

A tool for distinguishing different neutrinoless double beta mechanisms

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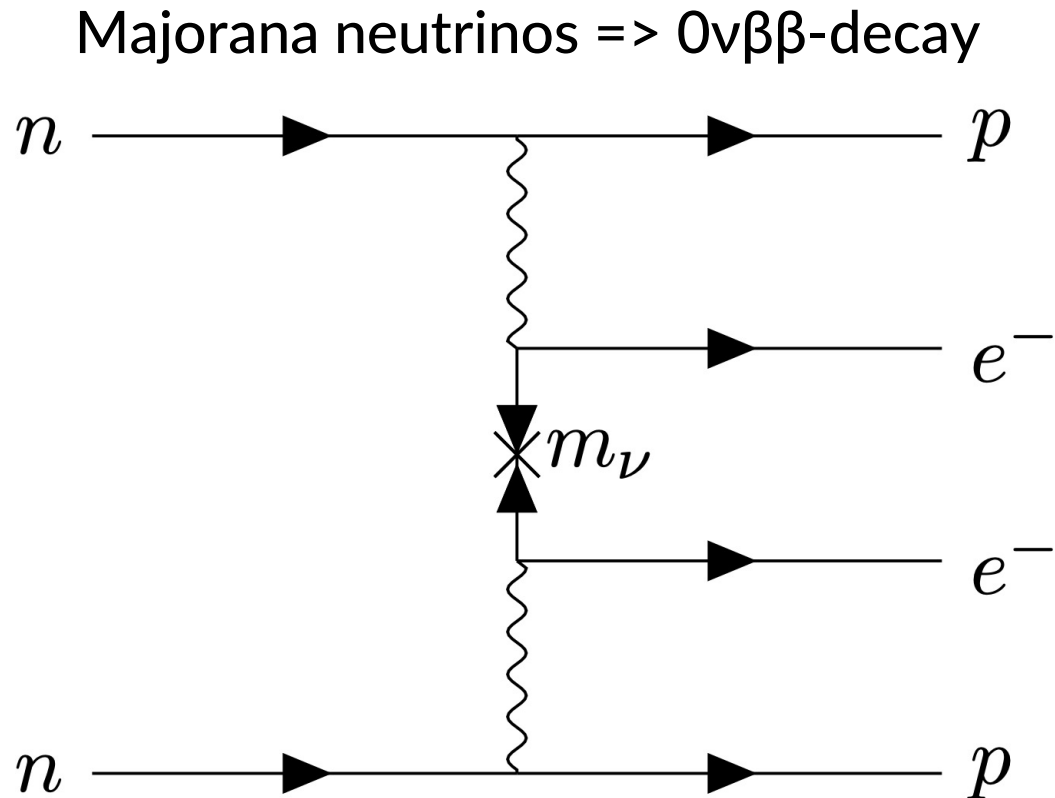
Max Planck Institute for Nuclear Physics, Heidelberg

Overview

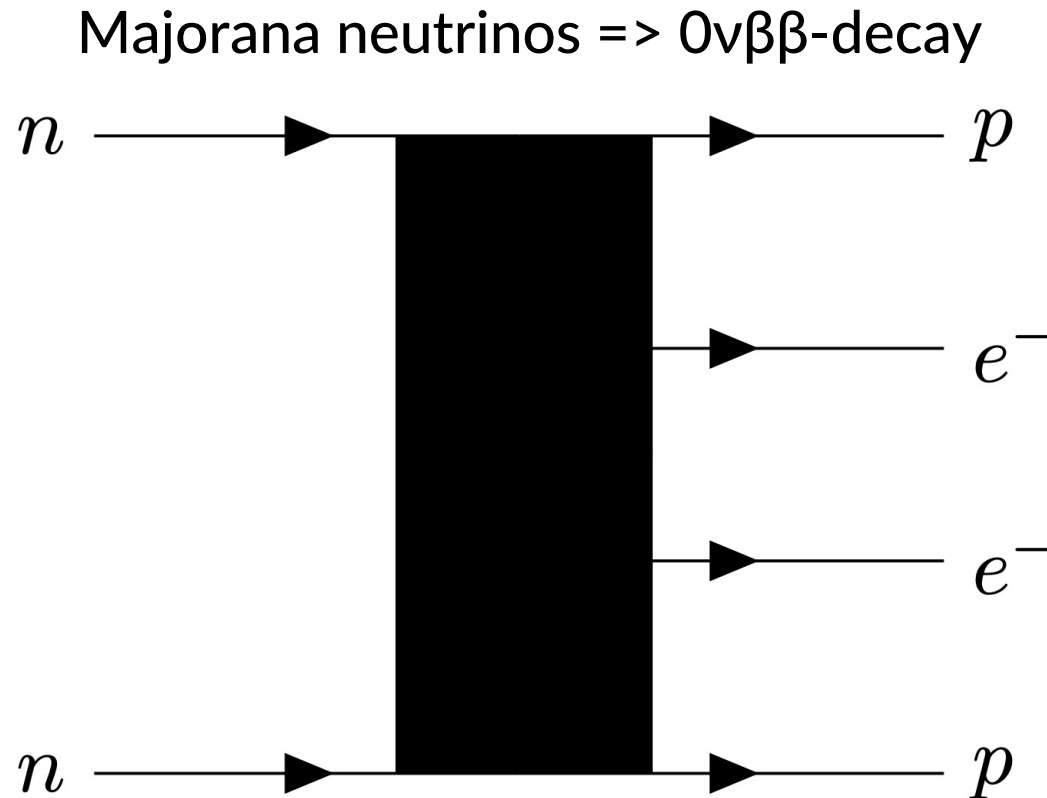
What we will discuss:

- Classification of $0\nu\beta\beta$ mechanisms (standard vs non-standard)
- Brief summary of EFT framework
- Ways to distinguish different mechanisms
- A generalized online tool

$0\nu\beta\beta$ standard mechanism

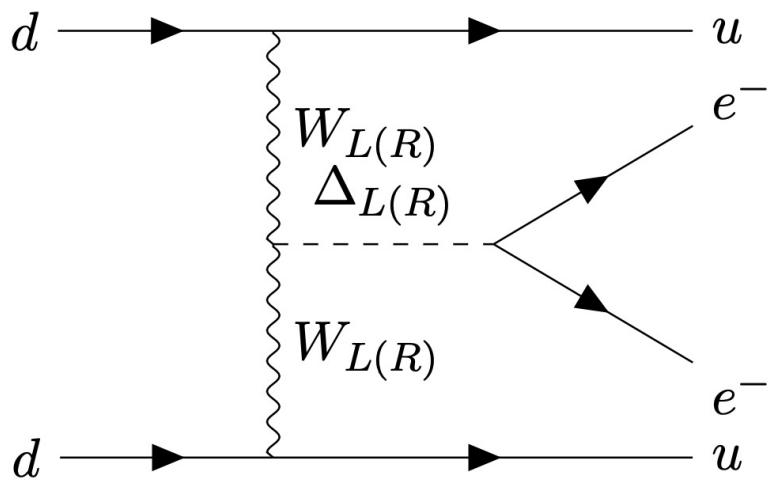


$0\nu\beta\beta$ standard mechanism?

