcal{O}(1)$	$O(10^{-1})$	0	0	0
$\bmod el \ C$	0	0	0	0	$\mathcal{O}(10^{-2})$	$\mathcal{O}(10^{-2})$	$O(10^{-2})$

Outline

- Lecture 1: NSI Basics
- Lecture 2: NSI Model Building and Phenomenology
- Lecture 3: Going beyond ε
 - Scalar NSI
 - Neutrino Self Interactions
 - Neutrino-DM interactions

Going beyond Vector NSI

• Recall that the matter NSI operator involves (axial)vector currents:

$$\mathcal{L}_{\mathrm{NSI}}^{\mathrm{NC}} = -2\sqrt{2}G_{F}\varepsilon_{\alpha\beta}^{fX}(\bar{\nu}_{\alpha}\gamma^{\mu}P_{L}\nu_{\beta})(\bar{f}\gamma_{\mu}P_{X}f).$$

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- For a leptonic charged scalar mediator, the NSI operator can be Fierz-transformed to the usual form.
- For instance, in the Zee model: [Babu, BD, Jana, Thapa, 1907.09498]

$$\mathcal{L}_{\text{eff}}^{h^{+}} = \sin^{2}\varphi \frac{Y_{\alpha\rho}Y_{\beta\sigma}^{*}}{m_{h^{+}}^{2}} (\bar{\nu}_{\alpha L}\ell_{\rho R})(\bar{\ell}_{\sigma R}\nu_{\beta L})$$

$$= -\frac{1}{2}\sin^{2}\varphi \frac{Y_{\alpha\rho}Y_{\beta\sigma}^{*}}{m_{h^{+}}^{2}} (\bar{\nu}_{\alpha}\gamma^{\mu}P_{L}\nu_{\beta})(\bar{\ell}_{\sigma}\gamma_{\mu}P_{R}\ell_{\rho}).$$

50

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$$= -\frac{1}{2}\sin^{2}\varphi \frac{Y_{\alpha\rho}Y_{\beta\sigma}^{*}}{m_{\tau}^{2}} (\bar{\nu}_{\alpha}\gamma^{\mu}P_{L}\nu_{\beta})(\bar{\ell}_{\sigma}\gamma_{\mu}P_{R}\ell_{\rho}).$$

But for a neutral scalar mediator,

$$\mathcal{L}_{ ext{eff}}^{\phi} \; = \; rac{y_f y_{lphaeta}}{m_{\perp}^2} (ar{
u}_{lpha}
u_{eta}) (ar{f} f) \, ,$$

which cannot be Fierzed into a vector current, so it does not contribute to the matter potential.

• Same is true for a tensor current $(\bar{\nu}_{\alpha}\sigma^{\mu\nu}\nu_{\beta})(\bar{f}\sigma_{\mu\nu}f)$.

Scalar NSI

$${\cal L} \;\supset\; -y_{lphaeta}\overline{
u}_lpha\phi
u_eta-y_far{f}\phi f-m_{lphaeta}\overline{
u}_lpha
u_eta-rac{m_\phi^2}{2}\phi^2\,.$$

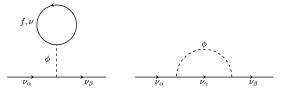
• NSI induced by a neutral scalar mediator:

$$\mathcal{L}_{\text{eff}}^{\phi} = \frac{y_f y_{\alpha\beta}}{m_{\phi}^2} (\bar{\nu}_{\alpha} \nu_{\beta}) (\bar{f} f) ,$$

appears as a medium-dependent correction to the neutrino mass.

