

Neutrino-Nuclear Responses and the Effective Value of Weak Axial Coupling

Jouni Suhonen

Department of Physics, University of Jyväskylä

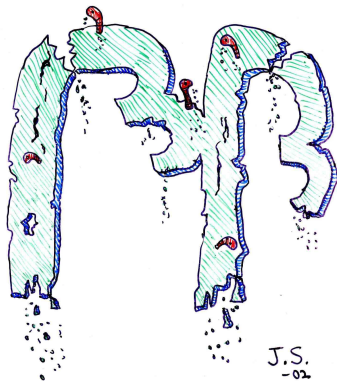
Matrix Elements for Double-beta-decay EXperiments (MEDEX'19)
Prague, Czech Republic, May 27 - 31, 2019



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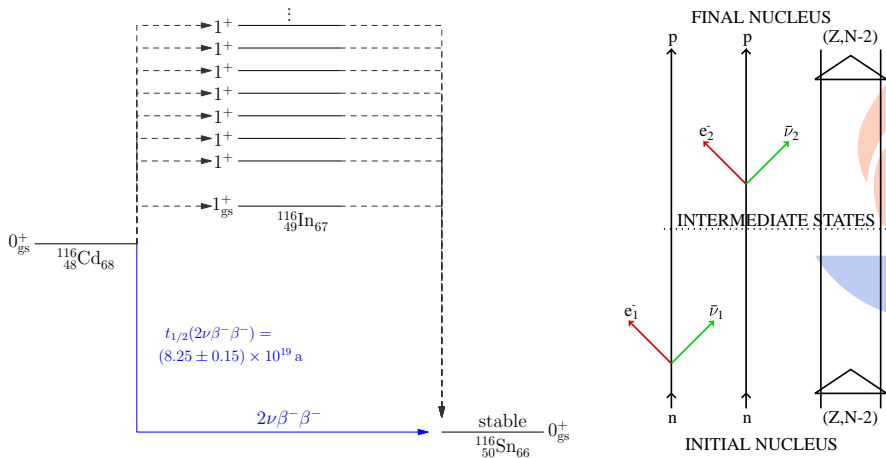
- Intro: DBD rates
- Effective value of g_A
- Impact on $0\nu\beta\beta$ NMEs
- OMC and $0\nu\beta\beta$: Twins?
- About reactor- $\bar{\nu}$ anomaly

INTRO: Rates of double beta decay



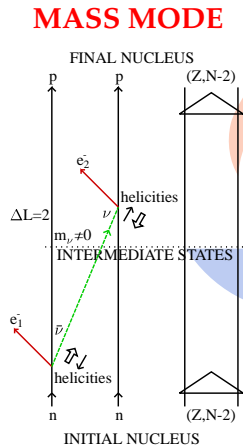
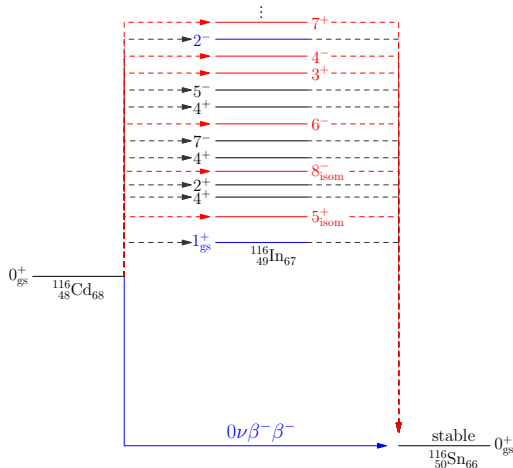
See the recent review: H. Ejiri, J. Suhonen, K. Zuber, [Neutrino-nuclear responses for astro-neutrinos, single beta decays and double beta decays](#), Physics Reports 797 (2019) 1–102