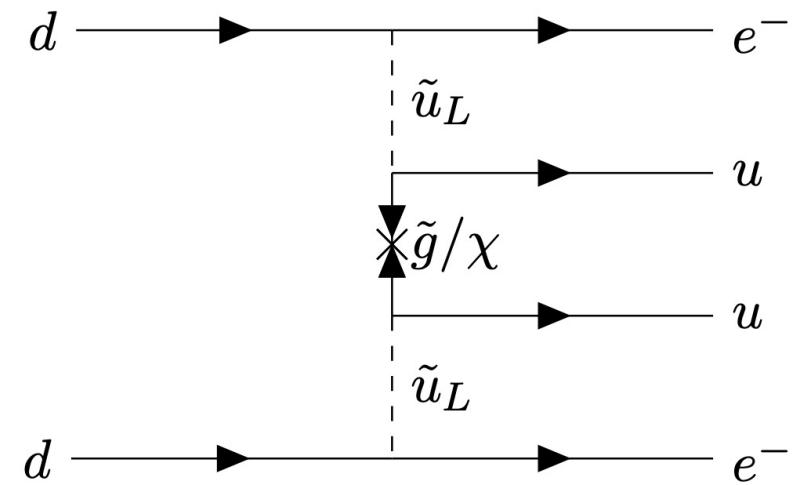


$0\nu\beta\beta$ non-standard mechanisms

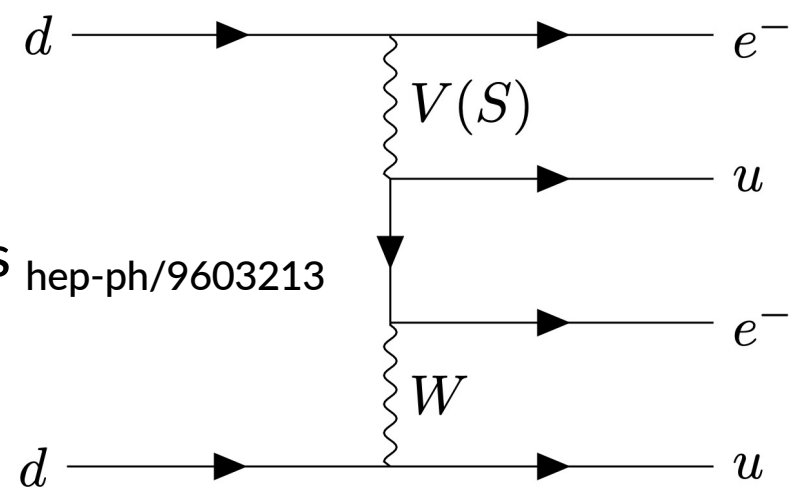
Scalars in minimal LR symmetry



R_p -violating SUSY Phys. Rev. Lett. 75, 17



Leptoquarks hep-ph/9603213



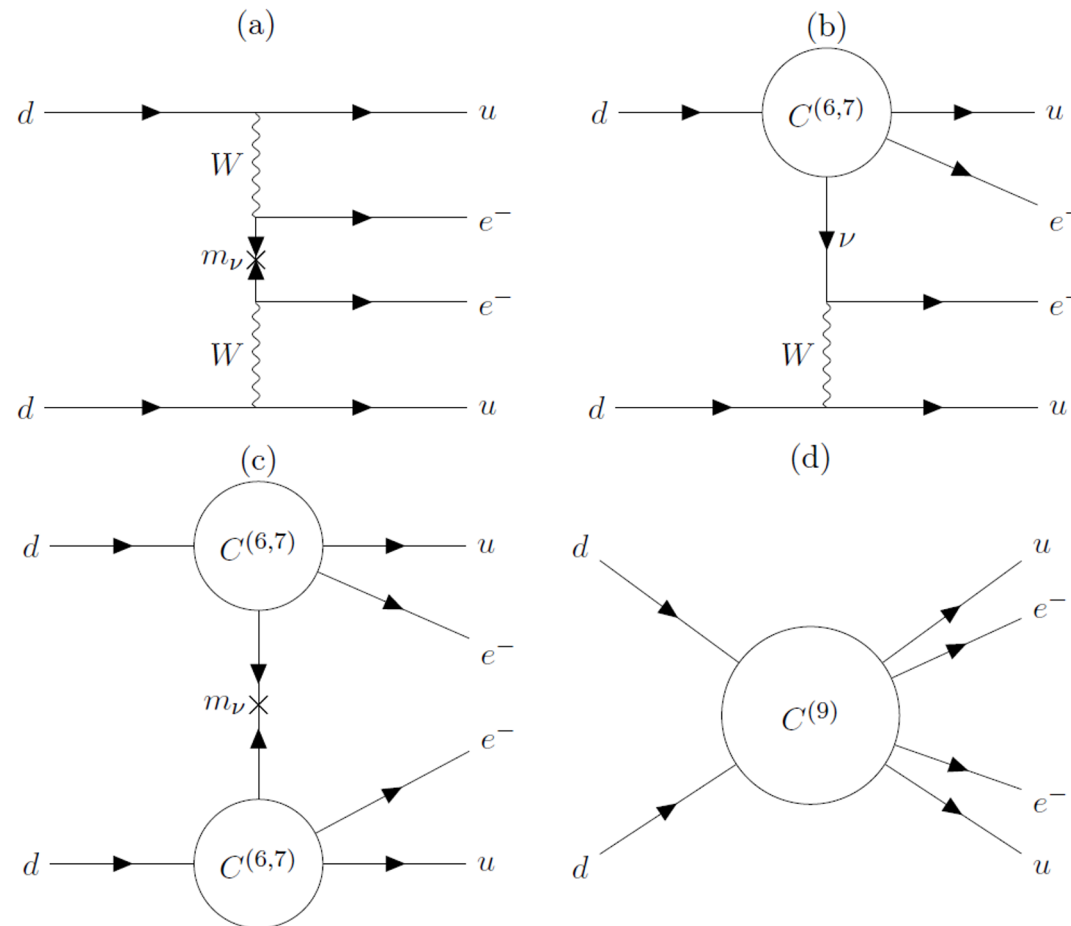
$0\nu\beta\beta$ mechanisms - Classification

a) mass mechanism

b) long-range

c) ignore_(suppressed)

d) short-range



EFT Approach [Cirigliano et al. ArXiv:1806.02780]

Low-Energy decay process
→ use LEFT (no light new physics!)