[Ge, Parke, 1812.08376; Smirnov, Xu, 1909.07505]

 Field-theoretic understanding from neutrino self-energy correction at finite temperature and density: [Babu, Chauhan, BD, 1912.13488]



$$\Sigma_{\alpha\beta} \; = \; rac{y_{lphaeta}y_{ff}m_{f}}{\pi^{2}m_{\phi}^{2}}\int_{m_{f}}^{\infty}dk_{0}\,\sqrt{k_{0}^{2}-m_{f}^{2}}\left[n_{f}(k_{0})+n_{ar{f}}(k_{0})
ight] \; \equiv \; \Delta m_{
u,lphaeta} \; .$$

$$\begin{split} \Sigma_{\alpha\beta} \; &= \; \frac{y_{\alpha\beta}y_f m_f}{\pi^2 m_\phi^2} \int_{m_f}^{\infty} dk_0 \, \sqrt{k_0^2 - m_f^2} \left[n_f(k_0) + n_{\bar{f}}(k_0) \right] \; \equiv \; \Delta m_{\nu,\alpha\beta} \; . \\ \Delta m_{\nu,\alpha\beta} \; &= \; \begin{cases} \frac{y_f y_{\alpha\beta}}{m_\phi^2} \left(N_f + N_{\bar{f}} \right) & (\mu, T \ll m_f) \\ \\ \frac{y_f y_{\alpha\beta}}{m_\phi^2} \frac{m_f}{2} \left(\frac{3}{\pi} \right)^{\frac{2}{3}} \left(N_f^{2/3} + N_{\bar{f}}^{2/3} \right) & (\mu > m_f \gg T) \\ \\ \frac{y_f y_{\alpha\beta} m_f}{3 \, m_\phi^2} \left(\frac{\pi^2}{12 \, \zeta(3)} \right)^{\frac{2}{3}} \left(N_f^{2/3} + N_f^{2/3} \right) & (\mu < m_f \ll T) \; . \end{cases} \end{split}$$

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Special cases:

• Earth and Sun: $N_{\bar{f}}=0$ and non-relativistic background of electrons and nucleons. Include finite-medium correction for light mediators $m_{\phi} \lesssim R^{-1}$.

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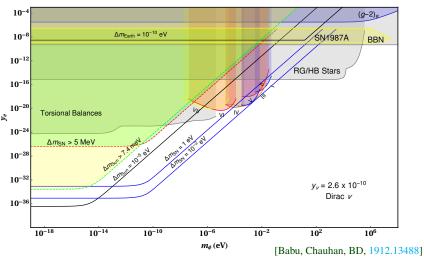
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- Earth and Sun: $N_{\bar{f}}=0$ and non-relativistic background of electrons and nucleons. Include finite-medium correction for light mediators $m_{\phi} \lesssim R^{-1}$.
- Supernova: Background nucleons are non-relativistic but electrons are relativistic. Additional effects from large thermal mass and trapping of the scalar.
- Early Universe: High-temperature limit. Thermal background of neutrinos is relevant.

Constraints on Scalar NSI



- Need $G_{\rm eff} \equiv y_f y_{\alpha\beta}/m_\phi^2 \sim 10^{10} G_F$ to have any observable effect.
- Possible only for a sufficiently light scalar mediator.
- Connection to Hubble tension? [see A. Trautner's lecture]

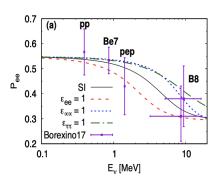
Comparison of Vector and Scalar NSI Effects

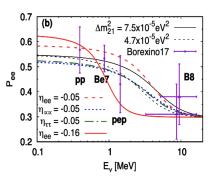
$$\delta \mathbb{M}_{lphaeta} \equiv \sqrt{|\Delta m_{31}^2|} egin{pmatrix} \eta_{ee} & \eta_{e\mu}e^{i\phi_{e\mu}} & \eta_{e au}e^{i\phi_{e au}} \ \eta_{e\mu}e^{-i\phi_{e\mu}} & \eta_{\mu\mu} & \eta_{\mu au}e^{i\phi_{\mu au}} \ \eta_{e au}e^{-i\phi_{e au}} & \eta_{\mu au}e^{-i\phi_{\mu au}} & \eta_{ au au} \end{pmatrix} \ \eta_{lphaeta} = rac{n_f y_f y_{lphaeta}}{\sqrt{|\Delta m_{31}^2|}m_{lpha}^2} \ \end{pmatrix}$$

