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COHERENT ELASTIC NEUTRINO-NUCLEUS SCATTERING

2nd EuCAPT Astroneutrino Theory Workshop IEAP CTU in Prague 16-27 September 2024

A FEW USEFUL REFERENCES

- Papers/Reviews:
 - <u>Coherent elastic neutrino-nucleus scattering: Terrestrial and astrophysical applications</u> M. Abdullah et al.
 - A view of Coherent Elastic Neutrino-Nucleus Scattering, M. Cadeddu, F. Dordei, C. Giunti
 - <u>Recent Probes of Standard and Non-standard Neutrino Physics With Nuclei</u>, Papoulias, Kosmas, Kuno
 - Probing new physics with coherent neutrino scattering off nuclei, Barranco, Miranda, Rashba
 - Walecka and Donnelly https://doi.org/10.1016/0375-9474(76)90209-8
- Dark Matter Direct detection:
 - The Theory of Direct Dark Matter Detection
 - <u>https://arxiv.org/pdf/1904.07915</u>
 - <u>https://arxiv.org/pdf/1002.1912</u>
- Books:
 - Walecka Theoretical Nuclear and Subnuclear Physics, Oxford Stud.Nucl.Phys. 16 (1995) 1-610
 - Giunti & Kim: <u>https://oxford.universitypressscholarship.com/view/10.1093/acprof:oso/</u> 9780198508717.001.0001/acprof-9780198508717
- ► Webpage:
 - http://www.nu.to.infn.it/Neutrino_Lectures
- Magnificent CEvNS workshop talks

OUTLINE

- 1. Introduction to $CE_{v}NS$ and main features
- 2. CE_vNS physics implications: SM
- 3. CEvNS physics implications: BSM

OUTLINE - 1st lecture

- Neutrino interactions with matter, especially nuclei
- CEvNS: introduction and features
- CEvNS: neutrino sources
- CEvNS: experiments and detection
- CEvNS: observations
- CEvNS cross section in the SM

NEUTRINO INTERACTIONS WITH MATTER

Neutrinos are elusive particles but not completely unfriendly



corresponding to the neutrino flavor



Adapted from Kate Scholberg



Adapted from Kate Scholberg



Adapted from Kate Scholberg



CEVNS: INTRODUCTION AND FEATURES



COHERENT ELASTIC NEUTRINO-NUCLEUS SCATTERING (CEVNS)

- ► Neutral-current process: $v + N(A,Z) \rightarrow v + N(A,Z)$
- Coherent: target nucleon wave functions remain in phase with each other before and after the collision. Amplitudes of scattering on individual nucleons add
- Elastic: no new particles are created and nuclear target remains in the same energy state
- The neutrino sees the nucleus as a whole:
 => cross section enhancement σ ~ (#scatter targets)²
 => upper limit on neutrino energy (up to E_v ~ 100 MeV)
- Total cross section scales approximately like N²

$$\frac{d\sigma}{dE_R} \propto N$$

Can be ~2 orders of magnitude larger than inverse beta decay process used first to observe neutrinos.



D. Akimov et al, Science 357 (2017)

INCOHERENT/INELASTIC SCATTERING

Incoherent scattering: $\sigma_{NC}(\nu \mathcal{N}) \propto \sum_{i} |\mathscr{A}(\nu n_{i})|^{2} \propto N$ (Probabilities of scattering on individual nucleons add)

Coherent scattering: $\sigma_{\rm NC}(\nu \mathcal{N}) \propto \left| \sum_{i} \mathscr{A}(\nu n_{i}) \right|^{2} \propto N^{2}$ (Amplitudes of scattering on individual nucleons add)

$$\mathscr{A}(\vec{q}) = \sum_{j=1}^{A} a_j(\vec{q}) \exp^{i\vec{q}x_j}$$

When the momentum transfer times the dimension of the nuclear target is very small, $qR \ll 1$, the phase factors are negligible: the amplitude is given by the single constituent amplitude multiplied by the constituents number A.

Bednyakov and Naumov Phys. Rev. D 98 no. 5, (2018) 053004 Pirinen+ Adv. High Energy Phys. 2018 (2018) 9163586, Bednyakov and Naumov Phys. Part. Nucl. Lett. 16 no. 6, (2019) 638–646

INCOHERENT/INELASTIC SCATTERING



Neutrinos with energies of tens of MeV can excite many states in the target nuclei used for CEvNS experiments.

This cross-section has a linear dependence on the number of nucleons.

Going to higher neutrino energies, an approximation hints towards a smooth transition between the coherent and incoherent neutrino-nucleus scattering regime.

A correct treatment of both channels requires an accurate evaluation of the transition matrix elements describing the various interaction channels between the initial and final nuclear states.

Sahu+ Phys. Rev. C. 102 035501 Bednyakov+ Phys. Rev. D 98 (2018) 053004 Dutta+ Phys. Rev. D 106, 113006 (2022)

. . .