32 different operators

1 mass mechanism (dim 3)

7 long-range (dim 6,7)

24 short-range (dim 9)

Class	Op. Name	Op. Structure
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Dim 3

Ψ^2	$\mathcal{O}_{m_{\beta\beta}}$	$-\frac{1}{2}m_{ee}\overline{\nu_{L,e}^C}\nu_{L,e}$
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Dim 6

Ψ^4	$\mathcal{O}_{SL}^{(6)}$	$[\overline{u_R}d_L][\overline{e_L}\nu_L^C]$
	$\mathcal{O}_{SR}^{(6)}$	$[\overline{u_L}d_R][\overline{e_L}\nu_L^C]$
	$\mathcal{O}_{VL}^{(6)}$	$[\overline{u_L}\gamma^\mu d_L][\overline{e_R}\gamma_\mu\nu_L^C]$
	$\mathcal{O}_{VR}^{(6)}$	$[\overline{u_R}\gamma^\mu d_R][\overline{e_R}\gamma_\mu\nu_L^C]$
	$\mathcal{O}_T^{(6)}$	$[\overline{u_L}\sigma^{\mu\nu}d_R][\overline{e_L}\sigma_{\mu\nu}\nu_L^C]$

Dim 7

$\Psi^4\partial$	$\mathcal{O}_{VL}^{(7)}$	$[\overline{u_L}\gamma^\mu d_L][\overline{e_L}\overset{\leftrightarrow}{\partial}_\mu\nu_L^C]$
	$\mathcal{O}_{VR}^{(7)}$	$[\overline{u_R}\gamma^\mu d_R][\overline{e_L}\overset{\leftrightarrow}{\partial}_\mu\nu_L^C]$

Dim 9

Ψ^6	$\mathcal{O}_{1L,R}^{(9)}$	$[\overline{u_L}\gamma_\mu d_L][\overline{u_L}\gamma^\mu d_L][\overline{e_L}R e_{L,R}^C]$
	$\mathcal{O}_{1L,R}'^{(9)}$	$[\overline{u_R}\gamma_\mu d_R][\overline{u_R}\gamma^\mu d_R][\overline{e_L}R e_{L,R}^C]$
	$\mathcal{O}_{2L,R}^{(9)}$	$[\overline{u_R}d_L][\overline{u_R}d_L][\overline{e_L}R e_{L,R}^C]$
	$\mathcal{O}_{2L,R}'^{(9)}$	$[\overline{u_L}d_R][\overline{u_L}d_R][\overline{e_L}R e_{L,R}^C]$
	$\mathcal{O}_{3L,R}^{(9)}$	$[\overline{u_R}^\alpha d_L^\beta][\overline{u_R}^\beta d_L^\alpha][\overline{e_L}R e_{L,R}^C]$
	$\mathcal{O}_{3L,R}'^{(9)}$	$[\overline{u_L}^\alpha d_R^\beta][\overline{u_L}^\beta d_R^\alpha][\overline{e_L}R e_{L,R}^C]$
	$\mathcal{O}_{4L,R}^{(9)}$	$[\overline{u_L}\gamma^\mu d_L][\overline{u_R}\gamma_\mu d_R][\overline{e_L}R e_{L,R}^C]$
	$\mathcal{O}_{5L,R}^{(9)}$	$[\overline{u_L}^\alpha\gamma^\mu d_L^\beta][\overline{u_R}^\beta\gamma_\mu d_R^\alpha][\overline{e_L}R e_{L,R}^C]$
	$\mathcal{O}_6^{(9)}$	$[\overline{u_L}\gamma_\mu d_L][\overline{u_L}d_R][\overline{e}\gamma^\mu\gamma_5 e^C]$
	$\mathcal{O}_6'^{(9)}$	$[\overline{u_R}\gamma_\mu d_R][\overline{u_R}d_L][\overline{e}\gamma^\mu\gamma_5 e^C]$
	$\mathcal{O}_7^{(9)}$	$[\overline{u_L}t^A\gamma_\mu d_L][\overline{u_L}t^A d_R][\overline{e}\gamma^\mu\gamma_5 e^C]$
	$\mathcal{O}_7'^{(9)}$	$[\overline{u_R}t^A\gamma_\mu d_R][\overline{u_R}t^A d_L][\overline{e}\gamma^\mu\gamma_5 e^C]$
	$\mathcal{O}_8^{(9)}$	$[\overline{u_L}\gamma_\mu d_L][\overline{u_R}d_L][\overline{e}\gamma^\mu\gamma_5 e^C]$
	$\mathcal{O}_8'^{(9)}$	$[\overline{u_R}\gamma_\mu d_R][\overline{u_L}d_R][\overline{e}\gamma^\mu\gamma_5 e^C]$
	$\mathcal{O}_9^{(9)}$	$[\overline{u_L}t^A\gamma_\mu d_L][\overline{u_R}t^A d_L][\overline{e}\gamma^\mu\gamma_5 e^C]$
	$\mathcal{O}_9'^{(9)}$	$[\overline{u_R}t^A\gamma_\mu d_R][\overline{u_L}t^A d_R][\overline{e}\gamma^\mu\gamma_5 e^C]$

EFT Approach [Cirigliano et al. ArXiv:1806.02780]

Standard Formula

$$\left(T_{1/2}^{0\nu}\right)^{-1} = |m_{\beta\beta}|^2 |M^{0\nu}|^2 G^{0\nu}(Q, Z)$$



0νββ “Master-Formula”

$$\begin{aligned} \left(T_{1/2}^{0\nu}\right)^{-1} = & g_A^4 \left[G_{01} \left(|\mathcal{A}_\nu|^2 + |\mathcal{A}_R|^2 \right) - 2(G_{01} - G_{04}) \operatorname{Re} [\mathcal{A}_\nu^* \mathcal{A}_R] \right. \\ & + 4G_{02} |\mathcal{A}_E|^2 + 2G_{04} \left(|\mathcal{A}_{m_e}|^2 + \operatorname{Re} [\mathcal{A}_{m_e}^* (\mathcal{A}_\nu + \mathcal{A}_R)] \right) \\ & - 2G_{03} \operatorname{Re} [(\mathcal{A}_\nu + \mathcal{A}_R) \mathcal{A}_E^* + 2\mathcal{A}_{m_e} \mathcal{A}_E^*] \\ & \left. + G_{09} |\mathcal{A}_M|^2 + G_{06} \operatorname{Re} [(\mathcal{A}_\nu - \mathcal{A}_R) \mathcal{A}_M^*] \right] \end{aligned}$$

Input: Wilson Coefficients + 3 numerical inputs (NMEs, PSFs, LECs)

EFT Approach [Cirigliano et al. ArXiv:1806.02780]

Standard Formula

$$\left(T_{1/2}^{0\nu}\right)^{-1} = |m_{\beta\beta}|^2 |M^{0\nu}|^2 G^{0\nu}(Q, Z)$$