Comparison of Vector and Scalar NSI Effects

$$\delta \mathbb{M}_{\alpha\beta} \equiv \sqrt{|\Delta m_{31}^2|} \begin{pmatrix} \eta_{ee} & \eta_{e\mu} e^{i\phi_{e\mu}} & \eta_{e\tau} e^{i\phi_{e\tau}} \\ \eta_{e\mu} e^{-i\phi_{e\mu}} & \eta_{\mu\mu} & \eta_{\mu\tau} e^{i\phi_{\mu\tau}} \\ \eta_{e\tau} e^{-i\phi_{e\tau}} & \eta_{\mu\tau} e^{-i\phi_{\mu\tau}} & \eta_{\tau\tau} \end{pmatrix}$$

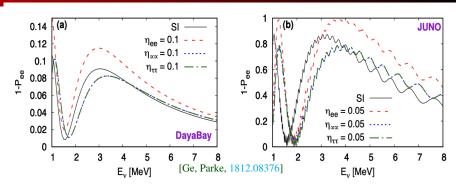
$$\eta_{lphaeta} = rac{n_f y_f y_{lphaeta}}{\sqrt{|\Delta m_{31}^2|} m_\phi^2}$$



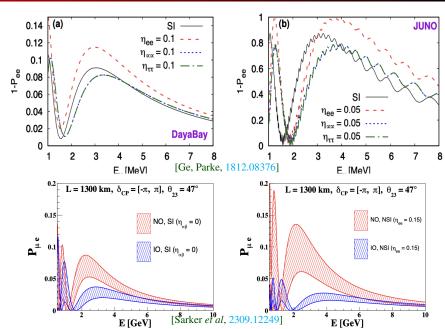


[Ge, Parke, 1812.08376 (PRL)]

Future Prospects

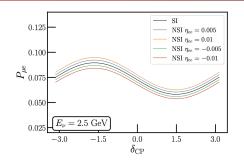


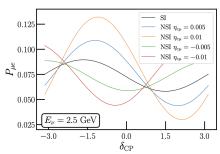
Future Prospects



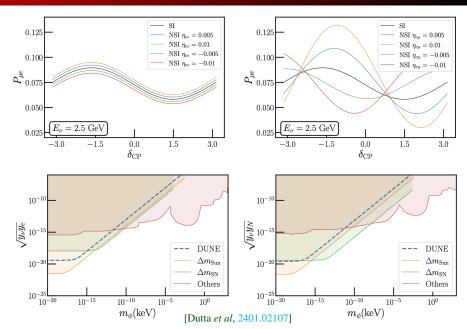
55

Future Prospects at DUNE



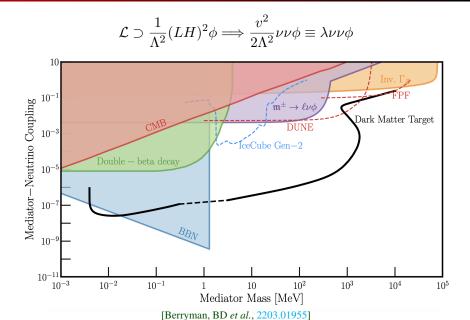


Future Prospects at DUNE

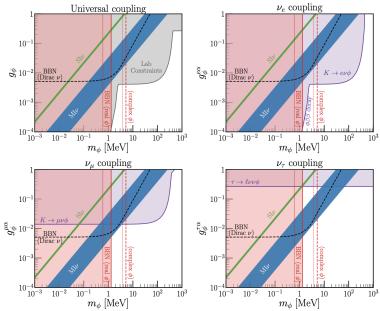


56

Neutrino Non-Standard Self-Interactions

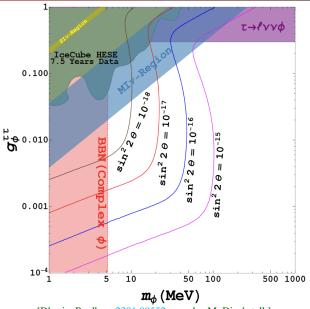


Hubble Tension



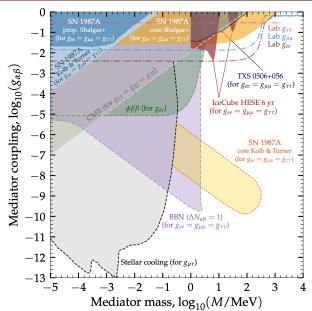
[Blinov et al., 1905.02727 (PRL); see also A. Trautner's lecture]