Sahu+ Phys. Rev. C. 102 035501

AN ACT OF HUBRIS

First theoretically predicted in 1974

D.Z. Freedman, Phys. Rev. D 9 (1974) V.B. Kopeliovich and L.L. Frankfurt, JETP Lett. 19 4 236 (1974)

PHYSICAL REVIEW D	VOLUME 9, NUMBER 5	1 MARCH 1974							
Coherent effects of a weak neutral current									
Nation and Institute for Theoretica (Received 15 Oc	Daniel Z. Freedman [†] al Accelerator Laboratory, Batavia, Illinois 6 & Physics, State University of New York, Stor tober 1973: revised manuscript received 19 N	50510 ny Brook, New York 11790 November 1973)							
If there is a weak neutral current, then the elastic scattering process $\nu + A \rightarrow \nu + A$ should have a sharp coherent forward peak just as $e + A \rightarrow e + A$ does. Experiments to observe this peak can give important information on the isospin structure of the neutral current. The experiments are very difficult, although the estimated cross sections (about 10^{-38} cm ² on carbon) are favorable. The coherent cross sections (in contrast to incoherent) are almost energy-independent. Therefore, energies as low as 100 MeV may be suitable. Quasi-									
the weak neutral current. nuclear elastic scattering emission in stellar colla	Because of strong coherent effects at very l g process may be important in inhibiting cooli pse and neutron stars.	ow energies, the ing by neutrino							

Our suggestion may be an act of hubris, because the inevitable constraints of interaction rate, resolution, and background pose grave experimental difficulties for elastic neutrino-nucleus scattering. We will discuss these problems at the end of this note, but first we wish to present the theoretical ideas relevant to the experiments. Experimentally the most conspicuous and most difficult feature of our process is that the only detectable reaction product is a recoil nucleus of low momentum. Ideally the apparatus should have sufficient resolution to identify and determine the momentum of the recoil nucleus and sufficient mass to achieve a reasonable interaction rate. Neutron background is a serious problem

 CE_VNS was observed for the first time ~40 years later, in 2017 by the COHERENT experiment at the Oak Ridge Spallation Neutron Source.

COHERENT ELASTIC NEUTRINO-NUCLEUS SCATTERING

CEvNS is an exceptionally challenging process to observe

Despite its large cross section, not observed for years due to tiny nuclear recoil energies



Credit: R. Strauss @ Magnificent CEvNS



Credit to K. Scholberg @ISAPP 2021





Different types of interactions of a neutrino v_{α} with a nucleus, depending on the wavelength of the mediator.

Adapted from Carlo Giunti



Inelastic incoherent $\lambda_Z \ll 2R$

When $\lambda_Z \ll 2R$ the Z boson has a high probability of interacting with a single nucleon in the nucleus, ejecting it.

 $\lambda_Z = 2\pi \frac{\hbar}{|\overrightarrow{q}|}$



When $\lambda_Z \leq 2R$ the Z boson has a high probability of interacting with a group of nucleons inside the nucleus, exciting the latter to the state N^{*}.

Inelastic incoherent $\lambda_Z \ll 2R$

Elastic incoherent $\lambda_Z \lesssim 2R$

 $\lambda_Z = 2\pi \frac{\hbar}{|\overrightarrow{q}|}$





CEvNS occurs when the neutrino energy E_v is such that amplitudes sum up coherently: $|\vec{q}| \le 1/R_{nucleus}$ (Natural units!)

COHERENT ELASTIC NEUTRINO-NUCLEUS SCATTERING

Heavy target nucleus:

A = 133, M ~ 133 GeV R = $1.2 A^{1/3} \sim 6 \text{ fm}$

CEvNS occurs for $|\vec{q}| \approx 35$ MeV

Non-relativistic nuclear recoil: $|\vec{q}| \sim \sqrt{2ME_R}$



COHERENT ELASTIC NEUTRINO-NUCLEUS SCATTERING

Maximum nuclear recoil is $E_R^{\max} = \frac{2E_{\nu}^2}{m_N}$

Accelerator neutrinos: $E_{\nu} \lesssim 50 \text{ MeV}$ $E_R \lesssim \mathcal{O}(10) \text{ keV}$

Close to decoherence

Reactor neutrinos: $E_{\nu} \lesssim 10 \text{ MeV} \ E_R \lesssim \mathcal{O}(100) \text{ eV}$

Full coherence



Drukier, Stodolsky, PRD 30 (1984) 2295

- No threshold
- Heavier nuclei: higher cross section but lower recoil
- Both cross-section and maximum recoil energy increase with neutrino energy

BONUS SLIDE. WHAT HAPPENS AT EVEN LOWER E_R?

The de Broglie wavelength of particles scales inversely with their momentum: $\lambda_{DB} \sim \frac{1}{p}$. Particles scattering with lower momentum see a larger target and scatter with larger cross sections.

BONUS SLIDE. WHAT HAPPENS AT EVEN LOWER E_R?