0νββ "Formula"

$$\begin{aligned} \left(T_{1/2}^{0\nu}\right)^{-1} &= \frac{m_{\beta\beta}}{m_e} \mathcal{M}_\nu^{(3)} + \frac{m_N}{m_e} \mathcal{M}_\nu^{(2)} - 2(G_{01} - G_{04}) \text{Re}[\mathcal{A}_\nu^* \mathcal{A}_R] \\ &+ \frac{m_N^2}{m_e v} \mathcal{M}_\nu^{(9)} \left(C_{SL}^{(6)}, C_{SR}^{(6)}, C_T^{(6)}, C_{VL}^{(7)}, C_{VR}^{(7)} \right) \\ &- 2G_{03} \text{Re}[\mathcal{A}_\nu] \left(C_{1L}^{(9)}, C_{1L}'^{(9)}, C_{2L}^{(9)}, C_{2L}'^{(9)}, C_{3L}^{(9)}, C_{3L}'^{(9)}, C_{4L}^{(9)}, C_{5L}^{(9)} \right) \\ &+ G_{09} |\mathcal{A}_M|^2 + G_{06} \text{Re}[(\mathcal{A}_\nu + \mathcal{A}_R)] \end{aligned}$$

Input: Wilson Coefficients + 3 numerical inputs (NMNS, LECs)

EFT Approach [Cirigliano et al. ArXiv:1806.02780]

Standard Formula

$$\left(T_{1/2}^{0\nu}\right)^{-1} = |m_{\beta\beta}|^2 |M^{0\nu}|^2 G^{0\nu}(Q, Z)$$



$0\nu\beta\beta$ "Formula"

$$\left(T_{1/2}^{0\nu}\right)^{-1} = \frac{m_{\beta\beta}}{m_e} \mathcal{M}_\nu^{(3)}$$

Input

$$\mathcal{A}_R = \frac{m_N^2}{m_e v} \mathcal{M}_R^{(9)} \left(C_{1R}^{(9)}, C_{1R}^{(9)'} , C_{2R}^{(9)}, C_{2R}^{(9)'} , C_{3R}^{(9)}, C_{3R}^{(9)'} , C_{4R}^{(9)}, C_{5R}^{(9)} \right),$$

$$\mathcal{A}_E = \mathcal{M}_{E,L}^{(6)} \left(C_{VL}^{(6)} \right) + \mathcal{M}_{E,R}^{(6)} \left(C_{VR}^{(6)} \right),$$

$$\mathcal{A}_{me} = \mathcal{M}_{me,L}^{(6)} \left(C_{VL}^{(6)} \right) + \mathcal{M}_{me,R}^{(6)} \left(C_{VR}^{(6)} \right),$$

$$\mathcal{A}_M = \frac{m_N}{m_e} \mathcal{M}_M^{(6)} \left(C_{VL}^{(6)} \right) + \frac{m_N^2}{m_e v} \mathcal{M}_M^{(9)} \left(C_6^{(9)}, C_6^{(9)'} , C_7^{(9)}, C_7^{(9)'} , C_8^{(9)}, C_8^{(9)'} , C_9^{(9)}, C_9^{(9)'} \right),$$

Coefficients + 3 numerical inputs (NMEs, C_{3L}, C_{4L}, C_{5L}), LECs)

EFT Approach [Cirigliano et al. ArXiv:1806.02780]

Standard Formula

$$\left(T_{1/2}^{0\nu}\right)^{-1} = |m_{\beta\beta}|^2 |M^{0\nu}|^2 G^{0\nu}(Q, Z)$$

$0\nu\beta\beta$ "N"

$$A_\nu = \frac{m_{\beta\beta}}{m_e} \mathcal{M}_\nu^{(3)}$$

$$\mathcal{M}_\nu^{(3)} = -V_{ud}^2 \left(-\frac{1}{g_A^2} M_F + \mathcal{M}_{GT} + \mathcal{M}_T + 2 \frac{m_\pi^2 g_{NN}^{\text{NN}}}{g_A^2} M_{F,sd} \right),$$

$\left(T_{1/2}^{0\nu}\right)^{-1}$

$$\mathcal{M}_\nu^{(6)} = V_{ud} \left(\frac{B}{m_N} (C_{SL}^{(6)} - C_{SR}^{(6)}) + \frac{m_\pi^2}{m_N v} (C_{VL}^{(7)} - C_{VR}^{(7)}) \right) \mathcal{M}_{PS} + V_{ud} C_T^{(6)} \mathcal{M}_{T6},$$

$$\mathcal{M}_\nu^{(9)} = -\frac{1}{2m_N^2} C_{\pi\pi L}^{(9)} (M_{GT,sd}^{AP} + M_{T,sd}^{AP}) - \frac{2m_\pi^2}{g_A^2 m_N^2} C_{NNL}^{(9)} M_{F,sd},$$

Input

$$A_M = \frac{m_N}{m_e} \mathcal{M}_M^{(6)} (C_{VL}^{(6)}) + \frac{m_N^2}{m_e v} \mathcal{M}_M^{(9)} (C_6^{(9)}, C_6^{(9)'}, C_7^{(9)}, C_{3L}^{(9)'}, C_{4L}^{(9)}, C_{5L}^{(9)}), \text{ LECs}$$

EFT Approach [Cirigliano et al. ArXiv:1806.02780]

Standard Formula

$$\left(T_{1/2}^{0\nu}\right)^{-1} = |m_{\beta\beta}|^2 |M^{0\nu}|^2 G^{0\nu}(Q, Z)$$

0νββ “N”

$$A_\nu = \frac{m_{\beta\beta}}{m_e} \mathcal{M}_\nu^{(3)}$$

$$\mathcal{M}_\nu^{(3)} = -V_{ud}^2 \left(-\frac{1}{g_A^2} M_F + \mathcal{M}_{E,R}^{(6)} \right)$$

$\left(T_{1/2}^{0\nu}\right)^{-1}$

$$\mathcal{M}_\nu^{(6)} = V_{ud} \left(\frac{B}{m_N} \left(C_{E,L}^{(6)} \mathcal{M}_{E,L}^{(6)} - C_{E,R}^{(6)} \mathcal{M}_{E,R}^{(6)} \right) \right)$$

$$\mathcal{M}_{E,L}^{(6)} = -\frac{V_{ud} C_{VL}^{(6)}}{3} \left(\frac{g_V^2}{g_A^2} M_F + \frac{1}{3} (2M_{GT}^{AA} + M_T^{AA}) + \frac{6g_V^E L}{g_A^2} M_{F,sd} \right)$$

$$\mathcal{M}_{E,R}^{(6)} = -\frac{V_{ud} C_{VR}^{(6)}}{3} \left(\frac{g_V^2}{g_A^2} M_F - \frac{1}{3} (2M_{GT}^{AA} + M_T^{AA}) + \frac{6g_V^E L}{g_A^2} M_{F,sd} \right)$$

$$\mathcal{M}_\nu^{(9)} = -\frac{1}{2m_N^2} C_{\pi\pi L}^{(9)} \left(M_{E,R}^{(6)} - C_{VR}^{(7)} \right) \mathcal{M}_{PS} + V_{ud} C_T^{(6)} \mathcal{M}_{T6}$$

$$A_R = \frac{m_N^2}{m_e v} \mathcal{M}_R^{(9)} \left(C_{\pi\pi L}^{(9)} \mathcal{M}_{E,R}^{(6)} - C_{VR}^{(7)} \right)$$

