MEDEX '19, Prague, May 27-31 2019

# EFT approach to neutrino-less double beta decay

#### Vincenzo Cirigliano Los Alamos National Laboratory



#### Outline

- "End-to-end" Effective Field Theory (EFT) framework for Lepton Number Violation (LNV) and  $0\nu\beta\beta$  and its benefits
- $0\nu\beta\beta$  from light Majorana  $\nu$  exchange mechanism
- $0\nu\beta\beta$  from (multi)TeV-scale dynamics [if time permits]

Special thanks to collaborators: W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, S. Pastore, U. van Kolck, A. Walker-Loud EFT framework for LNV and neutrino-less double beta decay

• Ton-scale  $0 \vee \beta \beta$  searches  $(T_{1/2} > 10^{27-28} \text{ yr})$  will probe at unprecedented levels LNV from a variety of mechanisms



• Ton-scale  $0\nu\beta\beta$  searches (T<sub>1/2</sub> >  $10^{27-28}$  yr) will probe at unprecedented levels LNV from a variety of mechanisms





• Ton-scale  $0\nu\beta\beta$  searches (T<sub>1/2</sub> >  $10^{27-28}$  yr) will probe at unprecedented levels LNV from a variety of mechanisms



• Ton-scale  $0\nu\beta\beta$  searches (T<sub>1/2</sub> >  $10^{27-28}$  yr) will probe at unprecedented levels LNV from a variety of mechanisms



• Ton-scale  $0\nu\beta\beta$  searches (T<sub>1/2</sub> >  $10^{27-28}$  yr) will probe at unprecedented levels LNV from a variety of mechanisms



Impact of 0vββ searches most efficiently analyzed in a BSM-EFT framework, encompassing a large class of underlying models

Hadronization of resulting quarklevel operators is most efficiently and rigorously achieved using chiral EFT techniques

• Ton-scale  $0\nu\beta\beta$  searches (T<sub>1/2</sub> >  $10^{27-28}$  yr) will probe at unprecedented levels LNV from a variety of mechanisms



Impact of 0vββ searches most efficiently analyzed in a BSM-EFT framework, encompassing a large class of underlying models

Hadronization of resulting quarklevel operators is most efficiently and rigorously achieved using chiral EFT techniques

"End-to-end" EFT framework: connecting LNV scale  $\Lambda$  to nuclear scales, with controllable uncertainties

#### EFT framework for $0\nu\beta\beta$



#### EFT framework for $0\nu\beta\beta$



#### EFT framework for $0\nu\beta\beta$



lattice QCD & many-body methods

 $T_{1/2} \begin{bmatrix} \widetilde{C}_i \begin{bmatrix} C_j \end{bmatrix} \end{bmatrix} \sim (m_W / \Lambda)^A (\Lambda_X / m_W)^B (k_F / \Lambda_X)^C$ 

# 0vββ from light Majorana neutrino (dim-5 operator)





Effective Lagrangian just below the weak scale

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{QCD}} - \frac{4G_F}{\sqrt{2}} V_{ud} \,\bar{u}_L \gamma^\mu d_L \,\bar{e}_L \gamma_\mu \nu_{eL} - \frac{m_{\beta\beta}}{2} \,\nu_{eL}^T C \nu_{eL} + \text{H.c.}$$

V. Cirigliano, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729, Phys.Rev. C97 (2018) no.6, 065501



LNV hadronic amplitudes such as nn → ppee receive contributions from broad range of neutrino virtual momenta (q)

Chiral EFT captures contributions from all momentum regions

V. Cirigliano, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729, Phys.Rev. C97 (2018) no.6, 065501



"Hard neutrinos":  
E, 
$$|\mathbf{q}| > \Lambda_X \sim m_N \sim \text{GeV}$$





Short-range  $\Delta L=2$  operators at the hadronic level, still proportional to  $m_{\beta\beta}$ 







Non-local "Neutrino potential" (long- and pion-range) mediating nn→pp



### Anatomy of $0\nu\beta\beta$ amplitude

Figure adapted from Primakoff-Rosen 1969



#### Hard, soft, and potential V

$$\mathbf{V}_{\mathbf{l=2}} = \sum_{a \neq b} \left( V_{\nu,0}^{(a,b)} + V_{\nu,2}^{(a,b)} + \dots \right)$$

$$V_v \sim 1/Q^2$$
,  $1/(\Lambda_X)^2$ , ...  
  