Two-Neutrino Double Beta Decay of ^{116}Cd



$$2\nu\beta\beta - \text{rate} \sim \left| M_{\text{GTGT}}^{(2\nu)} \right|^2 = (g_A)^4 \left| \sum_{m,n} \frac{M_L(1_m^+) M_R(1_n^+)}{D_m} \right|^2$$

Neutrinoless Double Beta Decay of ^{116}Cd



$$0\nu\beta\beta - \text{rate} \sim \left| M_{\text{GTGT}}^{(0\nu)} \right|^2 = (g_{A,0\nu})^4 \left| \sum_{J^\pi} \langle 0^+_{\text{f}} || \mathcal{O}_{\text{GTGT}}^{(0\nu)}(J^\pi) || 0^+_{\text{i}} \rangle \right|^2$$

Studies of the effective values of the weak couplings (g_V, g_A, g_P)

Motivation:

Effective values of weak couplings are involved in all weak processes, and thus have impact on

- **studies of rare β decays**
- **processes in neutrino physics** ($\beta\beta$ decay, low-energy (anti)neutrino-nucleus scattering, **nuclear muon capture**, ...)
- **processes in astrophysics** (allowed and forbidden β decays, (anti)neutrino-nucleus scattering cross sections, ...)

Sources of quenching or enhancement of g_A

The free-nucleon value of g_A is changed in nuclear-structure calculations by:

- Non-nucleonic degrees of freedom (e.g. Δ resonances)
- Effects beyond the impulse approximation (e.g. two-body meson-exchange currents)
- Deficiencies in nuclear many-body approaches (e.g. restricted valence spaces, lacking many-body configurations, omission of three-body nuclear forces)

Definitions

See also: “Value of the axial-vector coupling strength in β and $\beta\beta$ decays: A review” published in **Frontiers in Physics** 5 (2017) 55.

Nucleon weak current in a nucleus:

$$j_N^\mu = g_V \gamma^\mu - g_A \gamma^\mu \gamma^5$$

Quenching:

$$q = g_A / g_A^{\text{free}}$$

Free value of g_A (Particle Data Group 2016) from the decay of free neutron:

$$g_A^{\text{free}} = 1.2723(23)$$

Effective value of g_A :

$$g_A^{\text{eff}} = q g_A^{\text{free}}$$

Gamow-Teller β and $2\nu\beta\beta$ decays

There are data on:

Gamow-Teller β transitions and **$2\nu\beta\beta$ transitions**

For these we have the low-momentum-exchange limit

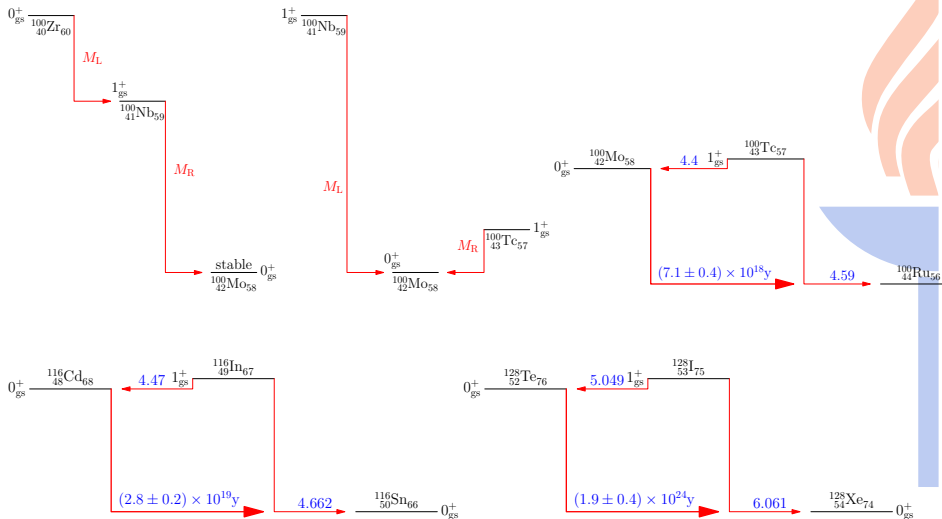
$$g_{A,0\nu}(J^\pi) \xrightarrow{q \rightarrow 0} g_A(J^\pi),$$