A_E

$$A_E = \mathcal{M}_{E,L}^{(6)} \left(C_{VL}^{(6)} \right) + \mathcal{M}_{E,R}^{(6)} \left(C_{VR}^{(6)} \right)$$

$$A_{me} = \mathcal{M}_{me,L}^{(6)} \left(C_{VL}^{(6)} \right) + \mathcal{M}_{me,R}^{(6)} \left(C_{VR}^{(6)} \right)$$

Input

$$A_M = \frac{m_N}{m_e} \mathcal{M}_M^{(6)} \left(C_{VL}^{(6)} \right) + \frac{m_N^2}{m_e v} \mathcal{M}_M^{(9)} \left(C_6^{(9)}, C_6^{(9)'} \right)$$

$$C_6^{(9)}, C_6^{(9)'}, C_7^{(9)}, C_{3L}^{(9)}, C_{4L}^{(9)}, C_{5L}^{(9)}$$

coefficients + 3 numerical inputs (NMEs,

LECs)

EFT Approach [Cirigliano et al. ArXiv:1806.02780]

Standard Formula

$$(T_{1/2}^{0\nu})^{-1} = |m_{\beta\beta}|^2 |M^{0\nu}|^2 G^{0\nu}(Q, Z)$$

$0\nu\beta\beta$ "N"

$$(T_{1/2}^{0\nu})^{-1}$$

$$\mathcal{A}_\nu = \frac{m_{\beta\beta}}{m_e} \mathcal{M}_\nu^{(6)}$$

$$\mathcal{M}_\nu^{(3)} = -V_{ud}^2 \left(-\frac{1}{g_A^2} M_F + \mathcal{M}_\nu^{(6)} \right)$$

$$\mathcal{M}_\nu^{(6)} = V_{ud} \left(\frac{B}{m_N} \left(C_{E,L} \mathcal{M}_{E,L}^{(6)} = -\frac{V_{ud} C_{VL}^{(6)}}{3} \left(\frac{g_V^2}{g_A^2} M_F + \frac{1}{3} (2M_{GT}^{AA} + M_T^{AA}) + \frac{6g_{VL}^E}{g_A^2} M_{F,sd} \right) \right) \right.$$

$$\left. C_{E,R} \mathcal{M}_{E,R}^{(6)} = -\frac{V_{ud} C_{VR}^{(6)}}{3} \left(\frac{g_V^2}{g_A^2} M_F - \frac{1}{3} (2M_{GT}^{AA} + M_T^{AA}) + \frac{6g_{VL}^E}{g_A^2} M_{F,sd} \right) \right)$$

$$A_R = \frac{m_N^2}{m_e v} \mathcal{M}_R^{(9)} \left(C_{E,R} \mathcal{M}_{E,R}^{(9)} \right)$$

$$A_E = \mathcal{M}_{E,L}^{(6)} \left(C_{VL}^{(6)} \right) +$$

$$A_{me} = \mathcal{M}_{me,L}^{(6)} \left(C_{VL}^{(6)} \right)$$

Input

$$A_M = \frac{m_N}{m_e} \mathcal{M}_M^{(6)} \left(C_{E,L} \mathcal{M}_{E,L}^{(6)} \right)$$

$$\mathcal{M}_{me,L}^{(6)} = \frac{V_{ud} C_{VL}^{(6)}}{6} \left(\frac{g_V^2}{g_A^2} M_F - \frac{1}{3} (M_{GT}^{AA} - 4M_T^{AA}) - 3 (M_{GT}^{AP} + M_{GT}^{PP} + M_T^{AP} + M_T^{PP}) \right) \mathcal{M}_{T6},$$

$$- \frac{12g_{VL}^{me}}{g_A^2} M_{F,sd} \Big),$$

$$\mathcal{M}_{me,R}^{(6)} = \frac{V_{ud} C_{VR}^{(6)}}{6} \left(\frac{g_V^2}{g_A^2} M_F + \frac{1}{3} (M_{GT}^{AA} - 4M_T^{AA}) + 3 (M_{GT}^{AP} + M_{GT}^{PP} + M_T^{AP} + M_T^{PP}) \right)$$

$$- \frac{12g_{VL}^{me}}{g_A^2} M_{F,sd} \Big),$$

EFT Approach [Cirigliano et al. ArXiv:1806.02780]

Standard Formula

$$\left(T_{1/2}^{0\nu}\right)^{-1} = |m_{\beta\beta}|^2 |M^{0\nu}|^2 G^{0\nu}(Q, Z)$$

$0\nu\beta\beta$ "N"

$$\mathcal{A}_\nu = \frac{m_\nu}{m_e}$$

$$\mathcal{M}_M^{(6)} = V_{ud} C_{VL}^{(6)} \left[2 \frac{g_A}{g_M} (M_{GT}^{MM} + M_T^{MM}) + \frac{m_\pi^2}{m_N^2} \left(-\frac{2}{g_A^2} g_{VL}^{NN} M_{F,sd} + \frac{1}{2} g_{VL}^{\pi N} (M_{GT,sd}^{AP} + M_{T,sd}^{AP}) \right) \right],$$

$\left(T_{1/2}^{0\nu}\right)^{-1}$

$$\mathcal{M}_M^{(9)} = \frac{m_\pi^2}{m_N^2} \left[-\frac{2}{g_A^2} (g_6^{NN} C_V^{(9)} + g_7^{NN} \tilde{C}_V^{(9)}) M_{F,sd} + \frac{1}{2} (g_V^{\pi N} C_V^{(9)} + \tilde{g}_V^{\pi N} \tilde{C}_V^{(9)}) (M_{GT,sd}^{AP} + M_{T,sd}^{AP}) \right].$$

$$\mathcal{A}_R = \frac{m_N^2}{m_e v} \mathcal{M}_R^{(9)} \left(C_{VL}^{(9)} - C_{VR}^{(9)} \right)$$

$$\mathcal{M}_{me,R}^{(6)} = -\frac{V_{ud} C_{VR}^{(6)}}{3} \left(\frac{g_V^2}{g_A^2} M_F - \frac{1}{3} (2M_{GT}^{AA} + M_T^{AA}) + \frac{6g_{VL}^E}{g_A^2} M_{F,sd} \right),$$

$$\mathcal{M}_{T6},$$

$$\mathcal{A}_E = \mathcal{M}_{E,L}^{(6)} \left(C_{VL}^{(6)} \right)$$

$$\mathcal{A}_{me} = \mathcal{M}_{me,L}^{(6)} \left(C_{VL}^{(6)} \right)$$

Input

$$\mathcal{A}_M = \frac{m_N}{m_e} \mathcal{M}_M^{(6)} \left(C_{VL}^{(6)} \right)$$

$$\mathcal{M}_{me,R}^{(6)} = \frac{V_{ud} C_{VR}^{(6)}}{6} \left(\frac{g_V^2}{g_A^2} M_F + \frac{1}{3} (M_{GT}^{AA} - 4M_T^{AA}) + 3 (M_{GT}^{AP} + M_{GT}^{PP} + M_T^{AP} + M_T^{PP}) - \frac{12g_{VL}^{me}}{g_A^2} M_{F,sd} \right),$$