LO N<sup>2</sup>LO

### Anatomy of $0\nu\beta\beta$ amplitude

Figure adapted from Primakoff-Rosen 1969



#### Hard, soft, and potential $\nu$

#### Ultrasoft V

$$\mathbf{V}_{l=2} = \sum_{a \neq b} \left( V_{\nu,0}^{(a,b)} + V_{\nu,2}^{(a,b)} + \dots \right)$$

$$V_v \sim 1/Q^2$$
,  $1/(\Lambda_X)^2$ , ...  
 $\uparrow$   $\uparrow$   
LO N<sup>2</sup>LO

Loop calculable in terms of  $E_n - E_i$  and  $f ||_{\mu}|n > n||^{\mu}|i>$ , that also control  $2\nu\beta\beta$ . Contributes to the amplitude at N<sup>2</sup>LO

EFT justifies the "closure approximation" and quantifies corrections to it

#### Leading order 0vBB potential



• Tree-level exchange of Majorana neutrinos

$$V_{\nu,0}^{(a,b)} = \tau^{(a)+}\tau^{(b)+}\left\{\frac{1}{\mathbf{q}^2}\left\{1 - g_A^2\left[\sigma^{(a)}\cdot\sigma^{(b)} - \sigma^{(a)}\cdot\mathbf{q}\,\sigma^{(b)}\cdot\mathbf{q}\,\frac{2m_\pi^2 + \mathbf{q}^2}{(\mathbf{q}^2 + m_\pi^2)^2}\right]\right\} \quad \begin{array}{l} \text{Hadronic} \\ \text{input: } \mathbf{g}_A \end{array}$$

#### Leading order 0vBB potential



Tree-level exchange of Majorana neutrinos

$$V_{\nu,0}^{(a,b)} = \tau^{(a)+}\tau^{(b)+}\left\{\frac{1}{\mathbf{q}^2}\left\{1 - g_A^2\left[\sigma^{(a)} \cdot \sigma^{(b)} - \sigma^{(a)} \cdot \mathbf{q} \,\sigma^{(b)} \cdot \mathbf{q} \,\frac{2m_\pi^2 + \mathbf{q}^2}{(\mathbf{q}^2 + m_\pi^2)^2}\right]\right\} \quad \begin{array}{l} \text{Hadronic} \\ \text{input: } \mathbf{g}_{\mathsf{A}} \end{array}$$

• Symmetries allow one to write down a contact term

$$V_{\nu,CT}^{(a,b)} = -2 \, \mathbf{g}_{\nu} \, \tau^{(a)+} \tau^{(b)+}$$

 $g_{v} \sim 1/(4\pi F_{\pi})^{2}$  in NDA / Weinberg counting (and hence sub-leading) But is it?

#### Weinberg 1991, Kaplan-Savage-Wise 1996

 Study nn→ppee amplitude (in <sup>1</sup>S<sub>0</sub> channel) with LO strong potential



#### Weinberg 1991, Kaplan-Savage-Wise 1996

 Study nn→ppee amplitude (in <sup>1</sup>S<sub>0</sub> channel) with LO strong potential



 $\tilde{C} \sim 4\pi/(m_N Q) \sim 1/F_{\pi^2}$  from fit to  $a_{NN}$ 



#### Weinberg 1991, Kaplan-Savage-Wise 1996

 Study nn→ppee amplitude (in <sup>1</sup>S<sub>0</sub> channel) with LO strong potential



 $\tilde{C} \sim 4\pi/(m_N Q) \sim 1/F_{\pi^2}$  from fit to  $a_{NN}$ 



#### Weinberg 1991, Kaplan-Savage-Wise 1996

 Study nn→ppee amplitude (in <sup>1</sup>S<sub>0</sub> channel) with LO strong potential



 $\tilde{C} \sim 4\pi/(m_N Q) \sim 1/F_{\pi^2}$  from fit to  $a_{NN}$ 



#### Weinberg 1991, Kaplan-Savage-Wise 1996

 Study nn→ppee amplitude (in <sup>1</sup>S<sub>0</sub> channel) with LO strong potential



 $\tilde{C} \sim 4\pi/(m_N Q) \sim 1/F_{\pi^2}$  from fit to  $a_{NN}$ 

• Renormalization requires contact LNV operator at LO!