where the usual convention is $g_A \equiv g_A(1^+)$

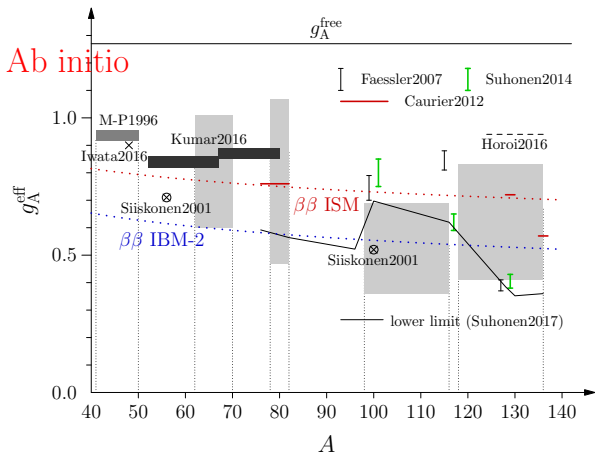
Nuclear models:

ISM (Interacting Shell Model)
pnQRPA (proton-neutron QRPA)
IBM-2 (microscopic interacting boson model)

Typical Gamow-Teller β and $2\nu\beta\beta$ transitions



Results extracted from the GT $\beta+2\nu\beta\beta$ calculations



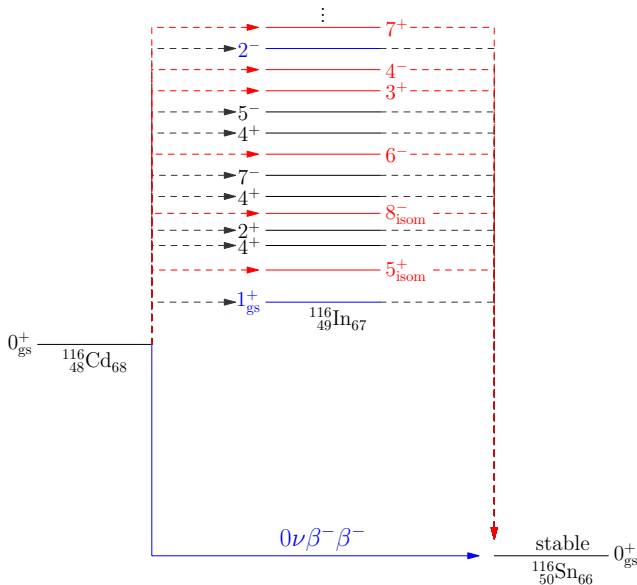
Ab initio: P. Gysbers *et al.*, Nature Physics 15 (2019) 428

- Faessler2007: **pnQRPA** A. Faessler *et al.*, arXiv 0711.3996v1 [Nucl-th]
- Suhonen2014: **pnQRPA** J. Suhonen *et al.*, Nucl. Phys. A 924 (2014) 1
- Suhonen2017: **pnQRPA** J. Suhonen, Phys. Rev. C 96 (2017) 055501
- Courier2012: **ISM** E. Courier *et al.*, Phys. Lett. B 711 (2012) 62
- Horoi2016: **ISM** M. Horoi *et al.*, Phys. Rev. C 93 (2016) 024308
- M-P1996: **ISM** G. Martínez-Pinedo *et al.*, Phys. Rev. C 53 (1996) R2602
- Iwata2016: **ISM** Y. Iwata *et al.*, Phys. Rev. Lett. 116 (2016) 112502
- Kumar2016: **ISM** V. Kumar *et al.*, J. Phys. G 43 (2016) 105104 Phys. Lett. B 711 (2012) 62
- Siiskonen2001: **ISM** T. Siiskonen *et al.*, Phys. Rev. C 63 (2001) 055501
- $\beta\beta$ ISM and IBM-2: J. Barea *et al.*, Phys. Rev. C 87 (2013) 014315
- Light hatched regions: **pnQRPA** H. Ejiri *et al.*, J. Phys. G 42 (2015) 055201 ; P. Pirinen *et al.*, Phys. Rev. C 91 (2015) 054309 ; F. Deppisch *et al.*, Phys. Rev. C 94 (2016) 055501