EFT Approach [Cirigliano et al. ArXiv:1806.02780]

Formula

$$\mathcal{M}_{GT} = M_{GT}^{AA} + M_{GT}^{AP} + M_{GT}^{PP} + M_{GT}^{MM},$$

$$\mathcal{M}_T = M_T^{AP} + M_T^{PP} + M_T^{MM},$$

$$\mathcal{M}_{PS} = \frac{1}{2} M_{GT}^{AP} + M_{GT}^{PP} + \frac{1}{2} M_T^{AP} + M_T^{PP},$$

$$\mathcal{M}_{T6} = 2 \frac{g'_T - g_T^{NN}}{g_A^2} \frac{m_\pi^2}{m_N^2} M_{F,sd} - \frac{8g_T}{g_M} (M_{GT}^{MM} + M_T^{MM})$$

$$+ g_T^{\pi N} \frac{m_\pi^2}{4m_N^2} (M_{GT,sd}^{AP} + M_{T,sd}^{AP}) + g_T^{\pi\pi} \frac{m_\pi^2}{4m_N^2} (M_{GT,sd}^{PP} + M_{T,sd}^{PP})$$

$$+ M_{T,sd}^{AP} + M_{T,sd}^{AP} \Big],$$

$$+ M_{T,sd}^{AP} \Big],$$

$$M_F - \frac{1}{3} (2M_{GT}^{AA} + M_T^{AA}) + \frac{6g_{V L}^E}{g_A^2} M_{F,sd},$$

$$- \frac{1}{6} \left(\frac{g_V^2}{g_A^2} M_F - \frac{1}{3} (M_{GT}^{AA} - 4M_T^{AA}) - 3 (M_{GT}^{AP} + M_{GT}^{PP} + M_T^{AP} + M_T^{PP}) \right) \mathcal{M}_{T6},$$

$$- \frac{12g_{V L}^{me}}{g_A^2} M_{F,sd},$$

$$\mathcal{M}_{me,R}^{(6)} = \frac{V_{ud} C_{VR}^{(6)}}{6} \left(\frac{g_V^2}{g_A^2} M_F + \frac{1}{3} (M_{GT}^{AA} - 4M_T^{AA}) + 3 (M_{GT}^{AP} + M_{GT}^{PP} + M_T^{AP} + M_T^{PP}) \right. \\ \left. - \frac{12g_{V L}^{me}}{g_A^2} M_{F,sd} \right),$$

$$A_R = \frac{m_N^2}{m_e v} \mathcal{M}_R^{(9)} (C_{V L}^{(9)})$$

$$A_E = \mathcal{M}_{E,L}^{(6)} (C_{V L}^{(6)})$$

$$A_{me} = \mathcal{M}_{me,L}^{(6)} (C_{V L}^{(6)})$$

Input

$$A_M = \frac{m_N}{m_e} \mathcal{M}_M^{(6)} (C_{V L}^{(6)})$$

EFT Approach [Cirigliano et al. ArXiv:1806.02780]

Formula

$$\begin{aligned}
 \mathcal{M}_{GT} &= M_{GT}^{AA} + M_{GT}^{AP} + M_{GT}^{PP} \\
 \mathcal{M}_T &= M_T^{AP} + M_T^{PP} \\
 \mathcal{M}_{PS} &= \frac{1}{2} M_{AP} \\
 C_V^{(9)} &= C_6^{(9)} + C_6^{(9)'} + C_8^{(9)} + C_8^{(9)'}, \quad \tilde{C}_V^{(9)} = C_7^{(9)} + C_7^{(9)'} + C_9^{(9)} + C_9^{(9)'} \\
 C_{\pi\pi L}^{(9)} &= g_2^{\pi\pi} (C_{2L}^{(9)} + C_{2L}^{(9)'}) + g_3^{\pi\pi} (C_{3L}^{(9)} + C_{3L}^{(9)'}) - g_4^{\pi\pi} C_{4L}^{(9)} - g_5^{\pi\pi} C_{5L}^{(9)} - \frac{5}{3} g_1^{\pi\pi} m_\pi^2 (C_{1L}^{(9)} + C_{1L}^{(9)'}) \\
 C_{\pi NL}^{(9)} &= \left(g_1^{\pi N} - \frac{5}{6} g_1^{\pi\pi} \right) (C_{1L}^{(9)} + C_{1L}^{(9)'}) + g_2^{NN} (C_{2L}^{(9)} + C_{2L}^{(9)'}) + g_3^{NN} (C_{3L}^{(9)} + C_{3L}^{(9)'}) + g_4^{NN} C_{4L}^{(9)} + g_5^{NN} C_{5L}^{(9)} \\
 C_{NNL}^{(9)} &= g_1^{NN} (C_{1L}^{(9)} + C_{1L}^{(9)'}) + g_2^{NN} (C_{2L}^{(9)} + C_{2L}^{(9)'}) + g_3^{NN} (C_{3L}^{(9)} + C_{3L}^{(9)'}) + g_4^{NN} C_{4L}^{(9)} + g_5^{NN} C_{5L}^{(9)} \\
 A_R C_{\{\pi\pi, \pi N, NN\}R} &= C_{\{\pi\pi, \pi N, NN\}L|L \rightarrow R} \cdot \left[4m_N^2 (M_{GT, sd}^{PP} + M_{T, sd}^{PP}) + M_{T, sd}^{AA} \right] \\
 A_E &= \mathcal{M}_{E,L}^{(6)} (C_{VL}^{(6)}) \\
 A_{me} &= \mathcal{M}_{me,L}^{(6)} (C_{VL}^{(6)}) \\
 A_M &= \frac{m_N}{m_e} \mathcal{M}_M^{(6)} (C_{VL}^{(6)}) \\
 \mathcal{M}_{me,R}^{(6)} &= \frac{V_{ud} C_{VR}^{(6)}}{6} \left(\frac{g_V^2}{g_A^2} M_F + \frac{1}{3} (M_{GT}^{AA} - 4M_T^{AA}) + 3 (M_{GT}^{AP} + M_{GT}^{PP} + M_T^{AP} + M_T^{PP}) \right. \\
 &\quad \left. - \frac{12g_{VL}^{me}}{g_A^2} M_{F, sd} \right), \\
 \mathcal{M}_{T6} &= \left(M_F - \frac{1}{3} (2M_{GT}^{AA} + M_T^{AA}) + \frac{6g_{VL}^E}{g_A^2} M_{F, sd} \right) \\
 &\quad - \frac{1}{6} \left(\frac{g_V^2}{g_A^2} M_F - \frac{1}{3} (M_{GT}^{AA} - 4M_T^{AA}) - 3 (M_{GT}^{AP} + M_{GT}^{PP} + M_T^{AP} + M_T^{PP}) \right) \\
 &\quad - \frac{12g_{VL}^{me}}{g_A^2} M_{F, sd}
 \end{aligned}$$

How to distinguish?