If $|\vec{q}| \le 1/R_{atom}$ the reaction occurs with the whole atom. Coherence would be visible for $|\vec{q}| \sim 2 \text{ keV}/R_{atom}$ with a corresponding recoil energy

$$E_R \approx 2 \text{meV}/(AR_{\text{atom}}^2[\text{\AA}])$$

For Helium,
$$R_{\text{atom}} = 0.5 \text{\AA}$$
 and $E_R \sim 2 \text{ meV}$.

Sehgal+ Phys.Lett.B 171 (1986) 107-112 Cadeddu+ Phys. Rev. D 100, 073014 (2019) Donchenko+ FIELDS, PARTICLES, AND NUCLEI 117 (2023)

Electrons "screen" the nuclear weak charge as seen by an electron neutrino (destructive interference).

Observation requires:

- Sensitivity to tiny recoil energies
- neutrinos with energy of few keV

BONUS SLIDE. WHAT HAPPENS AT EVEN LOWER E_R?

Observing relic neutrinos?

Relic neutrinos have momenta p ~ 0.5 meV, corresponding to macroscopic wavelengths λ ~ mm and an enhancement factor of order the Avogadro number.

Opher, Astron. Astrophys. 37 (1974) no.1, 135-137 Lewis, PRD 21 (1980), 663 Shvartsman+, JETP Lett. 36 (1982), 277-279 Smith and Lewin, PLB 127 (1983), 185-190 Duda+ PRD 64 (2001), 122001 Domcke and Spinrath, JCAP 06 (2017), 055 Shergold JCAP 11 (2021), 052

CEVNS EXPERIMENTS AND DETECTION



NEUTRINO SOURCES



NEUTRINO SOURCES

Preferable requisites:

- High flux
- Well understood spectrum
- Multiple flavours
- Possibility of locating the detector close to the source
- Background rejection



Rev.Mod.Phys. 84 (2012) 1307-1341

LOW-ENERGY NEUTRINOS FROM NATURAL SOURCES

Supernova bursts neutrinos



arXiv:1205.6003 [astro-ph.IM]





VDR, Majumdar+ 2309.04117 [hep-ph]



Atmospheric neutrinos



Aristizabal, VDR, Flores, Papoulias JCAP 01 (2022) 01, 055

Solar neutrinos

LOW-ENERGY NEUTRINOS FROM ARTIFICAL SOURCES

Stopped pions (Decay at rest)

High energy, pulsed beam



Reactors

Low energy, but high fluxes possible



Next-generation neutrino beams

Low-energy tail of the neutrino spectrum of LBNF



Aristizabal+ PRD 104, 033004 (2021)

Radioactive source 51Cr



Electron-capture decaying isotope 4 monochromatic lines very short baseline low energy challenging



Beam induced radioactive sources (IsoDAR)

Higher energy than reactors Does not exist yet

Adapted from K. Scholberg @ CNNP2017 and Snowmass 2021 2203.07361

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Aristizabal+ PRD 104, 033004 (2021)

Adapted from K. Scholberg @ CNNP2017 and Snowmass 2021 2203.07361

STOPPED-PION (π -DAR) NEUTRINOS



Credit: M. Green @ Magnificent CEvNS 2019

 $\mu^+ \rightarrow e^+$

 $\pi^+ \to \mu^+ +$



D. Akimov et al. (COHERENT). 2110.07730

STOPPED-PION (π -DAR) NEUTRINOS

- Spallation Neutron Source (SNS) at Oak Ridge National Laboratory (USA).
- Lujan center at Los Alamos Neutron Science Center LANSCE (USA).
- China Spallation Neutron Source CSNS (China).
- European Spallation Source (ESS) under construction (Sweden)



- Pulsed beam → good background rejection
- Neutron backgrounds



D. Akimov et al. (COHERENT). 2110.07730

TIME DISTRIBUTION OF A π -DAR NEUTRINO SOURCE (SNS)



NEUTRINOS FROM NUCLEAR REACTORS

PROs:

- Copious sources of electron antineutrinos
- Low energy (\leq 10 MeV): coherence condition for the recoil is largely preserved

CONs:

- Even smaller recoil energies
- Large backgrounds (although reactor-off allows to measure bckg)
- Only one flavor accessible