Results from:

Quenching of $g_A(J^\pi)$
as derived from
 β decays
of forbiddenness K

INCENTIVE: $0\nu\beta\beta$ decay through the higher angular-momentum states



Novel approach: Spectrum-shape method (SSM)

Results for higher-multipole transitions:

Effective value of $g_A(J^\pi)$
as derived from
electron spectra of
forbidden non-unique β decays

Spectrum shape of higher-forbidden non-unique β decays

Half-life:

$$t_{1/2} = \kappa / \tilde{C}.$$

Dimensionless integrated shape function:

$$\tilde{C} = \int_1^{w_0} C(w_e) p w_e (w_0 - w_e)^2 F_0(Z_f, w_e) dw_e.$$

Shape factor:

$$C(w_e) = \sum_{k_e, k_\nu, K} \lambda_{k_e} \left[M_K(k_e, k_\nu)^2 + m_K(k_e, k_\nu)^2 - \frac{2\gamma_{k_e}}{k_e w_e} M_K(k_e, k_\nu) m_K(k_e, k_\nu) \right],$$

where

$$\lambda_{k_e} = \frac{F_{k_e-1}(Z, w_e)}{F_0(Z, w_e)}; \quad \gamma_{k_e} = \sqrt{k_e^2 - (\alpha Z_f)^2},$$

$F_{k-1}(Z, w_e)$ being the generalized Fermi function.

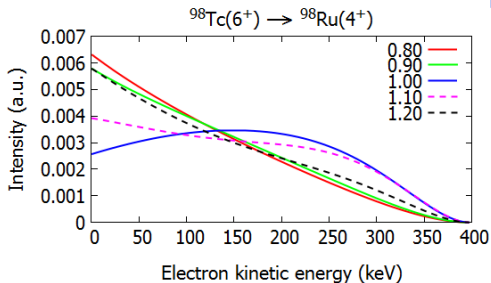
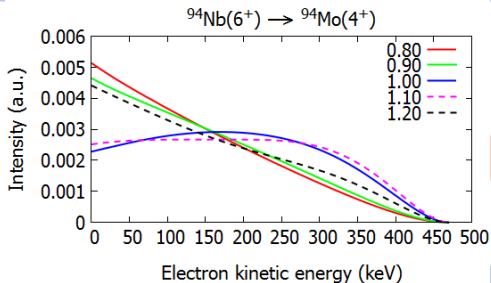
Decomposition of the shape factor:

$$C(w_e) = g_V^2 C_V(w_e) + g_A^2 C_A(w_e) + g_V g_A C_{VA}(w_e).$$

ISM-computed β spectra for different values of g_A

Normalized ISM-computed
electron spectra for the
 $2nd$ -forbidden nonunique
 β^- decays of ^{94}Nb and ^{98}Tc
($g_V = 1.0$).

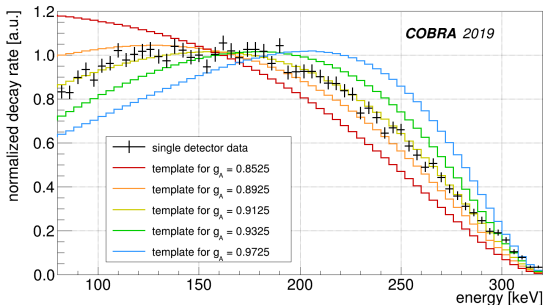
From: J. Kostensalo, J. Suhonen,
 g_A -driven shapes of electron
spectra of forbidden β decays in
the nuclear shell model, Phys.
Rev. C 96 (2017) 024317