Standard or non-standard mechanism?

3 different observables in decay experiments

1) Half-Life

2) Single Electron Spectra

3) Angular Correlation

1) Half-Life → Ratios

NMEs depend on (A,Z)

Study Ratios of Half-Lives [see Deppisch and Päs arXiv:hep-ph/0612165]

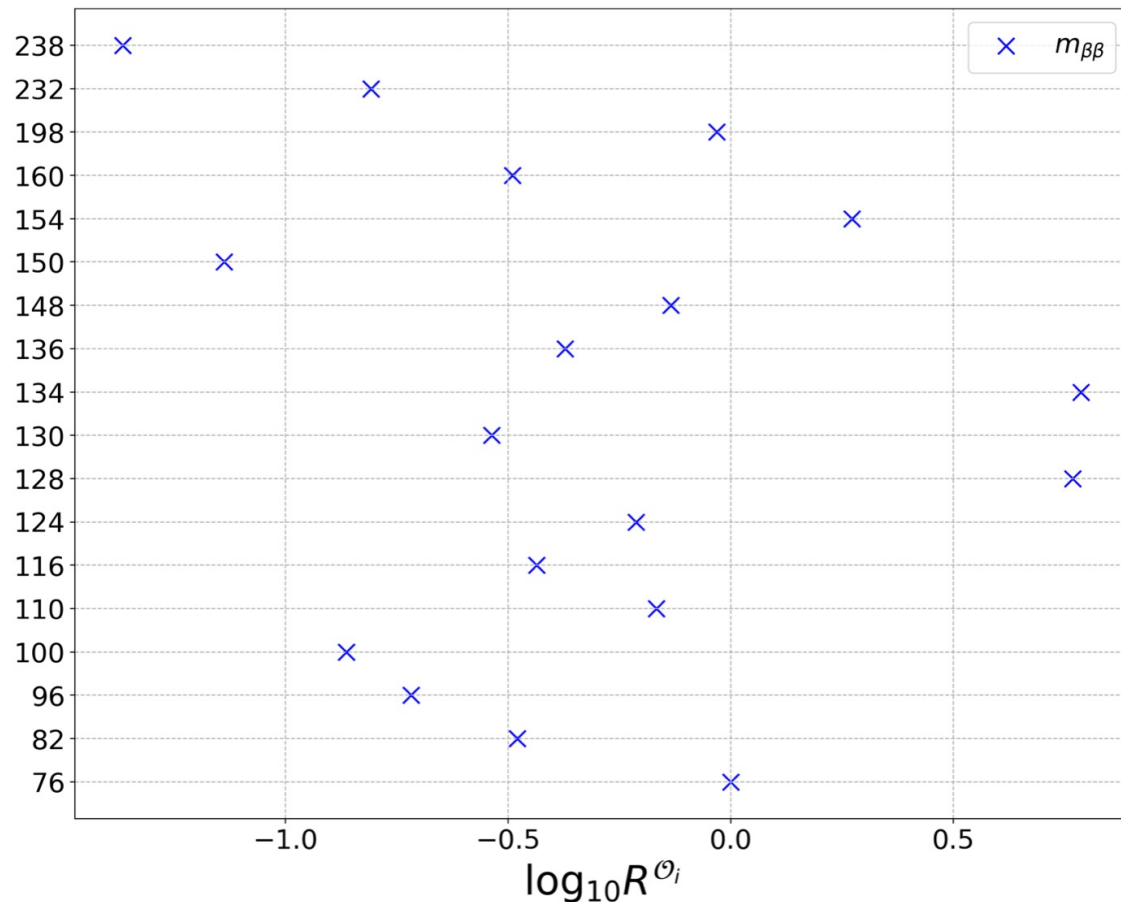
$$R^{\mathcal{O}_i}(AX) \equiv \frac{T_{1/2}^{\mathcal{O}_i}(AX)}{T_{1/2}^{\mathcal{O}_i}(^{76}\text{Ge})} = \frac{|\mathcal{M}^{\mathcal{O}_i}(^{76}\text{Ge})|^2 G^{\mathcal{O}_i}(^{76}\text{Ge})}{|\mathcal{M}^{\mathcal{O}_i}(AX)|^2 G^{\mathcal{O}_i}(AX)}$$

1) Half-Life → Ratios

NMEs depend on (A,Z)

Study Ratios of Half-Lives [see Deppisch and Päs arXiv:hep-ph/0612165]

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1) Half-Life → Ratios

NMEs depend on (A,Z)

Study Ratios of Half-Lives [see Deppisch and Päs arXiv:hep-ph/0612165]

$$R^{\mathcal{O}_i}(^A X) \equiv \frac{T_{1/2}^{\mathcal{O}_i}(^A X)}{T_{1/2}^{\mathcal{O}_i}(^{76}\text{Ge})} = \frac{|\mathcal{M}^{\mathcal{O}_i}(^{76}\text{Ge})|^2 G^{\mathcal{O}_i}(^{76}\text{Ge})}{|\mathcal{M}^{\mathcal{O}_i}(^A X)|^2 G^{\mathcal{O}_i}(^A X)}$$