Credit: constellationenergy.com



Snowmass 2021 2203.07361

EXPERIMENTS AND DETECTION



LOW-ENERGY NUCLEAR RECOIL DETECTION STRATEGIES



CEVNS EXPERIMENTS WORLDWIDE



Credit to I. Nasteva @NEUTRINO 2024

(INCOMPLETE! LIST OF) CEVNS EXPERIMENTS

Experiment	$T_{\mathbf{th}}$	Baseline (m)	Target	Mass (kg)	Technology	Source	Neutrino flux $(\nu/cm^2/s)$
	$6.5 \ \mathrm{keV_{nr}}$	19.3	CsI[Na]	14.57	Scintillating crystal		$4.3 imes 10^7$
COHERENT	$1.5 \ \mathrm{keV_{ee}}$	22	Ge	10.66	HPGe PPC	π -DAR	
	$20 \ \rm keV_{nr}$	29	LAr	2×10^3	Single phase	5N2	
	$13 \ \mathrm{keV_{nr}}$	28	NaI[Tl]	185*/3388	Scintillating crystal		
CCM	10-20 keV	20-40	LAr	10 ⁴	Scintillation	π -DAR	
						Lujan	
ESS*			CsI, Ge, Xe, Ar			π -DAR	.
CICENNS*	$2 \ {\rm keV_{nr}}$	10.5	CsI(Na)	300	Scintillation	π -DAR	$2 imes 10^7$
NCC-1701 (DRESDEN-II)	$200 \ eV_{ee}$	8	Ge	3	HPGe	NPP 2.9 GW	8.1×10^{13}
CONUS	210 eV_{ee}	17	Ge	4	HPGe	NPP 3.9 GW	$2 imes 10^{13}$
CONUS+	$150 \ eV_{ee}$	20.7	Ge	4	HPGe	NPP 3.6 GW	1.45×10^{13}
MINER	$100 \ eV_{\rm nr}$	1	${\rm Ge/Si/Al_2O_3}$	2-10	cryogenic	NPP 1 MW	1×10^{12}
CONNIE	$15 \mathrm{eV}_{\mathrm{ee}}$	30	Si	$0.5 imes 10^{-3}$	Si CCDs	NPP 3.9 GW	$7.8 imes 10^{12}$
Ricochet	$300 \ eV_{nr}$	8.8	Ge,Zn,Al, Sn	0.68	cryogenic	NPP 58 MW	$1.6 imes 10^{12}$
NUCLEUS	$200~{\rm eV}_{\rm ee}$	77, 102	${ m CaWO_4}$ ${ m Al_2O_3}$	10^{-2}	Cryogenic Ca WO_4 Al ₂ O ₃ calorimeter array	NPP 8.54 GW	1.7×10^{12}
RED100	500 eV	19	Xe	200	LXe dual phase	NPP 3.1 GW	1.35×10^{13}
vGEN	$200 \ eV_{ee}$	11-12	Ge	1.4	HPGe	NPP 3.1 GW	$5.4 imes 10^{13}$
TEXONO	$200 \ eV_{\rm ee}$	28	Ge	1.43	p-PCGe	NPP 2 \times 2.9 GW	$6.4 imes 10^{12}$
NEON	$200 \ eV_{\rm ee}$	23.7	Na(Tl)	16.7	scintillator	NPP 2 \times 2.8 GW	$\sim \times 10^{13}$
SBC*	$100 \ eV_{ee}$		Ar	10		NPP 2 \times 2.9 GW	

WHICH EXPERIMENTS HAVE OBSERVED CEVNS?



1st OBSERVATION OF CEVNS BY COHERENT





Hg TARGET

Observation at 6.7σ confidence level ~130 events observed

COHERENT-Csl[Na] was the world's smallest working neutrino detector!

CENNS-10 Nal Ge ARRAY MARS

D. Akimov et al. (COHERENT) Science 357, 1123–1126 (2017)

COHERENT CSI MEASUREMENT









D. Akimov et al. (COHERENT) Science 357, 1123–1126 (2017) D. Akimov et al. (COHERENT) Phys. Rev. Lett. 129, 081801

COHERENT CSI MEASUREMENT

Full Csl[Na] dataset 2.2 times bigger, before decommissioning in 2019. Updated scintillator response model, improved systematic uncertainties

Reject the no-CEvNS hypothesis at $11.6\ \sigma$ level ~300 events observed



COHERENT LAY MEASUREMENT





24 kg



D. Akimov et al. (COHERENT). Phys. Rev. Lett. 126, 012002 (2021)

COHERENT LAY MEASUREMENT



CENNS-10 Lar single-case (scintillation) detector. Reject the no-CEvNS hypothesis at 3.9 σ level ~150 events observed First confirmation of its N² dependence



D. Akimov et al. (COHERENT). Phys. Rev. Lett. 126, 012002 (2021)

COHERENT-Ge MEASUREMENT





Background-Subtracted On-Beam

R. Bouabid @Magnificent CEvNS 2024

Total

Ge-Mini detector system ~10 kg

Reject the no-CEvNS hypothesis at 3.9 σ level ~20 events observed

Ge, 2024 20 $\bar{\nu}_{\mu}, \nu_{e}$ ν_{μ} counts (keV_{ee})⁻¹ 15fit residuals 10 $\mathbf{5}$ 0 -5-102.55.07.510.0 12.515.017.520.0energy (keVee)

S. Adamski et al. (COHERENT) arXiV: 2406.13806

25

EVIDENCE OF CEVNS ? AT NCC-1701 (DRESDEN-II REACTOR)

Neutrino source: Dresden-II boiling water reactor (USA) 2.96GW \rightarrow 4.8 x10¹³ neutrinos/sec/cm²

Detector: NCC-1701, a 2.924 kg ultra-low noise ptype point contact (PPC) Germanium detector

- low energy threshold (0.2 keV_{ee})
- distance to core: 10.39m
- 96.4-day exposure

CEVNS results: suggestive evidence of CEVNS is reported with strong preference (with respect to the background-only hypothesis)

strongly dependent on quenching factor model



Colaresi, Collar et al. Phys. Rev. Lett. 129 (2022) 211802

EVIDENCE OF CEVNS ? AT NCC-1701 (DRESDEN-II REACTOR)

The quenching factor (QF) describes the observed reduction in ionization yield produced by a nuclear recoil when compared to an electron recoil of same energy

- often not (yet) well known at low recoil energies for $\text{CE}\nu\text{NS}$
- major uncertainty!