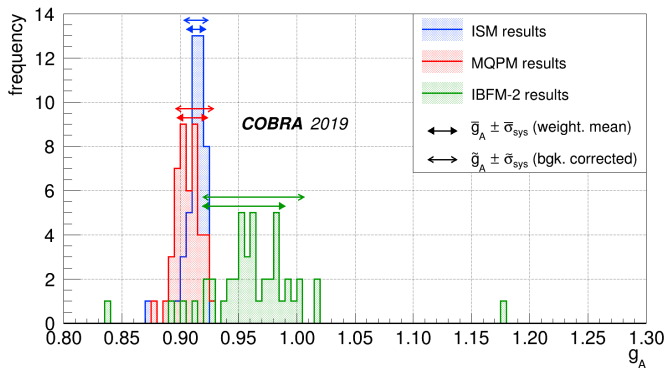
Example: Decay of ^{113}Cd – Comparison with data

Normalized electron spectra
for the 4th-forbidden
nonunique β^- decay
 $^{113}\text{Cd}(1/2^+) \rightarrow ^{113}\text{In}(9/2^+)$
($g_V = 1.0$).

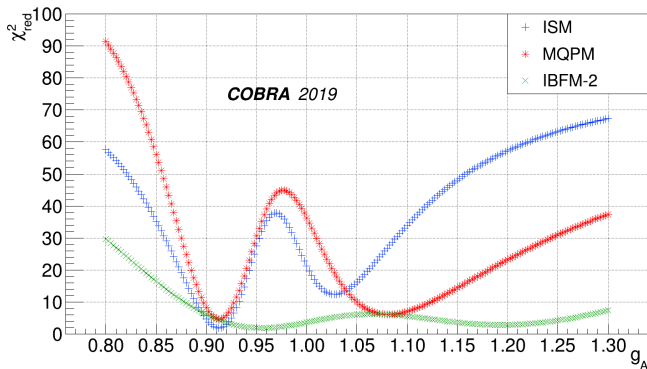
Experimental data from
The **COBRA** collaboration:
L. Bodenstein-Dresler *et al.*,
arXiv:1806.02254 [nucl-ex]



Distribution of the best-match g_A values from 44 detector units



Example: Decay of ^{113}Cd – Comparison with data



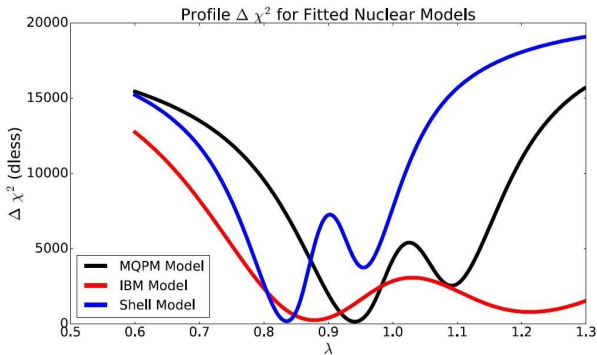
$$\begin{aligned}\bar{g}_A(\text{ISM}) &= 0.914 \pm 0.008 \\ \bar{g}_A(\text{MQPM}) &= 0.910 \pm 0.013 \\ \bar{g}_A(\text{IBFM-2}) &= 0.955 \pm 0.035\end{aligned}$$

Example: Decay of ^{115}In – Comparison with data

Normalized electron spectra
for the 4th-forbidden
nonunique β^- decay
 $^{115}\text{In}(9/2^+) \rightarrow ^{115}\text{Sn}(1/2^+)$
($g_V = 1.0$).