Sterile Neutrino Dark Matter Production

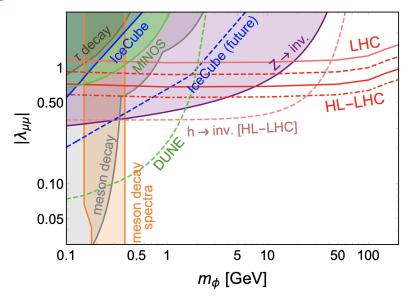


[Dhuria, Pradhan, 2301.09552; see also M. Dias's talk]

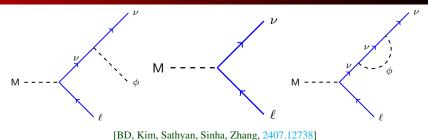
Astrophysical Constraints

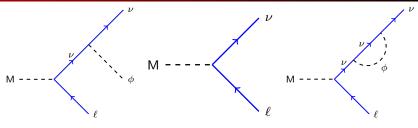


Laboratory Probes



[de Gouvêa, BD, Dutta, Ghosh, Han, Zhang, 1910.01132]

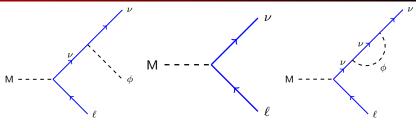




[BD, Kim, Sathyan, Sinha, Zhang, 2407.12738]

$$\Gamma^{\rm tree}({\sf M} \to \ell + \nu + \phi) \simeq \frac{G_F^2 m_{\sf M}^3 f_{\sf M}^2 |V|^2 g_\nu^2}{128 \pi^3} \left[-x_{\ell \sf M} (1-x_{\ell \sf M})^2 \log x_{\phi \sf M} + C_2(x_{\ell \sf M}) \right] \,, \tag{1}$$

$$\Delta\Gamma^{\rm loop}(\mathsf{M}\to\ell+\nu) = -\; \frac{g_\nu^2 G_F^2 m_{\mathsf{M}} m_\ell^2 f_{\mathsf{M}}^2 |V|^2}{128\pi^3} \left(1-x_{\ell\mathsf{M}}\right)^2 \left[\frac{5}{2} - \log\frac{x_{\phi\mathsf{M}} (1-x_{\ell\mathsf{M}})^2}{16\pi^2}\right]. \quad (2)$$

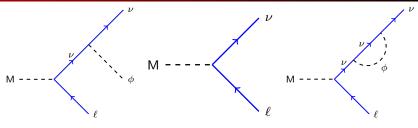


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The IR divergent part $x_{\ell M}(1-x_{\ell M})^2 \log x_{\phi M}$ cancels between (1) & (2).



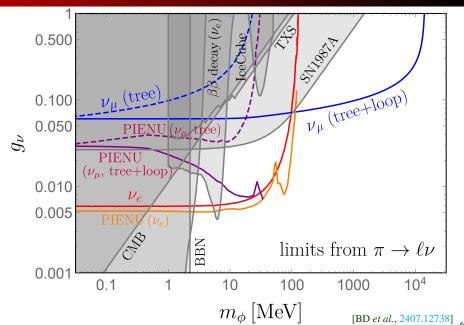
[BD, Kim, Sathyan, Sinha, Zhang, 2407.12738]

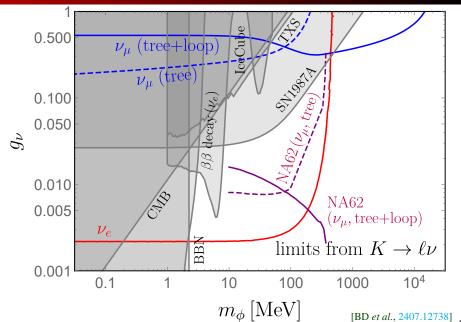
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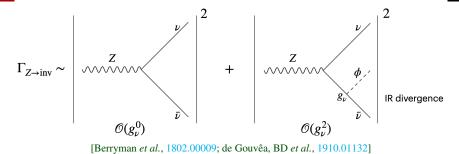
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Consequence of the KLN theorem. [Kinoshita '62; Lee, Nauenberg '64]