J.I. Collar et al, Phys. Rev. D 103, 122003

$$QF = E_{meas}/E_{nuclear reco}$$



Colaresi et al., Phys. Rev. D 104, 072003 (2021) Colaresi et al., 2202.09672 [hep-ex]

CONUS: Direct measurement of ionization quenching factor: k=0.162+-0.004 (compatible with Lindhard) CONUS Phys. Rev. Lett. 126, 041804

XENONNT



XENONnT "measures" the CEvNS signal in Xe from solar 8B neutrinos for the first time.

The background-only hypothesis is disfavored at 2.73σ

From Fei Gao's talk @ IDM 2024



Aprile et al. arXiv:2408.02877v1

PandaX-4T

Cathode +MD Counts/0.5e +8B CEVNS 60 4020 ⁸B CEvNS Data width $[\mu s]$ S MD 1σ ⁸B CEvNS 1σ Number of electron in 4 to 8 e Cathode 1σ Data 50 14 100 10 12 Number of electrons (S2) Counts/ 0.5μ s

The background-only hypothesis is disfavored at 2.64 σ significance

A combined analysis yields a best-fit ⁸B neutrino signal of 3.5 (75) events from the scintillation and ionization (ionization-only) data sample.



Z. Bo et al. (PandaX collaboration) arXiv:2407.10892

LIST OF EXPERIMENTAL PAPERS

- Coherent Elastic Neutrino-Nucleus Scattering Search in the vGeN Experiment, Phys.Part.Nucl.Lett. 21 (2024) 4, 680-682
- 2. First Measurement of SolarB Neutrino Flux through Coherent Elastic Neutrino-Nucleus Scattering in PandaX-4T, Zihao Bo et al. (PandaX), arXiv:2407.10892
- 3. First detection of coherent elastic neutrino-nucleus scattering on germanium, S. Adamski et al. (COHERENT), arXiv:2406.13806
- 4. Final CONUS results on coherent elastic neutrino-nucleus scattering at the Brokdorf reactor, N. Ackermann et al. (CONUS), arXiv:2401.07684
- 5. First results of the nuGeN experiment on coherent elastic neutrino-nucleus scattering, I. Alekseev et al. (nuGeN), Phys.Rev.D 106 (2022) L051101, arXiv:2205.04305.
- 6. Suggestive evidence for Coherent Elastic Neutrino-Nucleus Scattering from reactor antineutrinos, J. Colaresi, J.I. Collar, T.W. Hossbach, C.M. Lewis, K.M. Yocum, Phys.Rev.Lett. 129 (2022) 211802, arXiv:2202.09672
- 7. Search for coherent elastic neutrino-nucleus scattering at a nuclear reactor with CONNIE 2019 data, Alexis Aguilar-Arevalo et al. (CONNIE), JHEP 22 (2020) 017, arXiv:2110.13033
- 8. Measurement of the Coherent Elastic Neutrino-Nucleus Scattering Cross Section on CsI by COHERENT, D. Akimov et al. (COHERENT), Phys.Rev.Lett. 129 (2022) 081801, arXiv:2110.07730
- First results from a search for coherent elastic neutrino-nucleus scattering (CEvNS) at a reactor site, J. Colaresi, J. I. Collar, T. W. Hossbach, A. R. L. Kavner, C. M. Lewis, A. E. Robinson, K. M. Yocum, Phys.Rev.D 104 (2021) 072003, arXiv:2108.02880
- 10. Search for coherent elastic scattering of solar 8B neutrinos in the XENON1T dark matter experiment, E. Aprile et al. (XENON), Phys.Rev.Lett. 126 (2021) 091301, arXiv:2012.02846
- 11. COHERENT Collaboration data release from the first detection of coherent elastic neutrino-nucleus scattering on argon, D. Akimov et al. (COHERENT), arXiv:2006.12659
- 12. First Detection of Coherent Elastic Neutrino-Nucleus Scattering on Argon, D. Akimov et al. (COHERENT), Phys.Rev.Lett. 126 (2021) 012002, arXiv:2003.10630
- 13. First Constraint on Coherent Elastic Neutrino-Nucleus Scattering in Argon, D. Akimov et al. (COHERENT), Phys.Rev. D100 (2019) 115020, arXiv:1909.05913
- 14. COHERENT Collaboration data release from the first observation of coherent elastic neutrino-nucleus scattering, D. Akimov et al. (COHERENT), arXiv:1804.09459
- 15. Observation of Coherent Elastic Neutrino-Nucleus Scattering, D. Akimov et al. (COHERENT), Science 357 (2017) 1123-1126, arXiv:1708.01294