Result from

The MIT-CSNSM-Jyvaskylä
collaboration: A. Leder *et al.*,
to be submitted.



$$\begin{aligned}\bar{g}_A(\text{ISM}) &= 0.83 \pm 0.03 \\ \bar{g}_A(\text{IBFM-2}) &= 0.88 \pm 0.06 \\ \bar{g}_A(\text{MQPM}) &= 0.94^{+0.03}_{-0.04}\end{aligned}$$

Effects of quenched values of g_A

Results from:

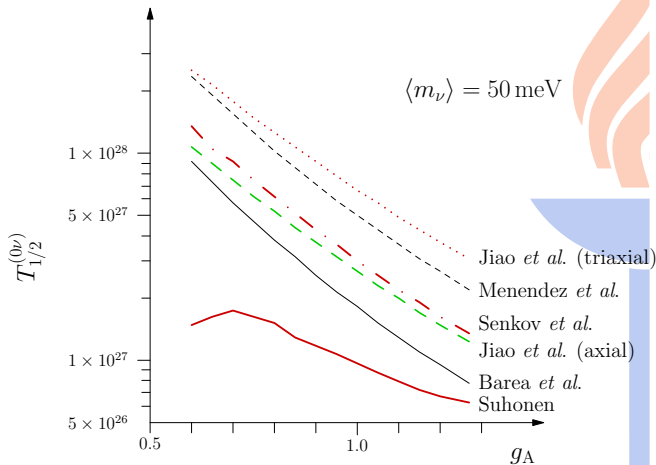
Effects of a quenched g_A on NMEs of $0\nu\beta\beta$ decays:

$$\left[T_{1/2}^{(0\nu)}\right]^{-1} = (g_{A,0\nu})^4 G^{(0\nu)} |M^{(0\nu)}|^2 \left(\frac{\langle m_\nu \rangle}{m_e}\right)^2$$

$$M^{(0\nu)} = M_{\text{GT}}^{(0\nu)} - \left(\frac{g_V}{g_{A,0\nu}}\right)^2 M_{\text{F}}^{(0\nu)} + M_{\text{T}}^{(0\nu)}$$

Example: $0\nu\beta\beta$ NMEs of ^{76}Ge , effect on the half-life

- **Jiao *et al.*:** Phys. Rev. C 96 (2017) 054310 (GCM+ISM)
- **Menendez *et al.*:** Nucl. Phys. A 818 (2009) 139 (ISM)
- **Senkov *et al.*:** Phys. Rev. C 93 (2016) 044334 (ISM)
- **Barea *et al.*:** Phys. Rev. C 91 (2015) 034304 (IBM-2)
- **Suhonen:** Phys. Rev. C 96 (2017) 055501 (pnQRPA + isospin restoration + data on $2\nu\beta\beta$)



OMC as a probe of $0\nu\beta\beta$ NMEs

There are and will be more data on:

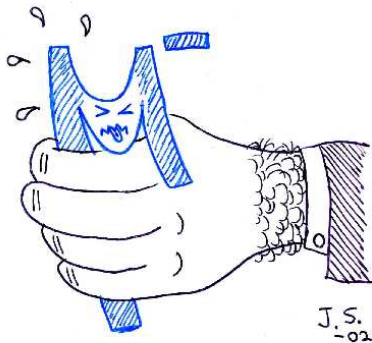
CAPTURE RATES

OF

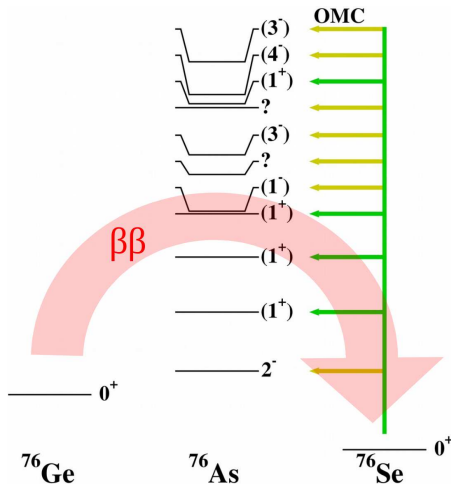
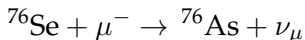
ORDINARY MUON CAPTURE (OMC)