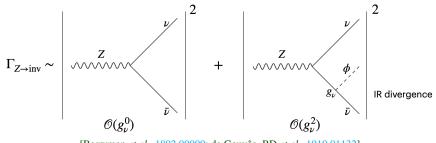




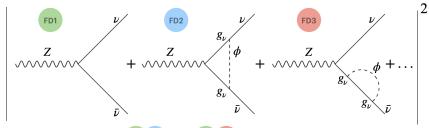
Updated Z Decay Constraints



Updated Z Decay Constraints



[Berryman et al., 1802.00009; de Gouvêa, BD et al., 1910.01132]

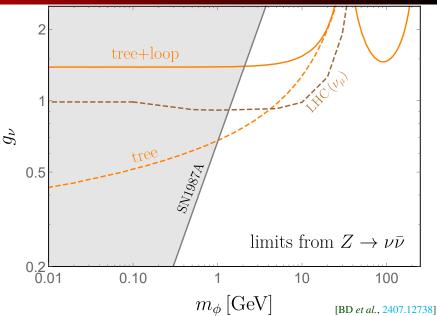


Interference terms FD1 FD2 and FD1 FD3 are $\mathcal{O}(g_{\nu}^2)$, like tree level $Z \to \nu\nu\phi$

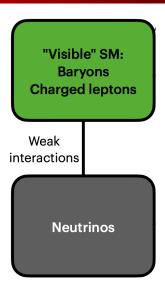
[Brdar, Lindner, Vogl, Xu, 2003.05339; BD, Kim, Sathyan, Sinha, Zhang, 2407.12738]

65

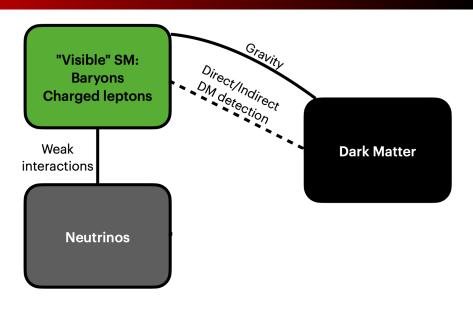
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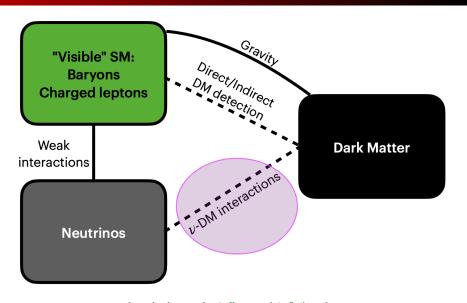
Neutrino-Dark Matter Interactions



Neutrino-Dark Matter Interactions



Neutrino-Dark Matter Interactions



[see also lectures by A. Ibarra and A. Smirnov]

69

How to Observe ν -DM Interactions Today?



$$\mathbf{Opacity}: \tau \ = \ \sigma_{\nu\chi} \int dl \, \frac{\rho_\chi(l)}{m_\chi}$$

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How to Observe ν -DM Interactions Today?



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• Large number density \Longrightarrow **Light DM**.

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7

Existing Constraints

• Cosmological:

- BBN and CMB [Serpico, Raffelt '04; Bœhm, Dolan, McCabe '13; Escudero '18; Giovanetti, Schmaltz, Weiner '24]
- Reionization History [Dey, Paul, Pal '22; Mosbech, Bohm, Wong '22]

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• Astrophysical:

- SN1987A and future galactic SN [Mangano et al '06; Fayet, Hooper, Sigl '06]
- DSNB (future) [Farzan, Palomares-Ruiz '14]
- AGNs [Arguelles, Kheirandish, Vincent '17; Murase, Shoemaker '19; Cline et al '22; Ferrer, Herrera, Ibarra '22]
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 Palomares-Ruiz, Pascoli '07; Covi, Grefe, Ibarra '09; El Aisati et al '17]
- Laboratory: Meson decays, Z decay, τ decay, double beta decay, ν scattering, etc. [Olivares-Del Campo, Bœhm, Palomares-Ruiz, Pascoli '17; Berryman et al. '18; Deppisch, Graf, Rodejohann, Xu '20; BD, Kim, Sathyan, Sinha, Zhang '24]

Modeling ν -DM Interactions

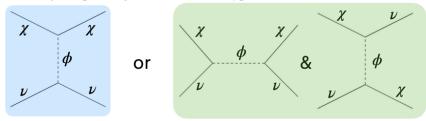
• Simplified EFT approach.