CEVNS CROSS SECTION: STANDARD MODEL



Illustration by Sandbox Studio, Chicago

Interplay of particle, hadronic and nuclear physics

$$\frac{d\sigma_{\nu\mathcal{N}}}{dE_{\mathrm{nr}}}\Big|_{\mathrm{CE}\nu\mathrm{NS}}^{\mathrm{SM}} \propto \left|\sum_{i} c_{i} \, \mathrm{kin}_{i} \, \mathscr{F}_{i}\right|^{2}$$

Kin_i: kinematics terms

C_i: particle physics coefficients (coupling neutrino-quarks)

 \mathcal{F}_i : nuclear structure physics

In the Donnelly-Walecka approach any semi-leptonic nuclear process at low and intermediate energies can be described by an effective interaction Hamiltonian, written in terms of the leptonic and hadronic currents

$$\langle \text{final} | \mathscr{L} | \text{initial} \rangle = \langle \text{final} | \int d^3 \mathbf{x} \, \hat{j}^{\text{lept}}_{\mu}(\mathbf{x}) \, \hat{J}^{\mu}(\mathbf{x}) | \text{initial} \rangle$$

The accurate evaluation of the required transition matrix elements is obtained on the basis of reliable nuclear wave functions.

We follow a multi-step process:

- First, we define the effective neutrino-quark interaction in the non-relativistic limit (small momentum transfer) — same as going from the electroweak theory to the Fermi fourfermion theory
- 2. Second, we need to account for the quark content of the nucleons: we need to take the quark field operators and express them in terms of nucleon ones
- 3. Finally, we need to promote the operators at the nucleon level to the nuclear one. We need a nuclear model.

Freedman Phys. Rev. D 9, 1389-1392 (1974) Drukier, Stodolsky, PRD 30 (1984) 2295 Amanik+ Astropart.Phys. 24 (2005) 160-182 J. Barranco+ JHEP 0512 (2005) 021 Papoulias+ Advances in High Energy Physics, vol. 2015, 763648 Lindner+ JHEP03(2017)097 Hoferichter+ Physical Review D 102, 074018 (2020) Tomalak+ JHEP 2102, 097 (2021) (Radiative corrections) Pandey Prog.Part.Nucl.Phys. (2023) Khaleq+ arXiv:2405.20060

We want to compute the cross-section for the process $\nu_{\ell} \mathcal{N} \to \nu_{\ell} \mathcal{N}$. Elastic process: final state nucleus remains unvaried.

The momentum transfer is much smaller than the mass of the mediator, so we can define an effective Lagrangian for the process.



$$\mathscr{L}_{\text{eff}}^{\text{NC}} = \frac{G_{\text{F}}}{\sqrt{2}} \sum_{q} \left[\bar{\nu} \gamma^{\mu} (g_V^{\nu} - g_A^{\nu} \gamma^5) \nu \right] \left[\bar{q} \gamma_{\mu} (g_V^q - g_A^q \gamma^5) q \right]$$

The Lagrangian is defined as a sum of the interactions at the quark level. The vector and axial couplings at the tree level are:

The term $\bar{q}\gamma^{\mu}\gamma^{5}q$ is the spin-dependent one. It is suppressed compared to the vector current. Only relevant for light nuclei with non-zero spin. Nuclei with even number of protons and neutrons have zero spin, so that axial terms vanish.

Promote the quark operators to the nucleon level. Project the quark current on the initial and final nucleon states:

 $\left| \left\langle \eta(p_f) \left| \mathcal{O}_q \right| \eta(p_i) \right\rangle = \left\langle \eta(p_f) \left| \bar{q} \gamma^{\mu} q \right| \eta(p_i) \right\rangle$

$$= \bar{u}_N \left(\boxed{F_1^{q,\eta}(\mathbf{q}^2)\gamma^{\mu}} + F_2^{q,\eta}(\mathbf{q}^2) \frac{i\sigma^{\mu\nu}q_{\nu}}{2m_{\eta}}\gamma^{\mu} \right) u_N$$

The nucleon matrix element can be parametrized by means of its transformation properties under the Lorentz symmetry, spatial parity and time reversal. F_2 is suppressed (involves spin and goes as q/m_η). At zero momentum transfer, vector currents 'count' the valence quarks in the nucleon.

$$\sum_{\eta=n,p} \sum_{q} \langle g_{V}^{q} \eta(p_{f}) | \bar{q} \gamma^{\mu} q | \eta(p_{i}) \rangle$$

$$= \underbrace{(g_{V}^{u} + 2g_{V}^{d})}_{g_{V}^{p}} \bar{n} \gamma^{\mu} n + \underbrace{(2g_{V}^{u} + g_{V}^{d})}_{g_{V}^{p}} \bar{p} \gamma^{\mu} p$$

Final step: we need to go from interaction with nucleons to interaction with the nucleus. At non-zero momentum transfer there will be a form-factor suppression given by the specific nuclear wave.