In particular:

OMC STRENGTH FUNCTIONS



Ordinary Muon Capture on ^{76}Se



$$m_\mu c^2 \approx 105 \text{ MeV}$$

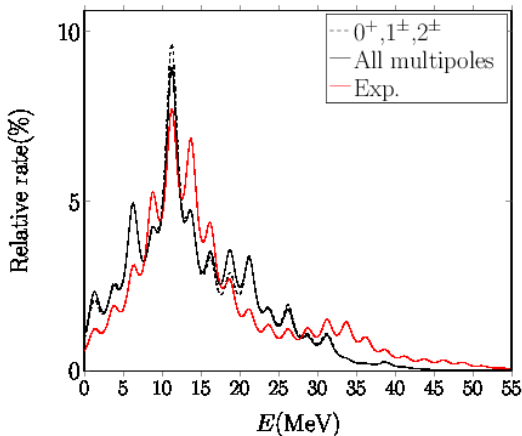


- OMC and $0\nu\beta\beta$ operate in the $q \approx 100 \text{ MeV}$ momentum-exchange region $\Rightarrow g_{A,0\nu}(J^\pi)$
- Induced currents ($g_P!$) are activated

Experiments:

RCNP, Osaka ; J-PARC MLE, Japan ; PSI, Villigen, Switzerland

Comparison of experimental and computed rates of OMC on ^{100}Mo (See: L. Jokiniemi, Wednesday 12:00)



Experiments: MuSIC beam channel at RCNP (Research Center for Nuclear Physics), Osaka, Japan
D2 beam channel in J-PARC (Japan Proton Accelerator Research Complex) MLF, Ibaraki, Japan

First evidence on OMC giant resonance: L. Jokiniemi, J. Suhonen, H. Ejiri, I.H. Hashim, Pinning down the strength function for ordinary muon capture on ^{100}Mo , Phys. Lett. B, submitted.

Novel application of electron spectra of forbidden decays

Try to investigate:

Reactor- $\bar{\nu}$ anomaly
and
the spectral shoulder

Neutrino-related anomalies imply oscillations to sterile neutrinos

See: L. Hayen, Tuesday 15:45 and J. Kostensalo, Thursday 12:00

Sterile neutrinos:

The gallium anomaly

The reactor antineutrino anomaly

imply oscillations of the “ordinary” neutrinos (ν_e, ν_μ, ν_τ) to

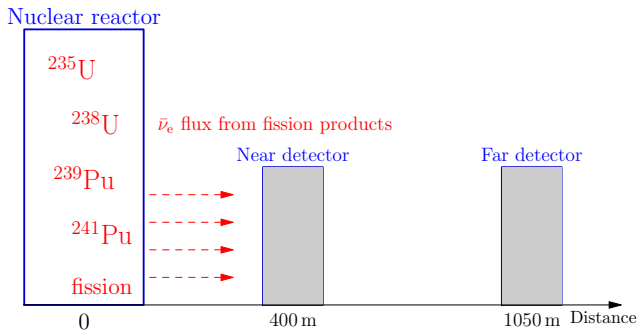
STERILE NEUTRINO

in the mass range of a few eV

But what is the reactor antineutrino anomaly?

The reactor antineutrino anomaly

The $\bar{\nu}_e$ flux from reactors has been measured in **short-baseline neutrino-oscillation experiments**¹: **Daya Bay** (in Daya Bay, China; 6 reactors, 8 detectors), **RENO** (South Korea; 2 detectors 294m and 1383 m from 6 reactors) and **Double Chooz** (Chooz, France, 2 detectors 400m and 1050 m from 2 reactors, schematic figure below).



¹RENO: Phys. Rev. Lett. 108 (2012) 191802; Double Chooz: J. High Energy Phys. 2014 (2014) 86; Daya Bay: Phys. Rev. Lett. 116 (2016) 061801.