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[Olivares-Del Campo, Bœhm, Palomares-Ruiz, Pascoli, 1711.05283;
Blennow, Fernandez-Martinez, Olivares-Del Campo, Pascoli, Rosauro-Alcaraz, Titov, 1903.00006]
```

• Categorize models into DM and mediator types: Scalar, fermion, vector.

Modeling ν -DM Interactions

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 [Olivares-Del Campo, Boehm, Palomares-Ruiz, Pascoli, 1711.05283;
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- Categorize models into DM and mediator types: Scalar, fermion, vector.
- Secondary categorization: t-channel or s and u channel ν -DM scatterings, depending on the mediator type.



Only free parameters: DM and mediator masses and couplings.

Cross Sections

• Differential cross sections can be computed analytically and *exactly*.

$$\frac{\mathrm{d}\sigma}{\mathrm{d}\cos\theta} = \frac{1}{8\pi} \frac{E_{\nu}^{\prime 2}}{4m_{\chi}^{2}E_{\nu}^{2}} \sum_{\mathrm{spins}} \overline{|\mathcal{M}|^{2}},$$
where
$$\frac{1}{E_{\nu}^{\prime}} = \frac{1}{E_{\nu}} + \frac{1 - \cos\theta}{m_{\chi}}.$$

73

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• Consider one example scenario:

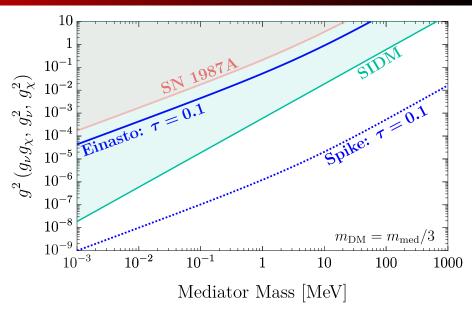
Dirac fermion DM, (pseudo)scalar mediator:

$$-\mathcal{L} = \phi \bar{\nu} (g_{\nu s} + i g_{\nu p} \gamma_5) \nu + \phi \bar{\chi} (g_{\chi s} + i g_{\chi p} \gamma_5) \chi.$$

$$\sum_{\text{spins}} |\mathcal{M}|^2 = 4 \left(g_{\nu s}^2 + g_{\nu p}^2 \right) \frac{t \left[g_{\chi s}^2 (t - 4m^2) + g_{\chi p}^2 t \right]}{(t - m_{\phi})^2},$$

where $t = -2E_{\nu}E'_{\nu}(1 - \cos \theta)$.

Astrophysical Bounds



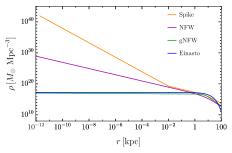


Is ν -DM Interaction Observable in a Future SN Event?