Construct the nuclear operator:

$$\langle \mathcal{N}(k_f) \,|\, \bar{\eta} \gamma^{\mu} \eta \,|\, \mathcal{N}(k_i) \rangle = N_{\eta} \,\bar{\mathcal{N}} \gamma^{\mu} \,\mathcal{N} F_{v}^{\eta}(\mathbf{q}^2)$$

Counts nucleons inside nuclei

$$= \left[Z g_{v}^{p} F_{v}^{p}(\mathbf{q}^{2}) + N g_{v}^{n} F_{v}^{n}(\mathbf{q}^{2}) \right] \bar{\mathcal{N}} \gamma^{\mu} \mathcal{N}$$

The weak form factor is defined as

$$\tilde{F}_{\mathrm{w}}(\mathbf{q}^2) = \left[Zg_{\mathrm{v}}^p F_{\mathrm{v}}^p(\mathbf{q}^2) + Ng_{\mathrm{v}}^n F_{\mathrm{v}}^n(\mathbf{q}^2) \right]$$

And then normalized to one through (valid at $q \rightarrow 0$)

$$Q_{\rm W} = (Zg_{\rm v}^p + Ng_{\rm v}^n) = -N/2 + (1/2 - 2\sin^2\theta_{\rm w})Z$$

 $F_{\rm w}(\mathbf{q}^2) = \frac{\tilde{F}_{\rm w}(\mathbf{q}^2)}{O}$

$$\mathscr{L}_{\text{eff}}^{\text{NC}} = \frac{G_{\text{F}}}{\sqrt{2}} \sum_{q} \left[\bar{\nu} \gamma^{\mu} P_{L} \nu \right] \left[Q_{\text{w}} F_{\text{w}}(\mathbf{q}^{2}) \bar{\mathcal{N}} \gamma_{\mu} \mathcal{N} \right]$$

Assume the nucleus is in a fermionic ground state, we can compute the amplitude squared of the process, starting from the matrix element

$$\mathscr{M}^{ss'rr'} = \frac{G_{\rm F}}{\sqrt{2}} Q_{\rm w} F_{\rm w}(\mathbf{q}^2) \left[\bar{u}^{s'}(p') \gamma^{\mu} P_L u^s(p) \right] \left[\bar{u}^{r'}(k') \gamma_{\mu} u^r(k) \right]$$

$$|\mathscr{M}|^{2} = \frac{G_{\rm F}^{2}}{4} Q_{\rm w}^{2} F_{\rm w}^{2}(\mathbf{q}^{2}) L^{\mu\nu} W_{\mu\nu}$$

Lepton Hadron tensor tensor

$$\frac{d\sigma_{\nu\mathcal{N}}}{dE_{\mathrm{nr}}}\Big|_{\mathrm{CE}\nu\mathrm{NS}}^{\mathrm{SM}} = \frac{G_F^2 m_N}{128\pi} \frac{Q_w^2 F_w^2(\mathbf{q}^2)}{E_\nu^2 m_N} L^{\mu\nu} W_{\mu\nu}$$

Performing all traces calculations one obtains

$$\frac{d\sigma_{\nu\mathcal{N}}}{dE_{\rm nr}}\Big|_{\rm CE\nu NS}^{\rm SM} = \frac{G_F^2 m_N}{\pi} F_W^2(\mathbf{q}^2) Q_{\rm w}^2 \left(1 - \frac{m_N E_{\rm nr}}{2E_\nu^2} - \frac{E_{\rm nr}}{E_\nu} + \frac{E_{\rm nr}^2}{2E_\nu^2}\right)$$

$$Q_{\rm W} = -N/2 + (1/2 - 2\sin^2\theta_{\rm w})Z$$

 $\sin^2 \theta_w = 0.23 \rightarrow \text{protons unimportant}$ Neutron contribution dominates

The form factor corrects for scattering that is not completely coherent at higher energies. It encodes information about the nuclear densities through a Fourier transform of the nuclear charge density distribution

$$F_{n,p}(q^2) = \frac{1}{Q_a} \int \rho_{p,n}(\vec{r}) e^{i\vec{q}\cdot\vec{r}} d^3\vec{r}$$

Q_a is the charge of the entire distribution. Assuming a spherically symmetrical distribution:

$$F_{n,p}(q^2) = \frac{4\pi}{Q_a q} \int \rho_{p,n}(r) \sin(q \cdot r) r dr$$

Patton et al, arXiv:1207.0693 Bednyakov, Naumov, arXiv:1806.08768 Papoulias et al, Phys.Lett. B800 (2020) 135133 Ciuffoli et al, arXiv:1801.02166 Canas et al, arXiv:1911.09831 Van Dessel et al, arXiv:2007.03658 Aristizabal-Sierra JHEP 1906:141 (2019) Coloma+ JHEP 08 (2020) 08, 030 Aristizabal-Sierra Phys.Lett.B 845 (2023) 138140