The neutrino-flux measurements find:

The reactor $\bar{\nu}_e$ anomaly:

The measured flux is some **5% smaller** than that predicted from the β decays of the fission yields of the reactor fuel

\Rightarrow ?
 \Rightarrow Oscillations to STERILE NEUTRINOS

The bump anomaly:

There is an unexpected **bump at 4 – 6 MeV (spectral shoulder)** in the measured $\bar{\nu}_e$ spectrum.

\Rightarrow ???

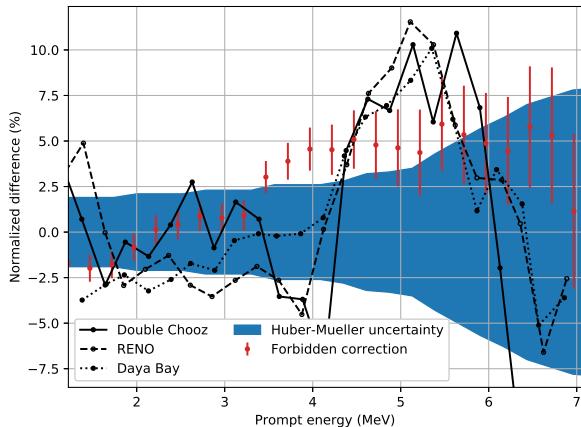
Results from the analyses including the β spectra

Taking into account the
(first-forbidden)
decays of

$^{86}\text{Br}(0^+)$, $^{86}\text{Br}(2^+)$, ^{87}Se , ^{88}Rb ,
 $^{89}\text{Br}(3/2^+)$, $^{89}\text{Br}(5/2^+)$, ^{90}Rb ,
 $^{91}\text{Kr}(5/2^-)$, $^{91}\text{Kr}(3/2^-)$, ^{92}Rb ,
 ^{92}Y , ^{93}Rb , $^{94}\text{Y}(0^+)$, $^{94}\text{Y}(0^+)$,
 $^{95}\text{Rb}(7/2^+)$, $^{95}\text{Rb}(3/2^+)$, ^{95}Sr ,
 ^{96}Y , ^{97}Y , ^{98}Y , ^{133}Sn , $^{134m}\text{Sb}(6^+)$,
 $^{134m}\text{Sb}(6^+?)$, ^{135}Te , ^{136m}I , ^{137}I ,
 ^{138}I , ^{139}Xe , ^{140}Cs , ^{142}Cs

decreases the $\bar{\nu}$ flux by
few % !

See: L. Hayen, J. Kostensalo, N. Severijns, J. Suhonen, First-forbidden transitions in reactor antineutrino spectra, Phys. Rev. C 99 (2019) 031301(R)



The spectral sholder appears due to forbidden
spectral corrections !

Conclusions and Outlook

Conclusions:

- The **effective value of g_A** is involved in all weak processes, and thus has impact on **studies of rare β decays, neutrino physics and astrophysics**
- The long chain of ISM calculations and the recent pnQRPA and IBM-2 calculations of Gamow-Teller β decays and $2\nu\beta\beta$ decays are surprisingly! **consistent with each other** and clearly point to a **A -dependent quenched g_A**
- The **spectrum-shape method (SSM)** for forbidden non-unique β decays is a **robust tool** (largely independent of the nuclear model, the assumed Hamiltonian and mean field) to search for the **effective value of g_A** and to try to solve other problems, like those related to the **reactor- $\bar{\nu}$ spectra**: Proper account of the spectral shapes of **first-forbidden β decays** is instrumental in the quest for the solution to the anomaly.
- The **OMC** can test the weak axial couplings at the **momentum-exchange region relevant for the $0\nu\beta\beta$ decay**

Outlook:

- Urge **measurements of the β spectra** for the interesting decays amenable to the SSM
- **Measurements of the OMC rates** for the $0\nu\beta\beta$ -decay daughters will yield important information on the (induced) axial couplings relevant for $0\nu\beta\beta$ decay

The end

THANKS FOR PATIENCE!