• The coupling flows to  $g_v \sim 1/F_{\pi^2} >> 1/(4\pi F_{\pi})^2$ , same order as  $1/q^2$  from tree-level neutrino exchange

### If you don't like Feynman diagrams...

- Same conclusion obtained by solving the Schroedinger equation
  - Use smeared delta function to regulate short range strong potential:  $\widetilde{C} \rightarrow \widetilde{C} (R_S) \sim I/F_{\pi}^2$
  - Compute amplitude



 $\delta^{(3)}(\mathbf{r}) \to \frac{1}{\pi^{3/2} R_s^3} e^{-\frac{r}{R_s^2}}$ 

Scattering states "fully correlated" according to the leading order strong potential in the <sup>1</sup>S<sub>0</sub> channel

### If you don't like Feynman diagrams...

- Same conclusion obtained by solving the Schroedinger equation
  - Use smeared delta function to regulate short range strong potential:  $\widetilde{C} \rightarrow \widetilde{C} (R_S) \sim I/F_{\pi}^2$
  - Compute amplitude

$$\mathcal{A}_{\nu} = \int d^3 \mathbf{r} \ \psi_{\mathbf{p}'}^{-}(\mathbf{r}) V_{\nu,0}(\mathbf{r}) \psi_{\mathbf{p}}^{+}(\mathbf{r})$$

 $\delta^{(3)}(\mathbf{r}) \to \frac{1}{\pi^{3/2} R_c^3} e^{-\frac{r^2}{R_S^2}}$ 

• Logarithmic dependence on  $R_s \Rightarrow$ 

need LO counterterm  $g_{\nu} \sim I/F_{\pi}^2 \log R_S$  to obtain physical, regulatorindependent result



#### Estimating finite part of $g_{\nu}$

• Long term: compute nn→pp in lattice QCD and match to EFT



#### Estimating finite part of $g_{\nu}$

- Long term: compute nn→pp in lattice QCD and match to EFT
- Chiral symmetry relates  $g_v$  to one of two I=2 EM LECs (hard  $\gamma$ 's vs V's)



#### Estimating finite part of $g_{\nu}$

- Long term: compute nn  $\rightarrow$  pp in lattice QCD and match to EFT
- Chiral symmetry relates  $g_v$  to one of two I=2 EM LECs (hard  $\gamma$ 's vs V's)



### $0\nu\beta\beta$ vs EM isospin breaking

- NN observables cannot disentangle  $C_1$  from  $C_2$  (need pions), but provide data-based estimate of  $C_1+C_2$
- C<sub>1</sub> + C<sub>2</sub> controls CIB combination of <sup>1</sup>S<sub>0</sub> scattering lengths a<sub>nn</sub> + a<sub>pp</sub> - 2 a<sub>np</sub>
- Fit to data, including Coulomb potential, pion EM mass splitting, and contact terms confirms the scaling  $C_1 + C_2 \sim 1/F_{\pi^2} >> 1/(4\pi F_{\pi})^2$



## $0\nu\beta\beta$ vs EM isospin breaking

- NN observables cannot disentangle  $C_1$  from  $C_2$  (need pions), but provide data-based estimate of  $C_1+C_2$
- C<sub>1</sub> + C<sub>2</sub> controls CIB combination of <sup>1</sup>S<sub>0</sub> scattering lengths a<sub>nn</sub> + a<sub>pp</sub> - 2 a<sub>np</sub>
- Fit to data, including Coulomb potential, pion EM mass splitting, and contact terms confirms the scaling  $C_1 + C_2 \sim 1/F_{\pi}^2 >> 1/(4\pi F_{\pi})^2$



The EFT analysis survives comparison with data!