We can expand the form factor in terms of q:

$$F_{n,p}(q^2) \approx \int \rho_{p,n}(r) \left(1 - \frac{q^2}{3!} r^2 + \frac{q^4}{5!} r^4 - \frac{q^6}{7!} r^6 + \dots \right) r^2 dr$$
$$\approx 1 - \frac{q^2}{3!} \langle R_{p,n}^2 \rangle + \frac{q^4}{5!} \langle R_{p,n}^4 \rangle - \frac{q^6}{7!} \langle R_{p,n}^6 \rangle + \dots$$

with the k-th radial moment defined as

Patton et al, arXiv:1207.0693 Papoulias et al, Phys.Lett. B800 (2020) 135133

$$\langle R_{p,n}^k \rangle = \frac{\int \rho_{p,n}(\vec{r}) r^k d^3 \vec{r}}{\int \rho_{p,n}(\vec{r}) d^3 \vec{r}}$$

In this way the form factor is a sum of the even moments of the neutron density distribution, that represent physically relevant and measurable quantities.



From Ryan Bouabid's talk @Magnificent CEvNS2024

How to obtain the nuclear form factors:

- Nuclear structure calculations; S. Kosmas+ Nucl. Phys. A 570 (1994) 637 Papoulias+ Phys.Lett. B800 (2020) 135133
- Use of available experimental data: the proton nuclear form factors are computed by means of a model-independent analysis (using a Fourier-Bessel expansion model or others) of the electron scattering data for the proton charge density; De Vries+ Data and Nucl. Data Tables 36 (1987) 495536
- Use of analytical approximations for the nuclear form factors.



Papoulias+ Phys.Lett. B800 (2020) 135133

FORM FACTORS: PARAMETRIZATIONS

The basic properties of nucleonic distributions can be described by different parametrizations.

J. Engel, Phys.Lett. B 264 (1991) 114

In the Helm model, the nuclear form factor is given by the convolution of two nucleonic densities: a uniform-density one with a cut-off radius R_0 and a second one with a Gaussian profile, in terms of the surface thickness s.

$$F_{\text{Helm}}(q^2) = 3 \frac{j_1(qR_0)}{qR_0} e^{(-qs)^2/2}$$

Helm Phys. Rev. 104 (1956) 1466-1475

 $j_1(x)$ denotes the 1st-order spherical Bessel function.

Th

e root-mean-square (rms) radius
$$\langle R_n^2 \rangle = \frac{3}{5}R_0^2 + 3s^2$$

s = 0.9 from muon spectroscopy data Fricke Nucl.Data Tabl. 60 (1995) 177-285

FORM FACTORS: PARAMETRIZATIONS

The Klein-Nystrand form factor follows from the convolution of short-range Yukawa potential with $a_k = 0.7$ fm, over a distribution approximated as a hard sphere with radius R_a .

$$F_{\rm KN}(q^2) = 3 \frac{j_1(qR_A)}{qR_A} \left[1 + (qa_k)^2\right]^{-1}$$

Klein, Nystrand Phys. Rev. C60 (1999) 014903

 $j_1(x)$ denotes the 1st-order spherical Bessel function.

The root-mean-square (rms) radius

$$\langle R_n^2 \rangle = \frac{3}{5} R_A^2 + 6a_k^2$$

semi-empirical formula $R_A \approx 1.2 \times A^{1/3} {
m fm}$

NUCLEAR RMS RADIUS

The form factor parametrizations depend on two parameters that measure different nuclear properties and that are constrained by means of the rms radius of the distribution:

$$\langle R_{p,n}^2 \rangle = \frac{\int \rho_{p,n}(\vec{r}) r^2 d^3 \vec{r}}{\int \rho_{p,n}(\vec{r}) d^3 \vec{r}}$$

The rms radii of the proton density distributions are determined from different experimental sources: optical and X-ray isotope shifts, muonic spectra, and electronic scattering Angeli+ Atom. Data Nucl. Data Tabl. 99, 69 (2013)

Neutron rms radii: their experimental values follow from hadronic experiments which are subject to large uncertainties.

CEVNS CROSS SECTION: RECAP

CEVNS has a well-calculable cross-section in the SM: (probability of kicking a nucleus with nuclear recoil energy T)



$$Q_{\rm W} = [Z(1 - 4\sin^2\theta_{\rm W}) - N]$$

 $sw^2 = 0.23 \rightarrow protons unimportant$ Neutron contribution dominates

- E_{ν} : is the incident neutrino energy
- M : the nuclear mass of the detector material
- 3-momentum transfer $|\vec{q}|^2 = 2MT$
- $(Q_A \text{ included in } F_A)$

Axial contribution is small for most nuclei, spin-dependent. It vanishes for nuclei with even number of protons and neutrons

Freedman, PRD 9 (1974) 1389; Drukier, Stodolsky, PRD 30 (1984) 2295; Barranco, Miranda, Rashba, hep-ph/0508299