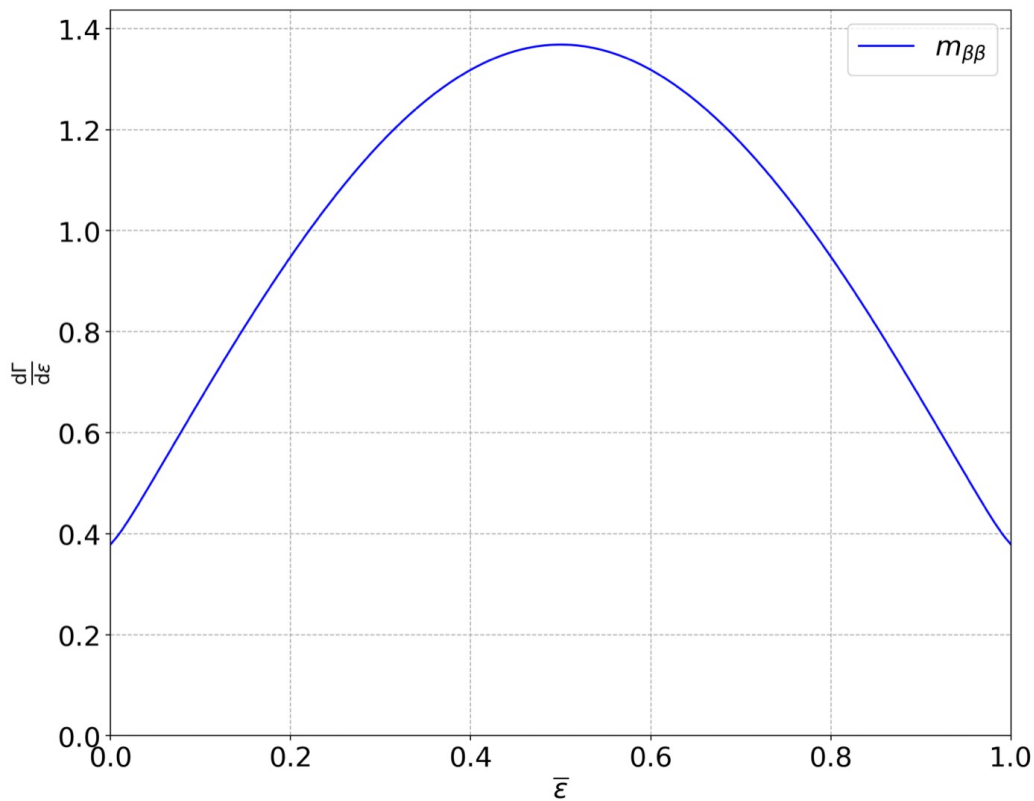
Distinguish 2 operators i, j by

$$R_{ij}(^A X) = \frac{R^{\mathcal{O}_i}(^A X)}{R^{\mathcal{O}_j}(^A X)}$$

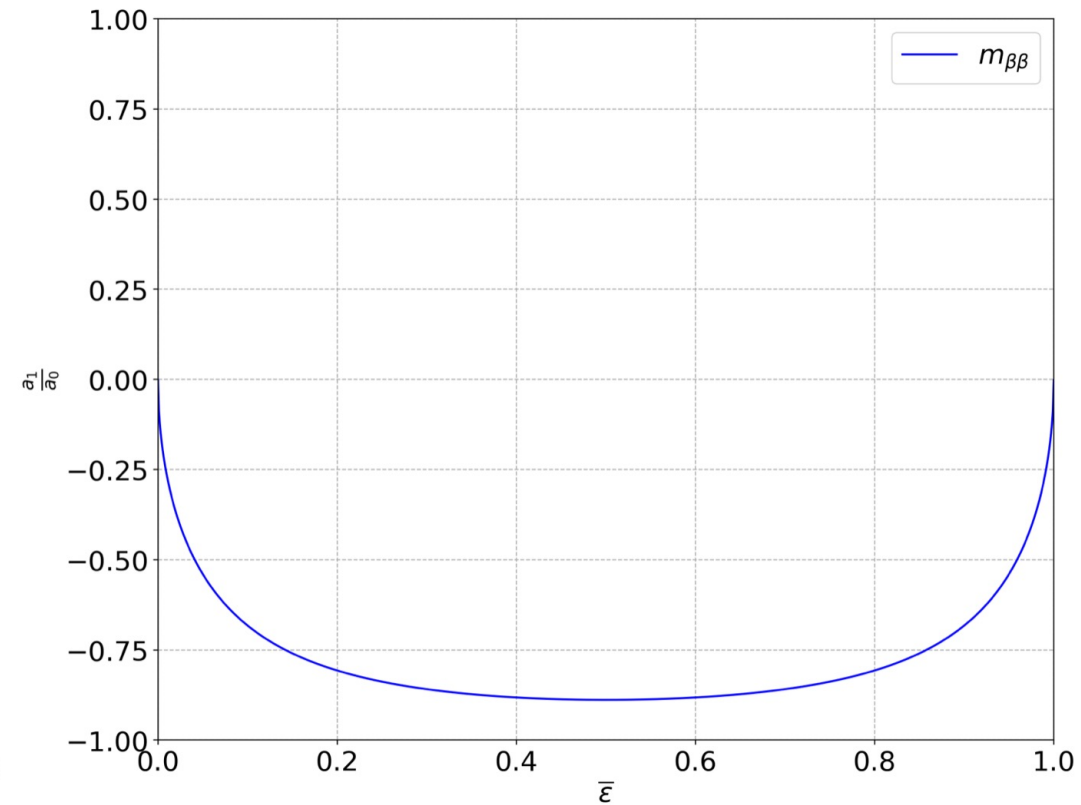
Similar for more complex models

2) + 3) Phase Space Observables

Single Electron Spectra



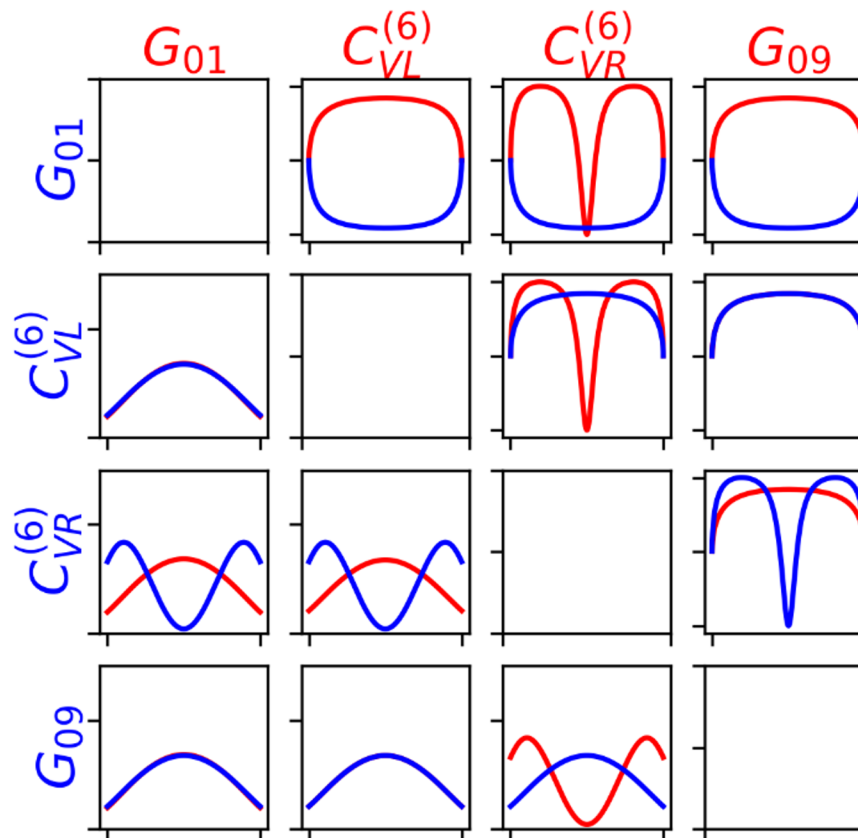
Angular Correlation



2) + 3) Phase Space Observables

→ 4 different groups (plot for ^{136}Xe)

Angular correlation



Normalized
Spectra

Tool for $0\nu\beta\beta$ -models

Tool to study all possible EFT models:

- $0\nu\beta\beta$ observables
- Distinguishability from standard-mechanism
- Operator Limits

Thank you for attention!