Depends on many things: DM density profile, location of the SN, DM and mediator masses and couplings.

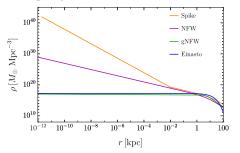
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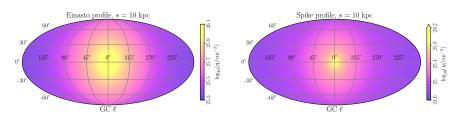
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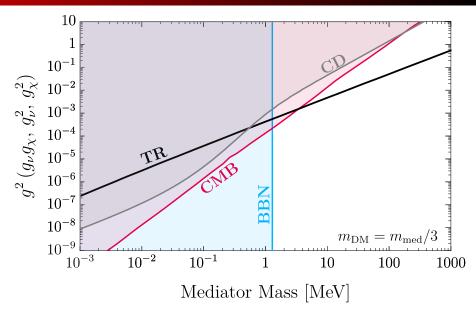
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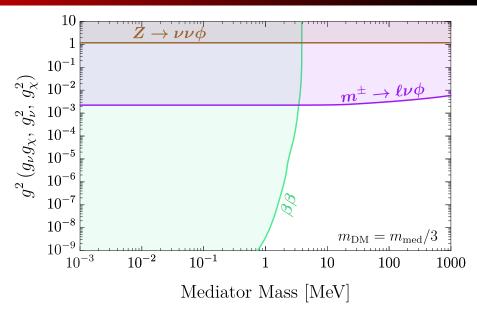




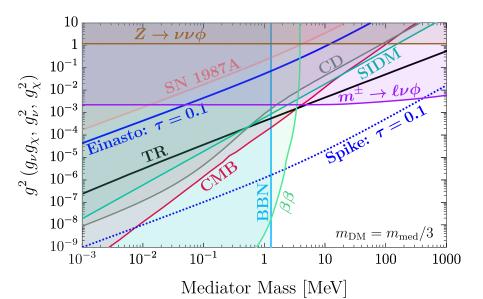
Cosmological Bounds



Laboratory Bounds

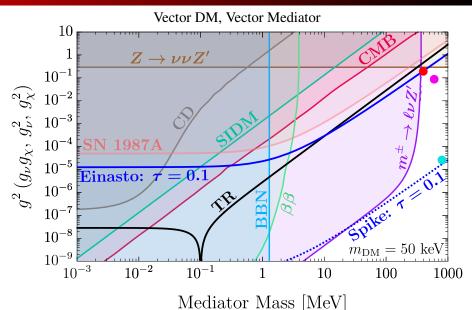


Combined ν -DM Constraints



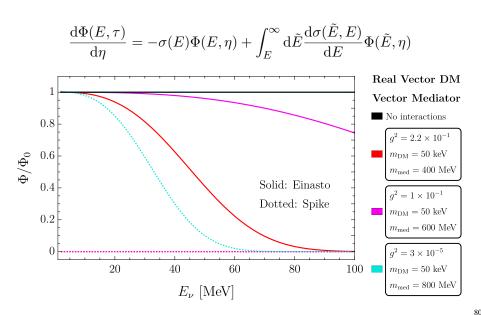
[BD, Kim, Sathyan, Sinha, Zhang, to appear (soon!)]

Best Case Scenario for Local Supernova

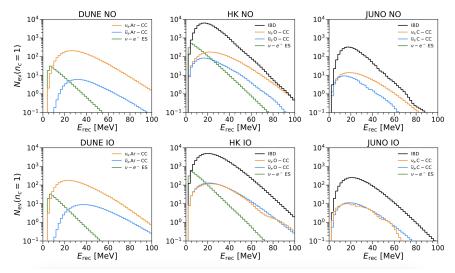


[BD, Kim, Sathyan, Sinha, Zhang, to appear]

SN Neutrino Flux Attenuation



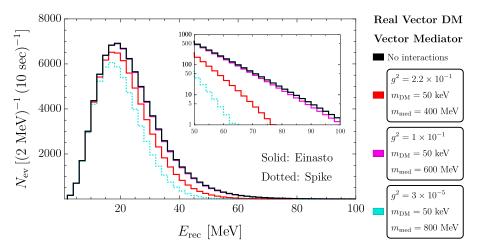
Event Distributions (Without Attenuation)



[Hajjar, Mena, Palomares-Ruiz, 2303.09369]

w/ Warren 20 SN neutrino spectrum [Warren, Couch, O'Connor, Morozova, 1912.03328]

Event Distributions (With Attenuation) at Hyper-K



Possible to detect ν -DM interaction but only for a spike profile.

[BD, Kim, Sathyan, Sinha, Zhang, to appear]

Conclusions

- Explaining neutrino mass requires new physics.
- Inevitably leads to NSI at some level.
- Understanding NSI effects is essential for the correct interpretation of the oscillation data.
- Possible to get observable NSI in UV-complete neutrino mass models.
- Heavy mediator case is done. Light mediator case requires more work.
- Going beyond vector NSI: Scalar NSI requires ultralight scalars.
- Neutrino self-interactions: Important implications for cosmology and astrophysics.
- Updated laboratory constraints on mediators.
- Neutrino-DM interactions and the case for a future galactic SN.