The analog of  $e^2(C_1+C_2)$  is included in all high-quality potentials (AV18, CD-Bonn, chiral, ...)

#### Guesstimating numerical impact

V. Cirigliano, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, S. Pastore, M. Piarulli, U. van Kolck, R. Wiringa, 1906.xxxxx



Assume  $g_v \sim (C_1 + C_2)/2$  with  $(C_1 + C_2)$ taken from fit to NN data

Evaluate impact in light nuclei using Variational Monte Carlo, with wavefunctions corresponding to the Norfolk chiral potential [1606.06335]

> $g_v$  contribution sizable in  $\Delta I=2$ transition (due to node): for A=12, A<sub>S</sub>/A<sub>L</sub> = 0.75

#### Guesstimating numerical impact

V. Cirigliano, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, S. Pastore, M. Piarulli, U. van Kolck, R. Wiringa, 1906.xxxxx



Assume  $g_v \sim (C_1 + C_2)/2$  with  $(C_1 + C_2)$ taken from fit to NN data

Evaluate impact in light nuclei using Variational Monte Carlo, with wavefunctions corresponding to the Norfolk chiral potential [1606.06335]

> $g_v$  contribution sizable in  $\Delta I=2$ transition (due to node): for A=12, A<sub>S</sub>/A<sub>L</sub> = 0.75

Transitions of experimental interest (<sup>76</sup>Ge  $\rightarrow$  <sup>76</sup>Se, ... ) have  $\Delta I=2$  (and node)  $\Rightarrow$  expect significant effect!

#### Strategies to determine $g_{\nu}$

- Long term → (I) Lattice QCD;
   (2) Processes sensitive to I=2 interactions with pions and nucleons (get C<sub>1</sub> and C<sub>2</sub>)
- Short term → explore methods to evaluate the forward amplitude W<sup>+</sup>(q)nn
   → W<sup>-</sup>(q)pp for a broad range of q



 Experimental input on (C<sub>1</sub>+C<sub>2</sub>) from CIB in NN scattering can be used to validate the method

# $N^2LO 0\nu\beta\beta$ potential

• Known factorizable corrections to 1-body currents (radii, ...)



• New non-factorizable contributions to  $V_{\nu,2} \sim V_{\nu,0} (k_F/4\pi F_\pi)^2 [\pi-N \text{ loops}]$ and <u>new contact terms</u>]



V. Cirigliano, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729

• 2-body x 1-body current (and <u>another contact</u>...)



Wang-Engel-Yao 1805.10276

# $N^2LO 0\nu\beta\beta$ potential

Calculations of these effects in light and heavy nuclei show O(10%) corrections

• New non-factorizable contributions to  $V_{\nu,2} \sim V_{\nu,0} (k_F/4\pi F_\pi)^2 [\pi-N loops$ and <u>new contact terms]</u>

S. Pastore, J. Carlson, V.C., W. Dekens, E. Mereghetti, R. Wiringa 1710.05026



V.C., J. Engel, E. Mereghetti, in preparation

V. Cirigliano, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729

• 2-body x 1-body current (and <u>another contact</u>...)



Wang-Engel-Yao 1805.10276

#### Ultrasoft neutrino contributions

#### Figure adapted from Primakoff-Rosen 1969



$$T_{\text{usoft}}(\mu_{\text{us}}) = \frac{T_{\text{lept}}}{8\pi^2} \sum_{n} \langle f|J_{\mu}|n\rangle \langle n|J^{\mu}|i\rangle \left\{ (E_2 + E_n - E_i) \left( \log \frac{\mu_{\text{us}}}{2(E_2 + E_n - E_i)} + 1 \right) + 1 \leftrightarrow 2 \right\}$$

V. Cirigliano, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729

- Ultrasoft V's couple to nuclear states: sensitivity to  $E_n E_i$  and  $\langle f ||\mu|n \rangle \langle n||\mu|i \rangle$  that also determine  $2\nu\beta\beta$  amplitude
- $T_{usoft}/T_0 \sim (E_n E_i)/(4\pi k_F) \rightarrow N2LO$  contribution
- $\mu_{us}$  dependence cancels with  $V_{\nu,2}$ : consistency check

# 0vββ from multi-TeV scale dynamics (dim-7, 9, ...operators)



#### Classifying contributions





Vergatos 1982, Faessler, Kovalenko, Simkovic, Schweiger 1996 Prezeau, Ramsey-Musolf, Vogel hep-ph/0303205



Naive dimensional analysis  $\rightarrow V_{\pi\pi}$  dominates for all but one operator

Vergatos 1982, Faessler, Kovalenko, Simkovic, Schweiger 1996 Prezeau, Ramsey-Musolf, Vogel hep-ph/0303205



- Two recent developments:
  - ΠΠ matrix elements now precisely know via direct and indirect lattice QCD calculations



Nicholson et al., 1805/02634



- Two recent developments:
  - ΠΠ matrix elements now precisely know via direct and indirect lattice QCD calculations





- Two recent developments:
  - 2. Renormalization  $\rightarrow V_{\pi\pi}$  and  $V_{NN}$  are both leading order



#### What scales are being probed?

VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, 1806.02780



Bounds reflect dependence on  $\Lambda_{\chi}$  / $\Lambda$  and Q/ $\Lambda_{\chi}$ 

#### **Conclusions & Outlook**

- Ton-scale  $0\nu\beta\beta$  searches will probe LNV from a broad variety of mechanisms high discovery potential, far reaching implications
- EFT approach provides a general framework to:
  - I. Relate  $0\nu\beta\beta$  to underlying LNV dynamics (and collider & cosmology)
  - 2. Organize contributions to hadronic and nuclear matrix elements
    - Identified new leading order short-range contributions
    - Implications for  $m_{\beta\beta}$  not yet clear (size of  $g_{\nu}$  & relative sign)

Improving the theory uncertainty is challenging, but there are exciting prospects thanks to advances in EFT, lattice QCD, and nuclear structure

# Backup

### Estimating finite part of $g_v$ (v2)

- Long term: compute nn→pp in lattice QCD and match to EFT
- Chiral symmetry relates  $g_v$  to one of two I=2 EM LECs (hard  $\gamma$ 's vs V's)



#### EFT-based master formula

• Framework to interpret experiments in terms of high-scale LNV sources



#### EFT-based master formula

• Framework to interpret experiments in terms of high-scale LNV sources



#### EFT-based master formula

• Framework to interpret experiments in terms of high-scale LNV sources



#### A leptoquark example

• Dim-5 ( $m_{\beta\beta}$ ) + Dim-7 operator (leptoquark-induced)



 $\mathcal{C}_{LL\bar{Q}uH} \epsilon_{ij} \left( \bar{Q}_m u \right) \left( L_m^T C L_i \right) H_j$ 

• Same leptonic structure as in  $V_M$  exchange: can cancel  $m_{\beta\beta}$  !!

VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, 1708.09390

#### A leptoquark example

• Dim-5 ( $m_{\beta\beta}$ ) + Dim-7 operator (leptoquark-induced)



• Same leptonic structure as in  $V_M$  exchange: can cancel  $m_{\beta\beta}$  !!

VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, 1708.09390

#### Left-Right symmetric model example

• Generates ops. at dim-5 (m<sub>ββ</sub>) + dim-7 & dim-9



Chirally enhanced for  $(\xi \neq 0)$ 



VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, 1806.02780

#### Left-Right symmetric model example

- Generates ops. at dim-5 (m<sub>ββ</sub>) + dim-7 & dim-9
- Dim-9 contribution can be dominant in NH

Illustrative LHC-safe parameters

 $m_{W_R} = 4.5 \text{ TeV}$   $m_{\Delta_R} = 10 \text{ TeV}$   $m_{\nu_R} = O(10 \text{ TeV})$   $U_R = U_{\text{PMNS}}$ 



VC, W. Dekens, J. de Vries, M. Graesser, E. Mereghetti, 1806.02780